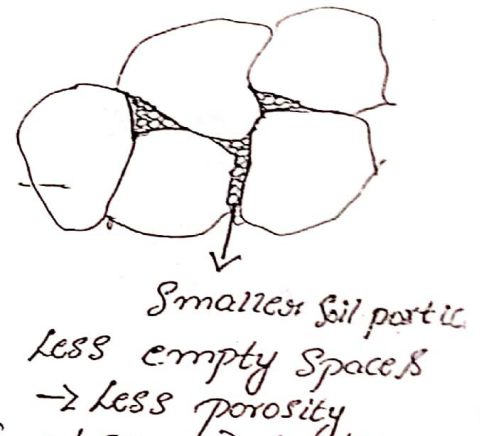
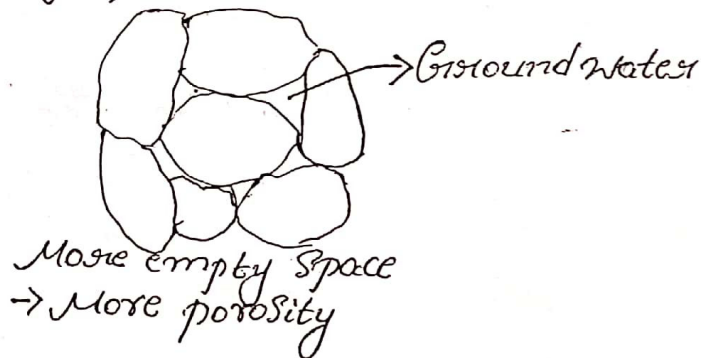


Module - 2

Aquifer Parameters

- Porosity
- Specific yield
- Permeability
- Transmissibility
- Specific retention
- Storage Co-efficient (or) Storetivity

→ Porosity (n)

The ratio of volume of pore space (void space) to the volume of formation (rocks) is called porosity

$$\text{i.e. Porosity (n)} = \frac{V_v}{V} \quad \text{where } V_v = \text{volume of void space}$$

$$V = \text{Total volume of formation (rocks)}$$

Sedimentary rocks → Porosity is more

Igneous rocks → } Porosity is less as these are formed
Metamorphic rocks → } under high pressure and temperature

According to classification of sedimentary rocks

Well rounded → Greater porosity

Poorly sorted → Lesser porosity

Well cemented rocks → Least porosity.

→ Specific yield (S_y)

It is the ratio of the volume of water which will drain freely from the material to the total volume of the formation

$$\text{i.e. Specific yield (S}_y\text{)} = \frac{V_d}{V}$$

$V_d = \text{Volume of water which will drain}$
 $V = \text{Total volume of formation (rocks)}$

Specific yield depends on

- * Grain Size
- * Shape & Distribution of pores
- * Compaction of formation.

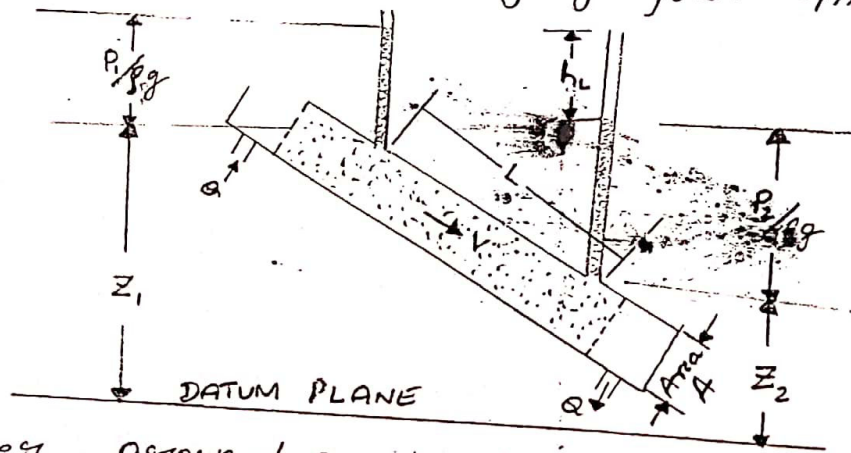
for fine grained soil \rightarrow Specific yield is less

for coarse grained soil \rightarrow Specific yield is more

Permeability

The permeability of material is a measure of its capacity to transmit water (or) any other fluid through its voids or pores.

