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Data Science Notes

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[SGGSCC DU]

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W

DATA SCIENCES using R!!

14th Jan 19

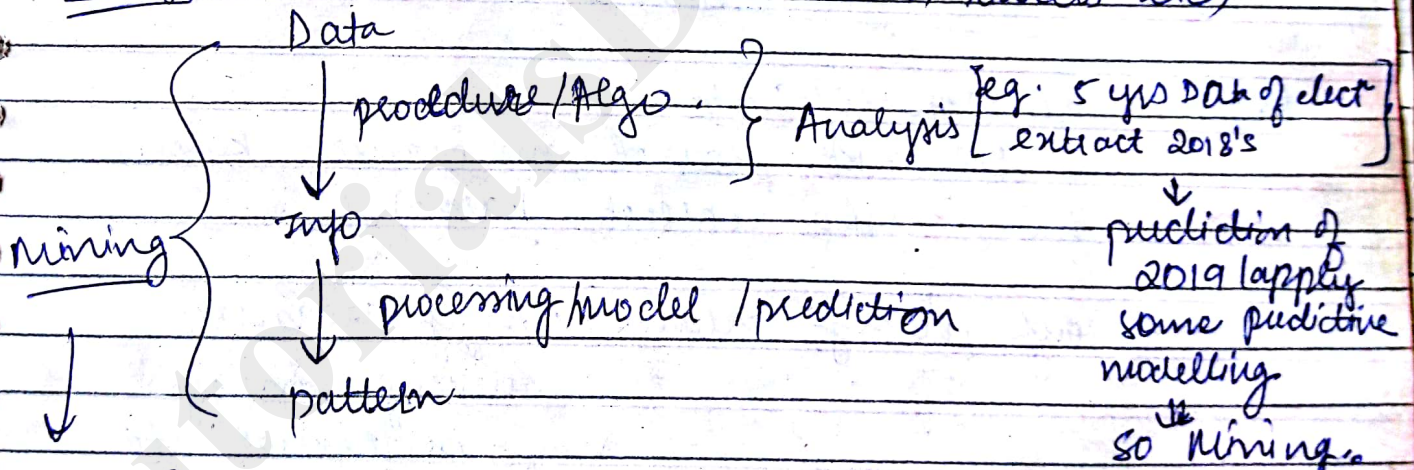
Unit -1.

chap (1-2) → 5 Marks

- Data Science / Dat Analytics
- Data Mining
- Machine Learning
- Big Data

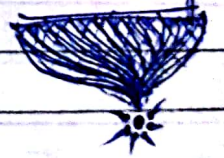
Data → Structured (data picked from DB)
 ↳ unstructured (data picked from any other form other than Databases, eg. newspapers, cookies, tweets etc)

Analysis:-



eg. Stores me kon sa product kiske sath rakna hai

Machine learning :- (i) supervised learning (under supervision of someone)
 (ii) unsupervised learning (Machine is learning by own).



Big Data → large volumes (for news)

Umbrella Activity

Data Science → changing data to product.

if making a software

→ which data I have for software → Analysis.

→

Data Mining - subset of Data Science.

STEPS OF DATA SCIENCE.

(i) collection of Data

(jis data ko product me change karna hai, usko collect karna)

through many means → surveys, images,

may be textual, etc

data can be in csv file.

which is feasible for any particular person.

(ii) Pre-processing Data

Data Set MOCK (2015-18)

intro to Data Science

Data in form of (structured Data)

Name	Joining Date	DOB	completion Date	email
------	--------------	-----	-----------------	-------

is Data se extract karna,
→ Avg. of completion time

predict → how many people are completing the course → difficult to find.
↳ if I have to find the factor of how many people not completing course
↳ can be found, by no. of days spent for course.

① SELECTION OF IMP. ATTRIBUTES

② HANDLING MISSING VALUES

↳ jo data specified nahi hai, missing hai to find using any calculation.

Suppose ending date → not given. ←
So, starting date + no. of days spent.

OR, excluding missing values.

OR, use any default value for the place.

(iii) Analysing Data.

