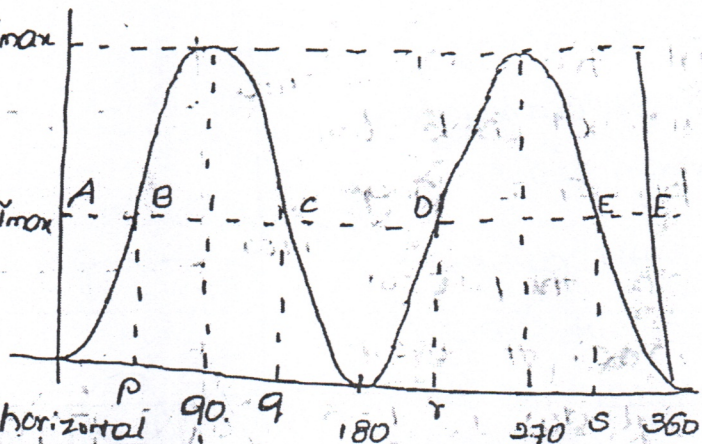


TURNING MOMENT DIAGRAMS

The turning moment diagram is a graphical representation of Crank for various position of Crank it is plotted on Cartesian points. In which turning moment taken as ordinate and Crank angle taken as abscissa.

Turning moment diagram for single cylinder double acting steam engine:-

The turning diagram for single cylinder double acting steam engine shown in fig the vertical line up



turning moment and horizontal line represent Crank angle (θ)

$$T = F_p \times r \left[ \sin \theta + \frac{\sin 2\theta}{2\sqrt{n^2 - \sin^2 \theta}} \right]$$

$F_p$  = piston effort

$r$  = radius of Crank

$n$  = radius of connecting rod to radius of Crank

$\theta$  = angle turn by Crank from inner dead center

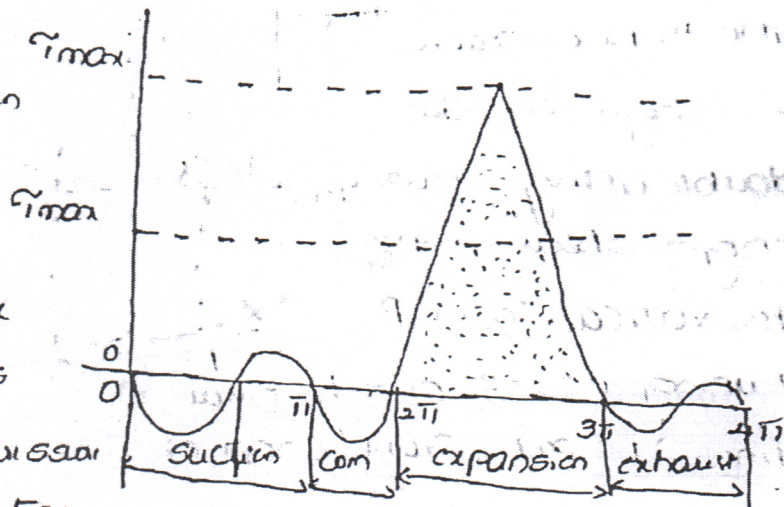
From above expression will be that turning moment is zero  $\theta = 0$ . It is maximum the crank angle at  $90^\circ$  and it is again zero at  $180^\circ$ . This is shown by a.b.c.

Since the work done is the product turning moment and crank angle. The area of turning moment diagram the work done per revolution.

Turning moment diagram for 4-stroke internal combustion engine:

The four stroke internal combustion engine having  $720^\circ$  angle

Since the pressure inside the engine cylinder is less than the atm. pressure during suction stroke,



therefore the negative loop is

formed shown in fig. During compression stroke work is done therefore high negative loop is formed

during expansion (or) working stroke the fuel burns and gas expand that is a large +ve loop in this flow the work is done by the gas. during exhaust stroke the work is done on the gas. therefore -ve loop is formed

## Fluctuation of energy:

The variations of energy above and below the mean torque is called fluctuations of energy.