Ground water is transmitted through aquifer at very small velocity ranging from $1m - 500m / year$



Consider ground water flow through porous medium

$\frac{P_1}{\rho g}$ = Pressure head at Section ①

$\frac{P_2}{\rho g}$ = Pressure head at Section ②

$Z_1 \& Z_2$ = Datum head at Section ① & ②

$\frac{v_1^2}{2g}$ & $\frac{v_2^2}{2g}$ = velocity head at Section ① & ②

Applying Bernoulli's equation to Section ① & ②

$$\frac{P_1}{\rho g} + Z_1 + \frac{v_1^2}{2g} = \frac{P_2}{\rho g} + Z_2 + \frac{v_2^2}{2g} + h_L$$

h_L = Head loss

③

Neglecting the velocity heads as velocity of groundwater will be very small

$$\frac{P_1}{\rho g} + Z_1 = \frac{P_2}{\rho g} + Z_2 + h_L$$

$$h_L = \left(\frac{P_1}{\rho g} + Z_1 \right) - \left(\frac{P_2}{\rho g} + Z_2 \right)$$

the Experimentally it is found that discharge Q from aquifer depends upon $h_L, L \ \& \ A$
 Where L = length between section 1 & 2

A = Area of flow

$$\therefore Q \propto \left(\frac{h_L \times A}{L} \right)$$

$$Q/A \propto \left(\frac{h_L}{L} \right)$$

$$v \propto \left(\frac{h_L}{L} \right)$$

$$v = -k \left(\frac{h_L}{L} \right)$$

If distance b/w 2 piezometers is small then

$$v = -k \left(\frac{dh}{dl} \right)$$

The -ve sign indicates loss of head takes place in the direction flow (or) vice versa

Where k is known as hydraulic conductivity (or) co-efficient of permeability.

v = velocity of water through porous medium

$\frac{dh}{dl}$ (or) Darcy's velocity = Hydraulic gradient

Darcy's Law states that rate of flow per unit area of an aquifer is proportional to gradient of potential head measured in the direction of flow i.e. $(v \propto k \frac{dh}{dl})$ (or) $(v \propto k \frac{h_L}{L})$

If $Re < 1$, then Darcy's law is applicable

$Re > 1$, then Darcy's law is not applicable

Where $Re \rightarrow$ Reynolds number

$$Re = \frac{\rho v d}{\mu}$$

$\rho \rightarrow$ Density of water

$v \rightarrow$ velocity of water / Darcy velocity

$d \rightarrow$ Diameter of void's space

$\mu \rightarrow$ Dynamic viscosity

Hydraulic Conductivity (or) Co-efficient of permeability (k)
It is defined as the rate of flow per unit area of
an aquifer under a unit hydraulic gradient

N.K.T from Darcy's law $v = -k \frac{dh}{dl}$

$$Q = A \times v$$

$$\left(\frac{Q}{A}\right) = v$$

$$\therefore \left(\frac{Q}{A}\right) = -k \times \left(\frac{dh}{dl}\right)$$

$$(or) k = \frac{\left(\frac{Q}{A}\right)}{\left(\frac{dh}{dl}\right)} \rightarrow \text{Discharge per unit area}$$

$\left(\frac{dh}{dl}\right) \rightarrow$ Hydraulic Gradient

For unit Hydraulic Gradient i.e when $\left(\frac{dh}{dl}\right) = 1$

$$k = \left(\frac{Q}{A}\right) \quad (or) \quad k = v$$

unit of v is m/s

Since velocity of Groundwater is very less
it is expressed in terms of m/year

\therefore The same unit holds good for co-eff of per-
meability

Intrinsic permeability

Intrinsic permeability is the property of the medium only and it does not depend on the fluid properties.

Based on Hagen poiseuille equation for laminar flow

$$k = \frac{C \times d_m^2 \times \bar{n}}{\mu}$$

where

$k \rightarrow$ Hydraulic Conductivity

$\mu \rightarrow$ Dynamic viscosity

$C \rightarrow$ shape factor

$d_m \rightarrow$ Average Grain Size

$\bar{n} \rightarrow$ sp. weight

w.k.T

$$\bar{n} = \rho \times g$$

$$k = \frac{(C \times d_m^2) \times \rho \times g}{\mu}$$

$$k = \frac{(C \times d_m^2) \times g}{\nu}$$

$\nu \rightarrow$ kinematic viscosity

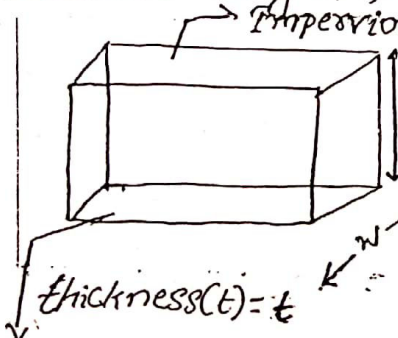
$$\nu = \frac{\mu}{\rho}$$

Intrinsic permeability is the product of $(C \times d_m^2)$
unit of intrinsic permeability $\rightarrow m^2$ or cm^2