↓
Data left would be analysed for further future.

(iv) Driving insights and generating BI reports.
↓
showing/representation of data
↓
pi chart etc.

(v) Taking decision based on insight.
↓
conclusion finding.
(Warehouse data collect kiya, bread & egg & milk & butter should be kept together.)

Big Data sources

↳ any source can be used to find data.

eg.

What is your data source?

How is your data?

Recommending system (Amazon for eg.)

↓
increasing revenue by the activity.

→ (eg. Netflix & prime, engaging more by not searching for a movie by watching one)

5 V's of Big Data

→ Raw data: Volume.

→ Change over time: velocity.

- Data type: velocity variety.
- Data quality: veracity
- info for decision: value making.

Statistics → Delhi Data Analysis.

→ population & Sample.

Entire area → Delhi

Sample 1 → North Delhi



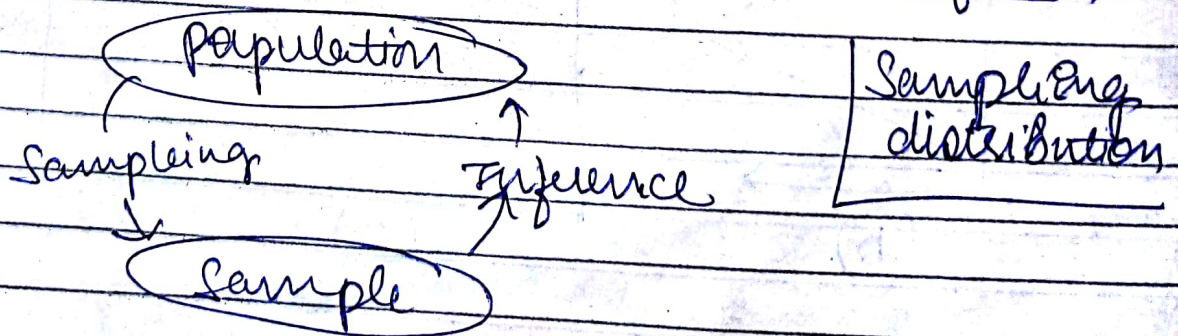
↓
predict can't be formed using only this sample.

Sample 2 → North, South, East, West → 200 people each
↳ Better than previous

Sample 3 → 250 for each part
↳ more Better (total 1000 people)

If any conclusion is valid for given sample & is also valid for Entire area (population)

↓
So, valid conclusion / Statistical inference.



size

Population = N^1

sample $s = N$

"N = ALL"

if sample is valid for populatⁿ

DATA MODELS

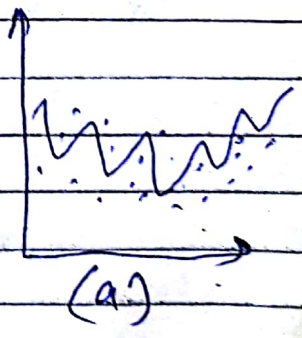
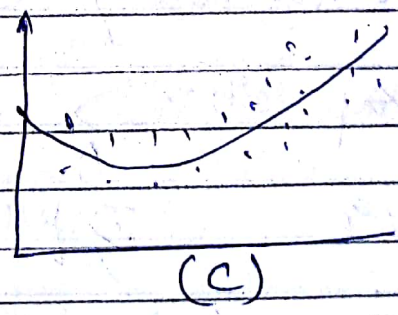
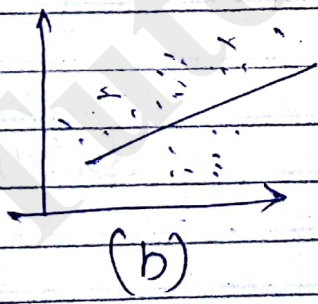
↓ sample

	Educated	Voted	2 class (Y or N)
a	10 th	Y	
b	12 th	N	
c	graduate	Y	
	⋮	⋮	

↑ classifier problem

→ Statistical infer the Data
(if majority of educated people are lying in Yes.)

