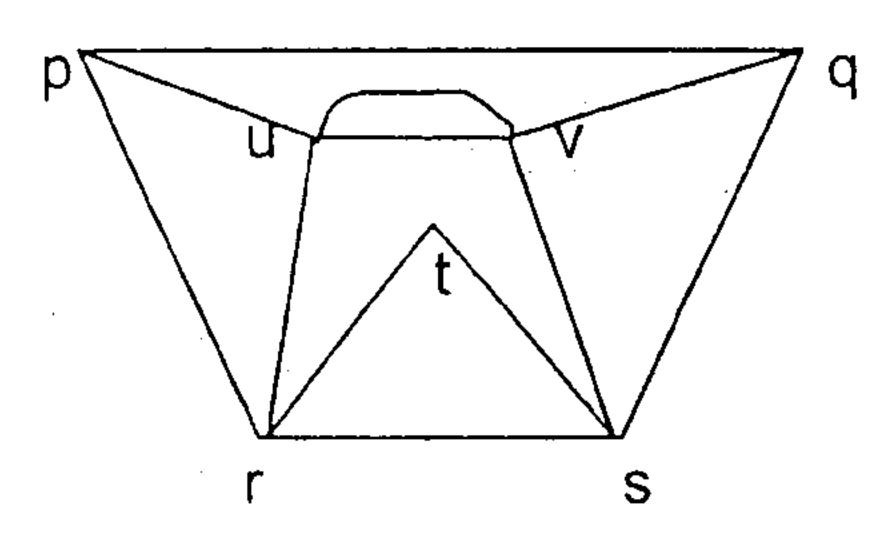
syg- DS

QP Code: NP-18755

(3 hours) Total Marks: 80 N.B. 1. Question No 1 is compulsory 2. Solve any three question out of remaining five questions 3. Assumption made should be clearly stated 4. Figure to the right indicates full marks Prove that $8^n - 3^n$ is a multiple of 5 by mathematical induction, $n \ge 1$ (a) Show that if a relation on set A is transitive an irreflexive, then it is asymmetric. (b) 5 Function f(x) = (4x + 3)/(5x - 2). Find f^{-1} 5 (c)What is the total number of vertices in a full binary tree with 20 leaves? (d) Let f(x) = x + 2, g(x) = x - 2 and h(x) = 3x for all $x \in R$. (R is the set of real number). 8 Find i) $f \circ g \circ h$ ii) $h \circ g \circ f$ iii) $f \circ f \circ f$ Let R be a relation on the set of integers Z defined by aRb if and only if $a \equiv m \pmod{5}$. Prove that R is an equivalence relation. Find 2 / R. Show that $A \times (B \cap C) = (A \times B) \cap (A \times B)$ 4 Let $A = \{1, 2, 3, 4\}$ and $R = \{(1,2), (2,3), (3,4), (2,1)\}$. Find the transitive closure using 3 6 Warshall's algorithm. Consider the lattices $L1 = \{1, 2, 4\}$, $L2 = \{1, 3, 9\}$ under divisibility. Draw the lattice $L1 \times L2$. Solve the recurrence relation $a_n = -3(a_{n-1} + a_{n-2}) - a_{n-3}$ with $a_0 = 5$, $a_1 = -9$ and $a_2 = 15$ Show that a group G is abelian if and only if $(ab)^2 = a^2b^2$ for all $a, b \in G$ 4 Prove that the set $G = \{1, 2, 3, 4, 5, 6\}$ is an abelian group under multiplication modulo 7. (b) Find the generating function for the following series i) {0, 1, 2, 3, 4, } ii) {1, 2, 3, 4, 5,} iii) {2, 2, 2, 2, 2,} iv) {0, 0, 0, 1, 1, 1, 1,} Decode the following words relative to maximum likelyhood decoding function. i) 011001 ii) 101011 iii) 111010 iv) 110110

(b) Determine the Eulerian and Hamiltonian path, if exists, in the following graphs:

6

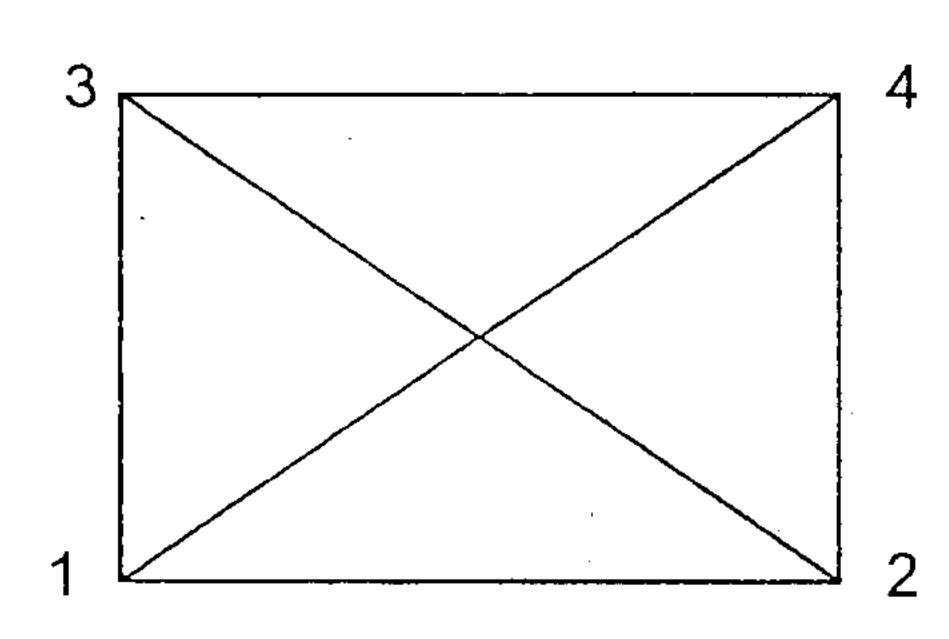


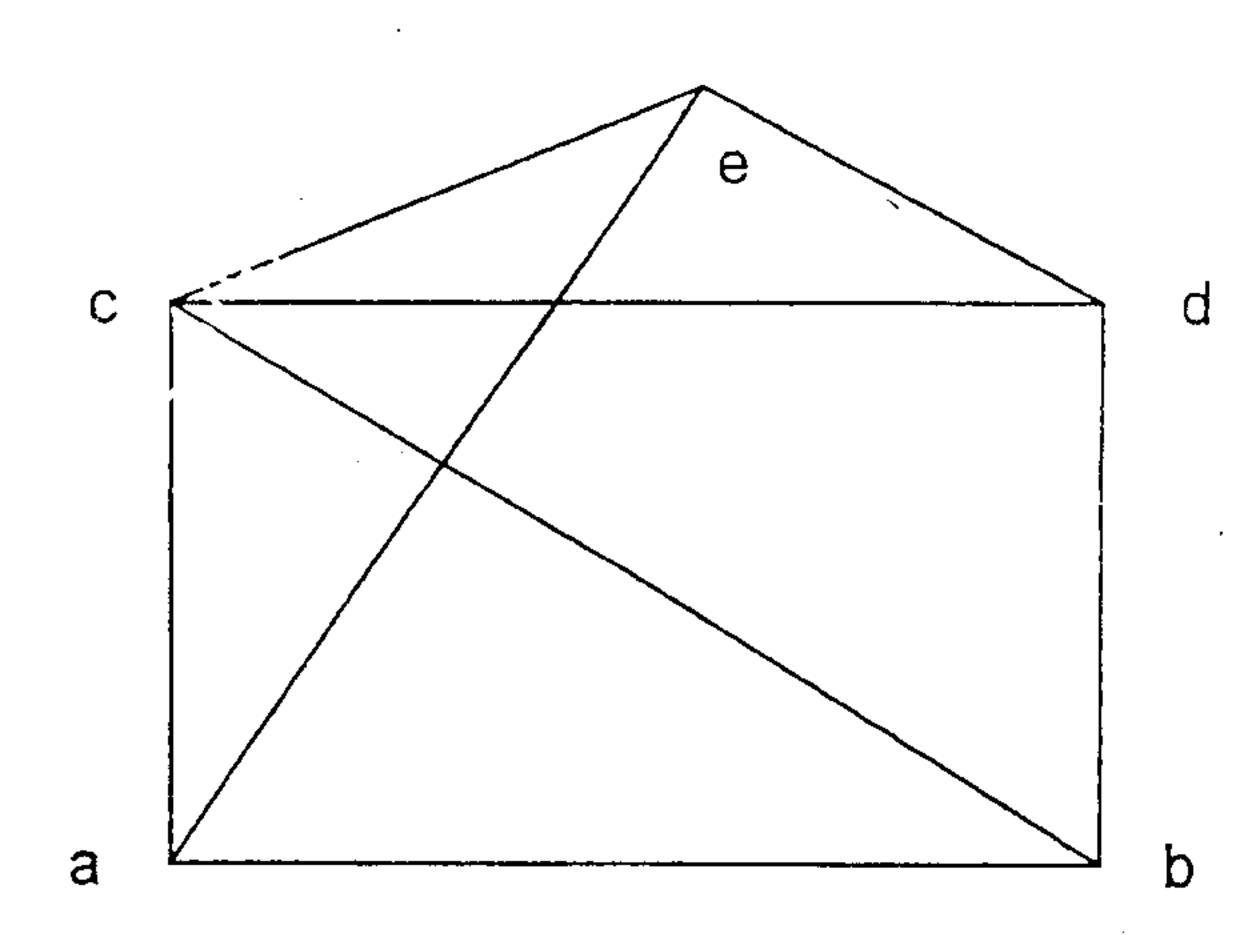
c

Let G be the set of real numbers and let Let G be the set of real numbers and let a*b=ab/2. Showthat (G,*) is a abelian group.

6

6 (a)





- (b) Use the laws of logic to determine the following expression as tautology or contradiction. $[p \land (p \Rightarrow q)] \Rightarrow q$
- ^

Draw the Hasse Diagram of the following:

6

- a) D_{105}
- b) D₇₂

Con. 13514_14.