$$1 \text{ Darcy} = 9.87 \times 10^{-12} m^2 \text{ (or)}$$

$$1 \text{ Darcy} = 0.987 \times 10^{-8} cm^2$$

Transmissivity (or) Transmissibility (T) or Transmissivity co-eff



Discharge through an aquifer

t is given by $Q = A \times v$

where $A \rightarrow$ Area of flow

$v \rightarrow$ Darcy's $t \rightarrow$ Thickness of aquifer

i.e $v = -k \times (dh/dl)$ Width of aquifer (w) = 1

$$Q = (t \times 1) \times -k \times (dh/dl)$$

$$Q = (t \times k) \times (-dh/dl) \quad \text{thickness } (t) = 1$$

The transmissibility of an aquifer is the product of hydraulic conductivity k and thickness of an aquifer

$$T = (t \times k)$$

The unit of hydraulic conductivity (k) is $m/year$ & of width (b) is m

\therefore unit of Transmissivity is $m^2/year$

$$Q = T \times (-dh/dl) \quad \text{(or)} \quad T = \frac{Q}{(dh/dl)}$$

> Specific Retention (S_{r1})

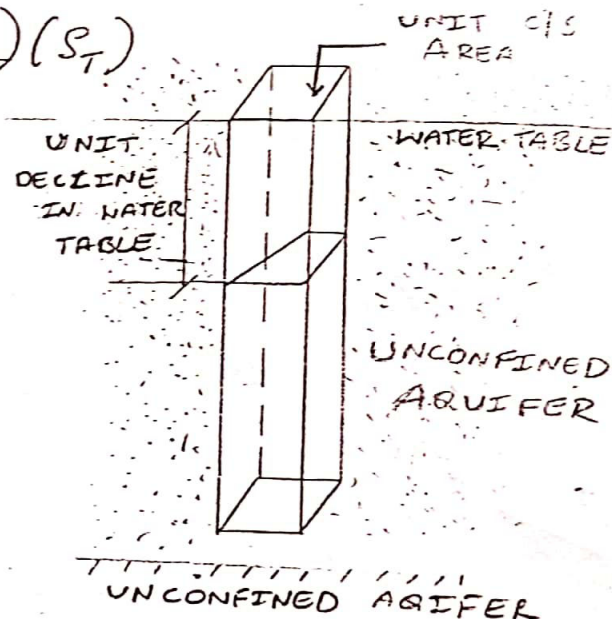
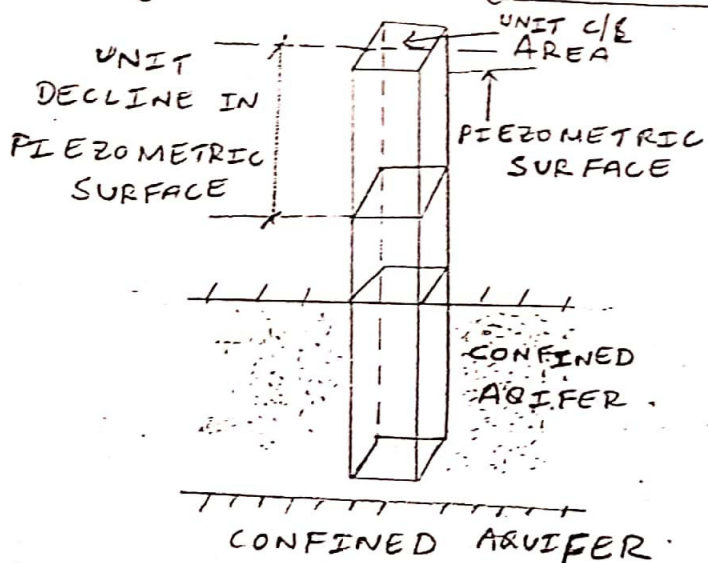
The Specific retention is defined as ratio of volume of water retained in the material to the volume of formation (or) material (rock)

i.e Specific Retention (S_{r1}) = $\frac{V_{r1}}{V}$

$V \rightarrow$ volume of water retained

$V \rightarrow$ volume of formation or material

Storage Co-efficient (Storativity) (S_T)



Storage Co-efficient is defined as the volume of water that an aquifer releases from (or) takes into storage per unit surface area of the aquifer per unit drop of water table in case of an unconfined aquifer & per unit drop of piezometric surface in the case of confined aquifer.

Permeability of isotropic and unisotropic Soil

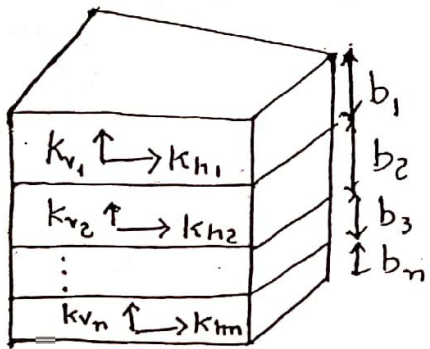
\rightarrow If the properties of soil has same value when measured in different directions, then such soils are called isotropic soil.

Permeability is the same along any direction in the isotropic soil mass

The permeability depends upon the grain size distribution, porosity, shape and arrangement of pores, properties of the pore fluid and entrapped air.