- (a) overfitting (estimated 70% study 90%)
- (b) under-fitting (not hold statistical inference)
- (c) just-fitted value



Exploratory Data Analysis = Data Analysis

chap 1 & 2 = End (unit 1)

15th Jan, 19

unit - 3 Ref [2] R-Intro (chap 1-10)

R → programming lang.

↳ used for data analysis & manipulation

① packages (data analysis, graphics, etc has every other package)

② Support - graphics (only in this technology)

③ Case-sensitive

Pre 2 marks

Features of R → study from Book

① # comments in R

↳ only single line using #

② > prompt symbol

```
> +2 ←  
3
```

③ Statement in multiple line

```
> 1 * ← + (automatically puts a +)  
2 + 3 ←  
3
```

↳ represent an incomplete statement.

R → untyped language (need not to specify Data types)

Data types in R.

(whatever rules we have for naming a variable, still holds)

① numeric
> a ← 1
(any int, float etc)

Assignment operators
=, ←, →

- a = a + 1 // mathematically wrong
- a ← a + 1
- a → b or b ← a

> class(a)
↓
tells the datatype of variable a i.e. numeric

output: [1] "numeric"

→ represent single output.

> b ← 131

② Integer → any no. w/o fractional part

> a ← 1L # L represents integer value

> class(a)

[1] "integer"

> c ← as.integer(b) # Type casting

> class(c)

[1] "integer"

③ logical - T/F

```
> v ← TRUE
> class(v)
```

[1] "logical"

• option to save work environment
• R file

```
> v ✓
TRUE
> print(class(v)) ✓
# True
```

```
> print(class(v))
> print(a) X
> v X
```

④ Complex → used to store complex numbers.

```
> a ← 1 + i3
> class(a)
```

[1] "complex"

⑤ character

```
> a ← "abc"
> b ← 'abc'
> c ← "123"
```

⑥ Raw

In this datatype, characters are explicitly stored as ASCII characters / codes.

```
> a ← charToRaw("Hello")
> class(a)
```

[1] "Raw"

a will store a value of HELLO concatenated ascii value.

R-objects

* vectors → collection of certain values, values need to be atomic & of single data-type (like array)
 [1, 2, 3] → vector

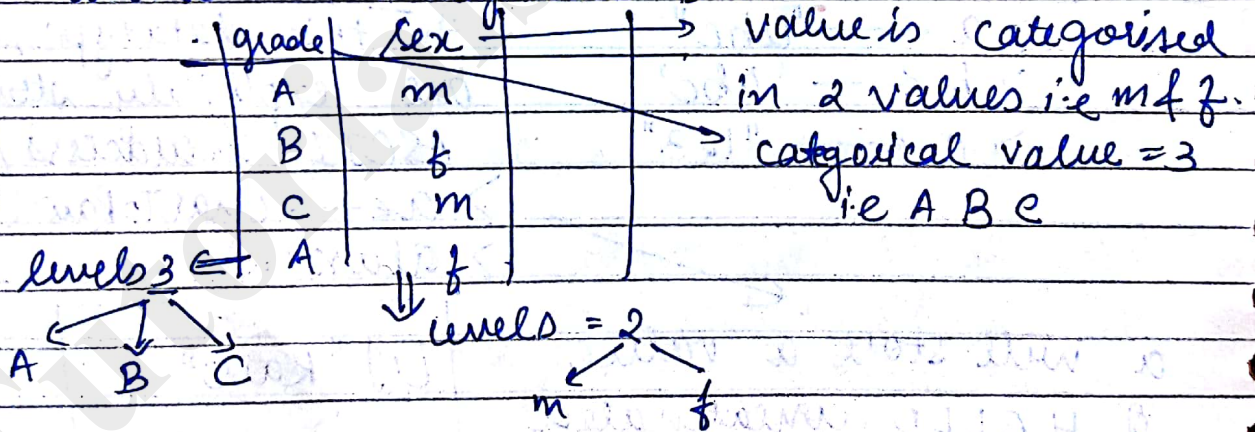
* Lists → any every need not to be atomic