## Maximum fluctuation of energy

The difference b/w maximum & minimum energies is known as maximum fluctuation of energy

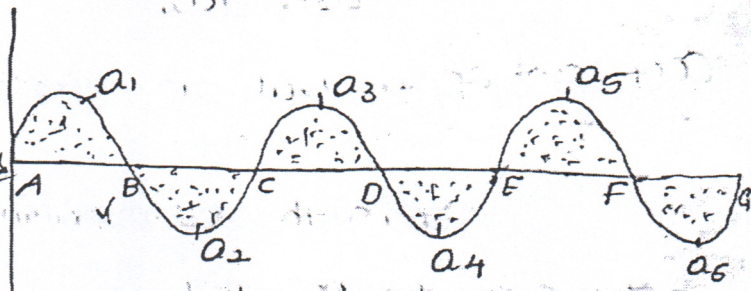
## Determination of maximum fluctuation of energy:

The diagram shows

turning moment diagram

from multi cylinder engine the horizontal

line represent mean torque



Let

$a_1, a_3, a_5$  are above mean torque line

$a_2, a_4, a_6$  are the area below mean torque line

Let the energy in fly wheel at A = E then B = E +  $a_1$

$$\text{energy at C} = E + a_1 - a_2$$

$$D = E + a_1 - a_2 + a_3$$

$$E = E + a_1 - a_2 + a_3 - a_4$$

$$F = E + a_1 - a_2 + a_3 - a_4 + a_5$$

$$G = E + a_1 - a_2 + a_3 - a_4 + a_5 - a_6 = E$$

Let us suppose the potential energy at B

$$B = E + a_1$$

least energy at E

$$E = E + a_1 - a_2 + a_3 - a_4$$

maximum fluctuation energy  $\Delta E =$

maximum energy - minimum energy

$$\Delta E = (E + a_1) - (E + a_1 - a_2 + a_3 - a_4)$$

$$= a_2 - a_3 + a_4$$

Coefficient of fluctuation of energy =

~ ~ ~ ~ ~

It is the ratio maximum fluctuation of energy

to work done per cycle

$$C_E = \frac{\text{maximum fluctuation of energy}}{\text{work done per cycle}}$$

work done per cycle

$$\tau_{\text{mean}} \times \theta$$

$\theta =$  angle turned in one revolution

$\theta = 2\pi$  in case of 2-stroke

$\theta = 4\pi$  (4-stroke)

$$\tau_{\text{mean}} = \frac{P \times 60}{2\pi N}$$

Work done per cycle also obtain =  $P \times \frac{60}{n}$

$n$  = no. of stroke per minute

$$n = \frac{N}{2} \text{ (4-stroke)}$$

$$n = N \text{ (2-stroke)}$$

Fly-wheel:

A fly wheel is used in machines, serves as a reservoir it stores energy when supply of energy is more than requirement and releases when requirement is more than supply.

Coefficient of fluctuation speed:

It is the ratio maximum fluctuation of speed to mean speed

Let  $N_1, N_2$  = maximum & minimum speed

$$N = \frac{N_1 + N_2}{2}$$

Coefficient of fluctuation energy speed

$$C_s = \frac{N_1 - N_2}{N}$$

$$= \frac{2(N_1 - N_2)}{N_1 + N_2}$$

Coefficient of steadiness:

It is the reciprocal of coefficient fluctuation

of speed

$$m = \frac{1}{C_s} = \frac{N_1 + N_2}{2(N_1 - N_2)}$$

Energy stored in flywheel :-

We know that the flywheel stores energy when its speed increases than requirement and it gives energy and speed decreases

Let  $m$  = mass of flywheel in (kg)

$k$  = radius of gyration

$I$  = mass moment of inertia about its axis of rotation

$$I = mk^2$$

$N_1, N_2$  = maximum & minimum speed

$\omega_1, \omega_2$  = angular speed maximum & minimum

$N$  = mean speed

$C_s$  = Coefficient of fluctuation speed

N.K.T

mean kinetic energy of flywheel

$$E = \frac{1}{2} I \omega^2$$

$$= \frac{1}{2} mk^2 \omega^2$$

As the speed of flywheel changes  $\omega_1, \omega_2$  then maximum fluctuation of energy

$$\Delta E = \text{Maximum} - \text{minimum}$$

$$= \frac{1}{2} mk^2 \omega_1^2 - \frac{1}{2} mk^2 \omega_2^2$$

$$= \frac{1}{2} mk^2 [\omega_1^2 - \omega_2^2]$$

$$= \frac{1}{2} mk^2 (\omega_1 + \omega_2) (\omega_1 - \omega_2)$$

$$\Delta E = \frac{(w_1 + w_2)(\omega_1 - \omega_2)}{2} \times \Sigma$$

$$\Delta E = \Sigma w (\omega_1 - \omega_2)$$

$$\Delta E = \Sigma w^v \frac{(\omega_1 - \omega_2)}{w}$$

$$\Sigma \Sigma w^v C_s$$

$$C_s = \frac{\omega_1 - \omega_2}{w}$$

$$\Delta E = 2 \times \frac{1}{2} \Sigma w^v C_s$$

$$\Delta E = \Sigma E \times C_s$$

The radius of gyration is taken equal to mean radius 'r' because the thickness of rim is very small compared to diameter of rim. substituting  $k=r$

$$\Delta E = m R^v w^v C_s$$

$$= m v^v C_s \quad [v = r\omega]$$

The mass of flywheel of engine is 6.5 tonnes and radius of gyration 1.8m is born from turning moment diagram the fluctuation of energy 68 kN-m, the mean speed 150 rpm find maximum & minimum speed