Anisotropic Layered Soil

- If the values of properties of soil are not same when measured in different directions, then such soils are called anisotropic soil.
- Permeability will not be same in the anisotropic soil mass
- Many soils are formed in horizontal layers as a result of sedimentation through water. Because of seasonal variation such soil tend to be horizontally layered and this results in different permeabilities in horizontal & vertical direction
- To determine permeability of anisotropic soil, samples are obtained from each layer and their permeabilities are determined.



The average permeability k_x & k_y in the horizontal and vertical directions are calculated as

$$k_x = \frac{1}{b} (k_{h1} b_1 + k_{h2} b_2 + k_{h3} b_3 + \dots + k_{hn} b_n)$$

$$k_y = \frac{b}{\left(\frac{b_1}{k_{v1}} + \frac{b_2}{k_{v2}} + \frac{b_3}{k_{v3}} + \dots + \frac{b_n}{k_{vn}} \right)}$$

Where

$k_{h1}, k_{h2} \dots k_{hn}$ → Permeability of each layer in x-direction

$k_{v1}, k_{v2} \dots k_{vn}$ → Permeability of each layer in y-direction

b → Total thickness of the aquifer

$$b = b_1 + b_2 + b_3 + \dots + b_n$$

Assumptions of Darcy's Law

According to Darcy's Law $v = k \times (dh/dl)$

Where $k \rightarrow$ co-efficient of permeability

$(dh/dl) \rightarrow$ Hydraulic Gradient

$v \rightarrow$ Darcy's velocity

The following assumptions are made in Darcy's Law

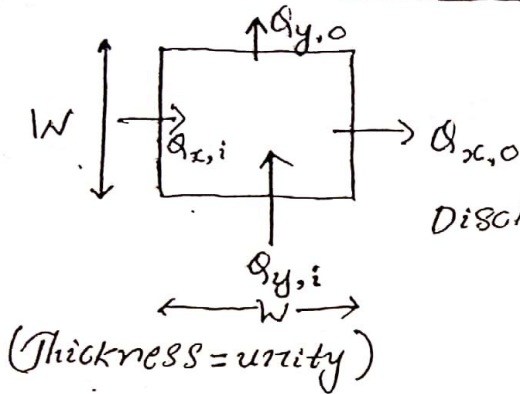
- \rightarrow The Soil is saturated
- \rightarrow The flow through Soil is laminar
- \rightarrow The flow is continuous and steady
- \rightarrow The total cross sectional area of Soil mass is considered
- \rightarrow During verification of Darcy's Law from the experiment, the temperature at the time of testing is 27°C .

Limitations

- \triangleright Darcy's Law is based on the assumption that the flow occurs through the entire cross-section of the material without regard to solid and pores. Actually the flow is limited to pore space only.
- \triangleright Darcy's Law is found to be valid for the flows with Reynolds number less than 1 (unity) only.
- \triangleright Darcy's Law is applicable only for steady flow
- \triangleright Darcy's Law is not applicable for the noncontinuous flow

General ground water flow equation / 3-Dimensional equation:

(or) Laplace equation



Consider an aquifer having the dimensions of W metre & thickness of unity

Discharge through an aquifer is given by $Q = A \times v$

$A \rightarrow$ Area of flow

$v \rightarrow$ Darcy's velocity (or) velocity of ground water

N.K.T

Darcy's velocity (v) = $-k \cdot \frac{dh}{dl}$

$k \rightarrow$ co-efficient of permeability

$(\frac{dh}{dl}) \rightarrow$ variation of head with respect to observed length

$Q = (W \times 1) \times -k \times \frac{dh}{dl}$ (Area of flow (A) = $W \times$ unit thickn)

Rate of flow of water in x-direction getting into aquifer is given by

$Q_{x,i} = (W \times 1) \times -k_x \times (\frac{dh}{dx})_i$

Transmissivity (T) = $k \times$ Thickness of aquifer

$T = (k \times 1)$ i.e $T_x = (k_x \times 1)$

Rate of flow of water in x-direction getting out of aquifer is given by

$Q_{x,o} = (W) \times (-T_x) \times (\frac{dh}{dx})_o$

Similarly

$Q_{y,i} = (W) \times (-T_y) \times (\frac{dh}{dy})_i$

$Q_{y,o} = (W) \times (-T_y) \times (\frac{dh}{dy})_o$

Volume of water in the aquifer is given by $= (Q_{x,i} - Q_{x,o}) + (Q_{y,i} - Q_{y,o})$

N.K.T Storativity (S_T) = $\frac{\text{Volume of water}}{\text{Surface} \times (\frac{dh}{dt})}$

Volume of water = $S_T \times (S.A) \times \frac{dh}{dt}$

S.A → Surface Area of aquifer

$(Q_{x,i} - Q_{x,o}) + (Q_{y,i} - Q_{y,o}) = S_T \times (S.A) \times \frac{dh}{dt}$