[[1, 2, 3], array, matrix]
 ↳ first element of list is list

* Arrays → 2D Matrix i.e for eg 3x3

* Matrices → 3x3x2 dim 2
 ↳ 2 matrix of with 3x3 etc
 # can have multiple dimension

* Factors → Categorical Data



* DataFrames :- something like a matrix but every value can have different datatypes.

eg.

sn.	Name	Gender	semedu
1	:	:	:
2	:	:	:

Readily used

• csv file will be stored in DataFrames

VECTORS

character
↓
> v ← c("red", "green", "blue")
↓
funct combines all its arguments
↓
c() # function

Memory

Red	green	blue
0	1	2

indexing same as normal array

> class(v) #

[1] "character"

w/o c(), vector can't be created

Lists

→ list() # function

> L ← list(c(2, 1, 3), 21.2, 'a')

① vector ② numeric ③ char

> print(L)

```
[1]
 [1] 2 1 3
 [2]
 [2] 21.2
 [3]
 [1] 'a'
```

* class(L)

find output



Matrix (dim 2)

`m <- matrix(c(1,2,3,4), nrow=2, ncol=2, byrow=TRUE)`
vector with value no. of rows no. of columns

dim = nrow x ncol

$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$

Byrow = T
(default)

$\begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix}$

Byrow = F

`m <- matrix(c(1,2,3,4), nrow=2)`

then ncolumn = 2 (By default)

if value are 9 & nrow=2

ARRAYS

vector of dimension

`a <- array(c(1,2), dim=c(3,3,2))`
value of elements 3x3x2

No. of elements = 18

mismatch in both argument, so the values would be repeated

`print(a)`
`a`

	1, 2	1, 2
[1]	[1] [2] [3]	[1] [2] [3]
[2]	$\begin{bmatrix} 1 & 2 & 1 \end{bmatrix}$	$\begin{bmatrix} 2 & 1 & 2 \end{bmatrix}$
[3]	$\begin{bmatrix} 2 & 1 & 2 \end{bmatrix}$	$\begin{bmatrix} 1 & 2 & 1 \end{bmatrix}$
		$\begin{bmatrix} 2 & 1 & 2 \end{bmatrix}$

[x, —]

xth Row

[—, x]

xth column

21st Jan, 2019

▲ Vectors

creating vectors

① using c() function.

```
> x ← c(1, 7, 6, 9);  
> x
```

```
[1] 1 7 6 9
```

numeric by default,
if you want int, write

② ~~typeof(x)~~ # class(x)

```
> y ← c(1, 2, true, "a")
```

logical → numerical → character.

```
> y
```

```
[1] "1" "2" "TRUE" "a"
```

② using infix function ":"

work only on continuous values. i.e

gap b/w the data members is one

> v ← c(1, 2, 3, ..., 9, 10)

> v ← 1:10

> y ← 11:1100 # (from 11 to 1100)

> y ← 2:-2; y # concatenation

> y ← 2:-2
> y

concatenation can be done for any no. of state

[1] 2 1 0 -1 -2 Output window

> z ← 3.4 : 10.2; z

[1] 3.4 4.4 5.4 6.4 7.4 8.4 9.4

③ using seq() # stepsize would be given

seq (from = a , to = b , [by = step-value , length.out = len of vectors])

> x ← seq(1, 7); x

[1] 1 2 3 ... 7

default values

- * step-value = 1
- *

> x ← 1:7

> x ← c(1, 2, 3, 4, 5, 6, 7)

} same

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$x \leftarrow \text{rep}(1, 10, \text{by} = 2); x$

[1] 1 3 5 7 9

$x \leftarrow \text{rep}(1, 10, \text{length.out} = 10); x$

$\rightarrow x$ will have a length of 10

[1] 1.0 2.0 3.0 4.0 5.0 6.0 7.0 8.0 9.0 10.0

if given all the 4 value, the functⁿ wouldn't work

multiplicity of any value in rep out : is 1.