Given

$$m = 6.5 \times 1000$$

$$= 6500 \text{ N}$$

$$k = 1.8 \text{ m}$$

$$\Delta E = 68 \times 10^3 \text{ N-m}$$

$$N = 150 \text{ rpm}$$

$$N = \frac{N_1 + N_2}{2}$$

$$150 = \frac{N_1 + N_2}{2}$$

$$N_1 + N_2 = 300 \rightarrow (1)$$

$$\Delta E = \frac{\pi^2}{900} m k^2 N (N_1 - N_2)$$

$$68 \times 10^3 = \frac{\pi^2}{900} (6500) (1.8)^2 (50) (N_1 - N_2)$$

$$N_1 - N_2 = 1.96 = 2 \rightarrow (2)$$

from (1) & (2)

$$N_1 = 151 \text{ rpm}$$

$$N_2 = 149 \text{ rpm}$$

A horizontal cross compound steam engine develops 300 kW at 90 rpm the coefficient of fluctuation of energy as found from the turning moment diagram. fluctuation speed is kept within  $\pm 0.5\%$  of mean speed find the weight of flywheel required the radius of gyration is 2m

Given

$$P = 300 \text{ kW}$$

$$N = 90 \text{ rpm}$$

$$C_E = 0.1$$

$$C_S = \pm 0.5\% = \frac{N_1 - N_2}{N}$$

$$k = 2 \text{ m}$$

$$\omega_1 - \omega_2 = 0.5 + 0.5 \omega$$

$$\omega_1 - \omega_2 = 0.01 \omega$$

$$\frac{\omega_1 - \omega_2}{\omega} = 0.01$$

$$\omega = \frac{2\pi N}{60}$$

$$= 9.42 \text{ rad/sec}$$



$$\text{Coefficient of speed } C_s = \frac{(\omega_1 - \omega_2) \omega}{\omega}$$

$$C_s = 0.01$$

N.K.T work done per cycle

$$= \frac{P \times 60}{n}$$

$$= \frac{300 (60)}{90}$$

$$= 2 \times 10^5 \text{ N/m}$$

Maximum fluctuation of energy

$$\Delta E = \text{N.K.T work per cycle} \times C_s$$

$$= 2 \times 10^5 \times 0.01$$

$$= 2 \times 10^4 \text{ N-m}$$

$$\therefore \Delta E = m k^2 \omega^2 C_s$$

$$2 \times 10^4 = m (2)^2 (4.42)^2 (0.01)$$

$$m = 5634.6 \text{ kg}$$

The turning moment diagram of a petrol engine is drawn to the following scales, turning moment 1mm = 5 N/m, crank angle 1mm the turning moment diagram repeat every half revolution of engine and areas above & below mean turning moment line taking order 295, 685, 40, 340, 960, 270 mm<sup>2</sup> the rotating part are equivalent to a mass of 50 kg and radius of gyration 130 mm. determine coefficient fluctuation of speed when engine runs at 1800 rpm?