$(w \times (-T_x) \times \left(\frac{dh}{dx}\right)_i - w \times (-T_x) \times \left(\frac{dh}{dx}\right)_o) + (w \times (-T_y) \times \left(\frac{dh}{dy}\right)_i - w \times (-T_y) \times \left(\frac{dh}{dy}\right)_o) = S_T \times (w^2) \times \frac{dh}{dt}$

$(S_T T_x) \left(\left(\frac{dh}{dx}\right)_i - \left(\frac{dh}{dx}\right)_o \right) + (-w \times T_y) \left(\left(\frac{dh}{dx}\right)_i - \left(\frac{dh}{dy}\right)_o \right) = S_T \times w^2 \times \frac{dh}{dt}$

$\frac{T_x \left(\left(\frac{dh}{dx}\right)_i - \left(\frac{dh}{dx}\right)_o \right) + T_y \left(\left(\frac{dh}{dy}\right)_i - \left(\frac{dh}{dy}\right)_o \right)}{w} = S_T \left(\frac{dh}{dt} \right)$

If w is very small then head difference h can be expressed in terms of 2nd order differential equation of x & y

$T_x \left(\frac{d^2 h}{dx^2} \right) + T_y \left(\frac{d^2 h}{dy^2} \right) = S_T \left(\frac{dh}{dt} \right)$ → 2-dimensional G.W flow equation

$T_x \left(\frac{d^2 h}{dx^2} \right) + T_y \left(\frac{d^2 h}{dy^2} \right) + T_z \left(\frac{d^2 h}{dz^2} \right) = S_T \left(\frac{dh}{dt} \right)$ → 3-dimensional G.W flow equation

The above equation is for unsteady flow

For Steady flow $\left(\frac{dh}{dt}\right) = 0$

$\frac{d^2 h}{dx^2} + \frac{d^2 h}{dy^2} + \frac{d^2 h}{dz^2} = \frac{S_T}{T} \left(\frac{dh}{dt} \right)$

$\frac{d^2 h}{dx^2} + \frac{d^2 h}{dy^2} + \frac{d^2 h}{dz^2} = 0$ → Laplace equation

(or) $\nabla^2 h = 0$

1D Groundwater Steady flow through Confined aquifer's between two water bodies [Without Recharge]
 (or)
Steady unidirectional flow in confined aquifer's [Without Recharge]

Consider a steady 1D flow through confined aquifer

W.K.T for 3-Dimensional flow

$$\frac{d^2h}{dx^2} + \frac{d^2h}{dy^2} + \frac{d^2h}{dz^2} = 0$$

for 1-Dimensional flow

$$\frac{d^2h}{dx^2} = 0$$

To find the final expression for head difference h

Integrating $\frac{d^2h}{dx^2}$

$$h = C_1x + C_2 \rightarrow \text{eqn 1}$$

$C_1 = ?$ & $C_2 = ?$

Consider the boundary conditions

i) @ $x=0$ $h=h_0$

$h_0 \rightarrow$ water level @ upstream side

$$h_0 = C_2$$

(or)

$$\boxed{C_2 = h_0}$$

ii) @ $x=L$ $h=h_1$

$h_1 \rightarrow$ water level @ down-stream side

$$h_1 = C_1L + h_0$$

$$(h_1 - h_0) = C_1 \times L$$

$$\boxed{C_1 = \frac{(h_1 - h_0)}{L}}$$

$$\therefore h = \frac{(h_1 - h_0)x}{L} + h_0$$

on re-arranging

$$\boxed{h = h_0 - \left(\frac{h_0 - h_1}{L}\right)x}$$

$L \rightarrow$ length of considered section

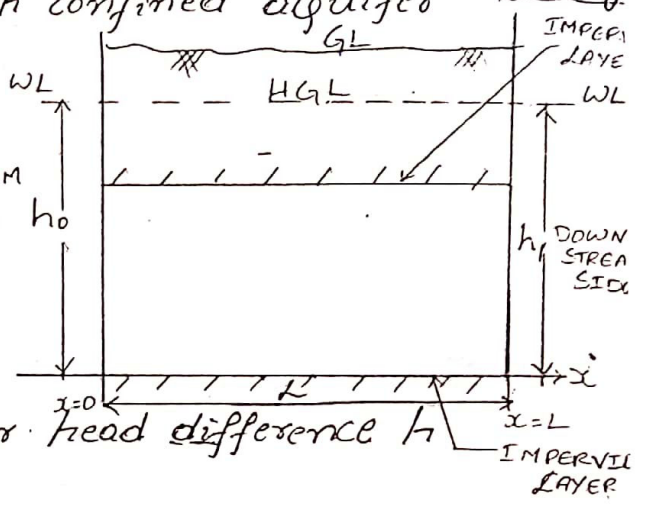
$$\boxed{\frac{dh}{dx} = -\left(\frac{h_0 - h_1}{L}\right) \times 1}$$

Discharge / unit width is given by

$$Q = A \times v$$

$A \rightarrow$ Area of flow

$v \rightarrow$ Darcy's velocity

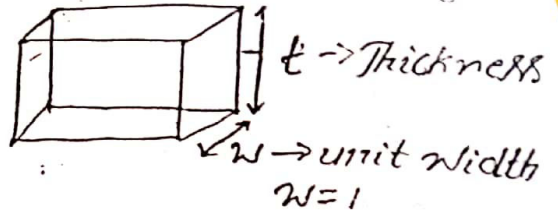


W.K.T

$$v = -k \times \frac{dh}{dl} \rightarrow -k \times \frac{dh}{dx}$$

$k \rightarrow$ Co-efficient of permeability

$$A = W \times t \text{ (m}^2\text{)}$$



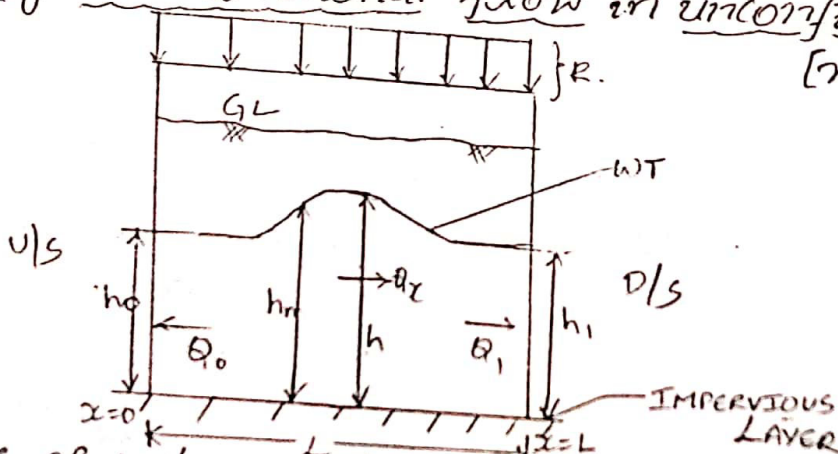
$$\therefore Q = (W \times t) \times (-k) \times \left(\frac{dh}{dx}\right)$$

$$Q = -T \times \frac{dh}{dx} \quad \left\langle T = W \times k \rightarrow \text{Transmissivity} \right\rangle$$

$$Q = -T \left[x - \frac{(h_0 - h_1)}{L} \right] \quad \text{(or)} \quad \boxed{Q = \frac{T (h_0 - h_1)}{L}}$$

1-Dimensional Ground water flow through unconfined aquifer b/w 2 water bodies [with recharge]
(or)

Steady unidirectional flow in unconfined aquifer [with recharge]



- \rightarrow Rate of recharge into the aquifer
- \rightarrow Distance b/w 2 sections (or) water bodies
- $h_m \rightarrow$ Maximum head of the water table
- $\bar{h} \rightarrow$ General level of the water table
- $h_0 \rightarrow$ Level of water body in the upstream side
- $h_1 \rightarrow$ Level of water body in the downstream side
- $Q_0 \rightarrow$ Discharge towards upstream side
- $Q_1 \rightarrow$ Discharge towards downstream side
- $Q_2 \rightarrow$ Discharge from general level of water table towards D/S
- $A \rightarrow$ Area of flow = (general level of the water table towards D/S \times unit width) = $(h \times 1)$

The General Groundwater Steady flow governing equation is given by

$$\frac{d^2 h^2}{dx^2} = \frac{-2R}{k}$$

on integration

$$d^2 h^2 = \frac{-2R}{k} \times dx^2$$

$$h^2 = \frac{-2R}{k} \iint dx^2$$

$$h^2 = \frac{-2R}{k} \times x^2 + C_1 x + C_2$$

$$h^2 = \frac{-R}{k} \times x^2 + C_1 x + C_2 \rightarrow \text{eq}^n 1)$$

Boundary Condition's

@ $x=0$ $h=h_0$

$$h_0^2 = C_2$$

@ $x=L$ $h=h_1$

$$h_1^2 = \frac{-R}{k} \times L^2 + C_1 \times L + h_0^2$$

$$\frac{h_1^2 - h_0^2 + \frac{R}{k} \times L^2}{L} = C_1$$

Substituting for C_1 & C_2 in equation 1)

$$h^2 = \frac{-R}{k} \times x^2 + \left[\frac{h_1^2 - h_0^2 + \frac{R}{k} \times L^2}{L} \right] x + h_0^2 \rightarrow \text{eq}^n 2)$$

$$h = \sqrt{\frac{-R}{k} \times x^2 + \left[\frac{h_1^2 - h_0^2 + \frac{R}{k} \times L^2}{L} \right] x + h_0^2}$$

The above equation represents general level of water table

W.K.T $Q = -k \times h \times \frac{dh}{dx}$

Substituting for $h \times \frac{dh}{dx}$ on differentiating eqⁿ 2)