$$m = 50 \text{ kg}$$

$$N = 1800 \text{ rpm}$$

$$r = 130 \text{ mm} = 0.13 \text{ m}$$

$$\omega = \frac{2\pi N}{60} = \frac{2\pi (1800)}{60} = 188.49 \text{ rad/sec}$$

$$A = E$$

$$B = E + 295$$

$$C = E + 295 - 685$$

$$= E - 390$$

$$D = E - 390 + 40$$

$$= E - 350$$

$$E = E - 350 - 340$$

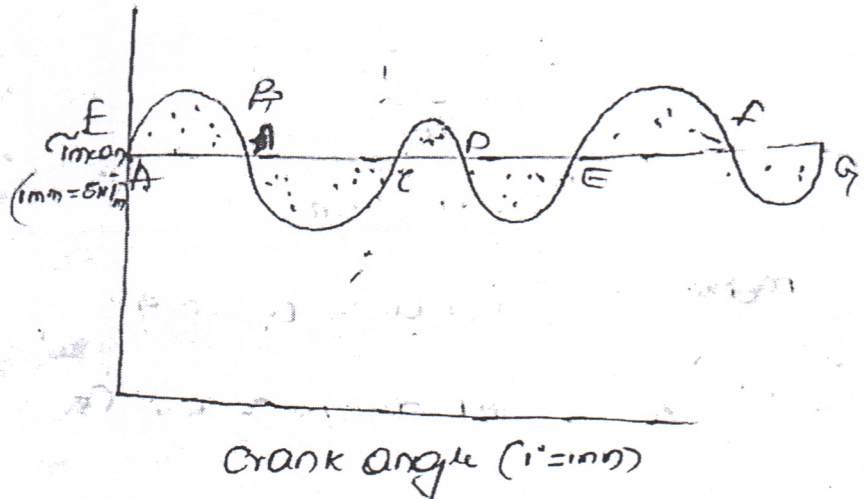
$$= E - 690$$

$$F = E - 690 + 960$$

$$= E + 270$$

$$G = E + 270 - 270$$

$$G = E$$



$$\text{maximum} = E + 295$$

$$\text{minimum} = E - 690$$

$$\Delta E = \text{max} - \text{min}$$

$$= E + 295 - (E - 690)$$

$$= 985$$

$$\Delta E = \frac{985 \times 5 \times \pi}{180}$$

$$\Delta E = 85.95 \text{ N.m}$$

$$\Delta E = m k^2 \omega^2 C_s$$

$$8595 = (50) (0.13)^2 (188.49)^2 C_s$$

$$C_s = 0.002$$

The turning moment diagram of multi cylinder engine is drawn as scale  $1 \text{ mm} = 600 \text{ N}\cdot\text{m}$  vertically,  $1 \text{ mm} = 3^\circ$  horizontally. The interchanged areas b/w the output torque curve & the mean resistance line taken in order from one end are as follows  $+52, -124, +92, -140, +85, -72, \& +107 \text{ mm}^2$  when the engine is running at  $600 \text{ rpm}$ . If the total fluctuation of speed is not exceed  $\pm 1.5\%$  of mean. Find necessary mass of fly wheel of radius  $(0.5) \text{ m}$ .

Given

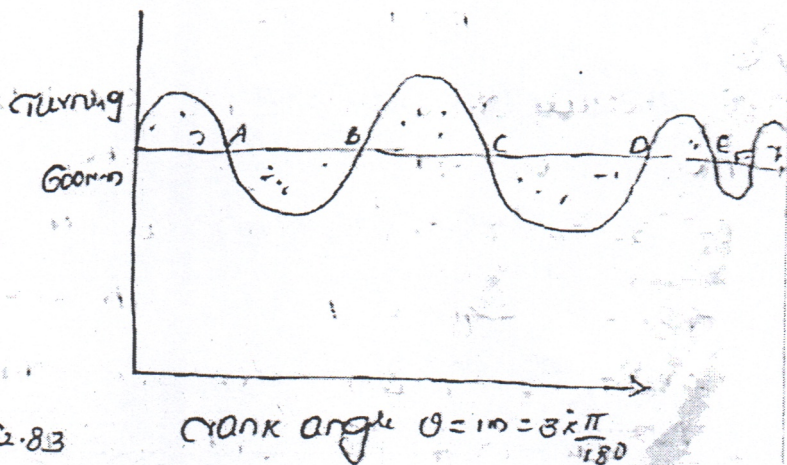
$$N = 600 \text{ rpm}$$

$$R = 0.5 \text{ m}$$

$$\omega_1 - \omega_2 = 0.03 \omega$$

$$\frac{\omega_1 - \omega_2}{\omega} = 0.03$$

$$\omega = 62.83$$



$$A = E$$

$$B = E + 52$$

$$C = E + 52 - 124$$

$$= E - 72$$

$$D = E - 72 + 92$$

$$= E + 20$$

$$E = E + 20 - 140$$

$$= E - 120$$

$$F = E - 120 + 85$$

$$= E - 35$$

$$G = E - 35 - 72$$

$$G_1 = E - 107$$

$$H = E - 107 + 107$$

$$H = E$$

$$= 10 \text{ mm}^2 = 1 \text{ mm} \times 10 \text{ mm}$$

$$= 600 \times 3 \times \frac{\pi}{180} \text{ N}\cdot\text{m}$$

$$\text{maximum} = E + 52$$

$$\text{minimum} = E - 120$$

$$\begin{aligned}\Delta E &= E + 52 - (E - 120) \\ &= 172 \text{ mm}^2\end{aligned}$$

$$\Delta E = 172 \times 600 \times \frac{3 \times \pi}{180}$$

$$= 5403.35 \text{ N-m}$$

$$\Delta E = m R^2 \omega^2 c_s$$

$$5403.35 = m (0.5)^2 (62.83)^2 (0.03)$$

$$m = 182.5 \text{ kg}$$

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