$\left\{ \begin{array}{l} \because Q = A \times v \quad v = -k \frac{dh}{dx} = -k \times \frac{dh}{dx} \\ A = h \times \text{unit width} \\ \therefore Q = -k \times h \times \frac{dh}{dx} \end{array} \right.$

$$2xh \frac{dh}{dx} = \frac{-2Rx}{k} + \left[\frac{h_1^2 - h_0^2 + \frac{R \times L^2}{k}}{L} \right]$$

$$\therefore h \frac{dh}{dx} = \frac{-Rx}{k} + \left[\frac{h_1^2 - h_0^2 + \frac{R}{k} \times L^2}{2L} \right]$$

$$Q_x = -k \times \left[\frac{-Rx}{k} + \frac{(h_1^2 - h_0^2 + \frac{R}{k} \times L^2)}{2L} \right]$$

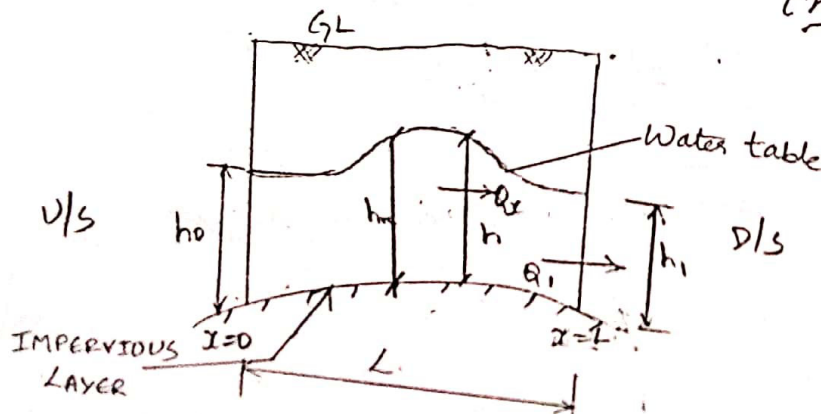
When $x=0$ $Q_{x=0}$

$$Q_{x=0} = -k \times \left[\frac{(h_1^2 - h_0^2) + (\frac{R}{k} \times L^2)}{2L} \right]$$

When $x=L$

$$Q_{x=L} = -k \left[\frac{-R \times L}{k} + \frac{(h_1^2 - h_0^2 + \frac{R}{k} \times L^2)}{2L} \right]$$

2 Dimensional Ground water flow through unconfined aquifer b/w 2 water bodies [Without Recharge] (or) steady unidirectional flow in unconfined aquifer [Without Recharge]



- $L \rightarrow$ Distance b/w 2 Sections (or) waterbodies
- $h_m \rightarrow$ Maximum head of the water table
- $h \rightarrow$ General level of the water table
- $h_0 \rightarrow$ Level of water body in the upstream side
- $h_1 \rightarrow$ Level of water body in the downstream side
- $Q_0 \rightarrow$ Discharge towards upstream side
- $Q_1 \rightarrow$ Discharge towards downstream side
- $Q_x \rightarrow$ Discharge from general level of water table towards u/s
- \rightarrow Area of flow = $(h \times x)$

$$\text{W.K.T } \frac{d^2 h^2}{dx^2} = \frac{-2R}{k} \quad [\text{with Recharge}] \quad \left. \begin{array}{l} \text{General Groundwater} \\ \text{Steady flow governing} \\ \text{equation} \end{array} \right\}$$

$$\frac{d^2 h^2}{dx^2} = 0 \quad [\text{without Recharge}]$$

on integration

$$h^2 = C_1 x + C_2 \rightarrow \text{eq}^n 1)$$

Boundary condition's

$$\text{i) } @ x=0 \quad h=h_0$$

$$\text{ii) } @ x=L \quad h=h_1$$

Substituting 1st boundary condition in eqⁿ 1)

$$\boxed{h_0^2 = C_2}$$

Substituting 2nd boundary condition in eqⁿ 1)

$$h_1^2 = (C_1 \times L) + h_0^2$$

$$C_1 \times L = h_1^2 - h_0^2$$

$$\boxed{C_1 = \frac{h_1^2 - h_0^2}{L}}$$

Substituting for C_1 & C_2 in eqⁿ 1)

$$h^2 = \left(\frac{h_1^2 - h_0^2}{L} \right) \cdot x x + h_0^2 \rightarrow 2)$$

$$h = \sqrt{\left(\frac{h_1^2 - h_0^2}{L} \right) x x + h_0^2}$$

$$\text{W.K.T } Q_x = -k x \left(h \times \frac{dh}{dx} \right)$$

Substituting for $(h \times \frac{dh}{dx})$ on differentiation eqⁿ 2)

$$\therefore 2h \times \frac{dh}{dx} = \left(\frac{h_1^2 - h_0^2}{L} \right) \quad (\text{or}) \quad h \times \left(\frac{dh}{dx} \right) = \left(\frac{h_1^2 - h_0^2}{2L} \right)$$

$$\therefore \boxed{Q = -k x \left(\frac{h_1^2 - h_0^2}{2L} \right)}$$

Problems

When 3.68 million m^3 of water was pumped out from an unconfined aquifer of 6.2 km² area extent, the water table was observed to go down by 2.6 m. What is the specific yield of the aquifer.

During the monsoon season if the water table of the same aquifer goes up by 10.8 m, what is the volume of recharge.

3) i) volume of water pumped out = $3.68 \times 10^6 m^3$

W.K.T Sp. yield = $\frac{\text{volume of water de. (pumped) / recharged}}{\text{volume of the aquifer considered}}$

$S_y = \frac{3.68 \times 10^6}{\text{Area extent} \times \text{water level dra. down}}$

$S_y = \frac{3.68 \times 10^6}{6.2 \times 10^6 \times 2.6} = 0.228$

ii) volume of recharge = ?

W.K.T Sp. yield = $\frac{\text{volume of water recharged}}{\text{volume of the aquifer considered}}$

$0.228 = \frac{\text{volume of water recharged}}{6.2 \times 10^6 \times 10.8}$

Volume of water recharged = $0.228 \times 6.2 \times 10^6 \times 10.8$
 $\Rightarrow 15.26 \times 10^6 m^3$

(or) 15.26 million m^3

The water table levels in two observation wells 350m apart are 210.5m and 206.25m. If the hydraulic conductivity & porosity of the aquifer are 12.5 m/day & 15%, what is the actual velocity of flow in the aquifer.

3) W.K.T
 forms

Darcy's law $v = -k \left(\frac{dh}{dl} \right)$

W.K.T

$V = \text{Darcy's velocity}$

$k = \text{Hydraulic Conductivity} = 12.5 \text{ m/day}$

$(\frac{dh}{dl}) = \text{Hydraulic Gradient} = \frac{210.5 - 206.25}{350}$

$\therefore (\frac{dh}{dl}) = \frac{4.25}{350}$

$V = -12.5 \times \frac{4.25}{350} = -0.1518 \text{ m/day}$

W.K.T

Actual velocity of flow through aquifer (v_a)

$$v_a = \frac{V}{n}$$

where $n = \text{porosity of the aquifer}$

$$v_a = \frac{0.1518}{0.15} = 1.01 \text{ m/day}$$

3) A sample has a hydraulic conductivity of 10 m/day. What would be its intrinsic permeability? what is its hydraulic conductivity in cm/s? what would be its hydraulic conductivity at 30°C

Note: At std temp, Dynamic viscosity, $\mu = 0.01 \text{ gm-cm/s}$

W.K.T $k_0 = C \times d_m^2 \rightarrow \text{Intrinsic permeability}$

$k = \frac{C \times d_m^2 \times g}{\nu}$

$\nu \rightarrow \text{kinematic viscosity}$

$$k = \frac{k_0 \times g}{\nu} \quad \text{or} \quad k_0 = \frac{k \times \nu}{g}$$

$\mu = \text{Dynamic viscosity}$

$$\nu = \frac{\mu}{\rho}$$

$$\therefore k_0 = \frac{k \times \mu}{\rho \times g} \quad (\text{m}^2 \text{ or } \text{cm}^2)$$

Ans

$$K_0 = \frac{k \times M}{\rho \times g} = \frac{10 \times \frac{100}{24 \times 60 \times 60} \times 0.01}{10000 \times 9.81 \times 1000 \times 10^3 \times 10^{-6}}$$

$$K_0 = 1.1798 \times 10^{-7} \text{ cm}^2$$

NOTE 1 Darcy = $0.987 \times 10^{-12} \text{ m}^2$ (or)

1 Darcy = $0.987 \times 10^{-8} \text{ cm}^2$

for $0.987 \times 10^{-8} \text{ cm}^2 \rightarrow 1 \text{ Darcy}$

$1.1798 \times 10^{-7} \text{ cm}^2 \rightarrow ?$

$$\therefore K_0 = 11.95 \text{ Darcy}$$

NOTE

For kinematic viscosity (ν) for water @ 20°C is $0.01 \text{ cm}^2/\text{sec}$ and @ 30°C is $0.008 \text{ cm}^2/\text{sec}$

W.K.T $K = \frac{k}{\nu}$

$$\frac{k}{k_t} = \frac{\nu_t}{\nu}$$

$$k = 10 \text{ m/day} = 0.0115 \text{ cm/sec}$$

$$\frac{0.0115}{k_t} = \frac{0.008}{\frac{0.01}{1000 \times 1000 \times 10^{-6}}}$$

$$k_t = 0.0137 \text{ cm/sec}$$

\therefore Hydraulic Conductivity @ 30° (k_t) = 0.0137 cm/sec