④ using rep()

$f \leftarrow \text{rep}(0, 5); f$

[1] 0 0 0 0 0

$f_1 \leftarrow \text{rep}(1:3, 4)$

[1] 1 2 3 1 2 3 1 2 3 1 2 3

$\text{length}(f_1)$

[1] 12

$h \leftarrow \text{rep}(4:6, 1:3); h$

[1] 4 5 5 6 6 6

Recycling

$h_1 \leftarrow \text{rep}(1:10, 1:5)$

↓ 10 ↓ 5 (5 a multiple of 10)

∅. [1] 1 2 2 3 3 3 4 4 4 4 5 5 5 5 5 6 7 7 8 8 8 9 9 9 10 10 10 10

> h1 ← rep(1:10, 1:4); h
 ↓ ↓
 10 4 [4 is not a multiple of 10]

so, a warning will occur
some interpreters will give out some not.

[1] 1 2 2 3 3 3 4 4 4 4 5 6 6 7 7 7 8 8 8 8
 9 10 10

> x ← rep(1:2, each=2); x

[1] 1 1 2 2

> y ← rep(1:2, time=2) # y ← rep(1:2, 2)

[1] 1 2 1 2

Indexing a vector

a [index]

- ① indexing starts with 1.
- ② multiple indexed value can be passed

eg. a [c(1,2)] = > a[1]
 > a[2]

③ index can be -ve value.

eg. [1] [2] [3]
 1 2 3

> a ← c(1,2,3)

> a [-1]

all elements except 1.

[1] 2 3

```
for (i=1; i<5; i++)
```

```
  cout << a [i%2 == 0]
```

[i]	1.0	1.5	2.0	2.5	3.0
	3.5	4.0	4.5	5.0	

①

```
> d <- seq (1, 5, by = 0.5); d
```

```
> d [3]
```

```
> d [5:7]
```

```
> d > 2.8
```

```
↳ # [1] FALSE FALSE FALSE TRUE TRUE TRUE TRUE TRUE
```

```
> d [d > 2.8] → # [1] 3.0 3.5 4.0 4.5 5.0
```

[i]	2.0	3.0	3.5	4.0
	3.0	3.5	4.0	
	4.5	5.0		

②

```
x <- c (0, 1, 2, 3, 4, 5, 6)
```

```
x <- x [c (2, 3, 6)]
```

```
print (x)
```

```
v <- x [c (TRUE, FALSE, FALSE, TRUE)]
```

```
print (v)
```

```
x <- x [c (-2, -3)]
```

```
print (x)
```

[i]	1	2	5
[i]	0	3	
[i]	0	3	4 5 6

- `ls()` → listing of all the values
- `rm(x)` → x will be deleted by R-environment
- `rm(c(x,y))` → `rm(x)`
→ `rm(y)`

R-Studio

script	variables in work environment
console o/p	Packages & library

<code>x <- c(0,1,2)</code>	x

22nd Jan, 19.

> unique(a)
NA # (not available)
→ same as null

NaN → not a no.
Inf → infinity
-Inf → -∞

> x ← c(1, 2, NA, 3)
> length(x)

4

Na have a memory location with no value.

vectors are dynamic in R.

```
> x[1] ← 3; x
[1] 3 2 NA 3
```

```
> x[10] # NO error as like out of Bound
[NA]
```

```
> length(x) ← 6; x
[1] 3 2 NA 3 NA NA
```

A vector having NA don't properly function for "functions"

```
eg. > sum(x) # 3 + 2 + NA + 3 = 8 + NA = NA
[1] NA
```

```
> sum(x, na.rm = TRUE)
```

na.rm(check) = exclude this condition

```
[1] 6
```

can be used for mean also,
length include NA.

```
> max(x)
[1] 3
```

```
> min(x)
[1] 1
```

①

```
> x = 1:8
> x[4] = -9; x
> x[c(1,4)]
> x[x > 3]
> x[x > 3 + x < 8]
```

	x[x % 2 == 0]							
[1]	1	2	3	-9	5	6	7	8
[1]	1	2	3	-9				
[1]	5	6	7	8				
[1]	5	6	7	8	2	6		8

```
(2) > y <- (1:5)^2; y
> y [2:4]
> y [c(-2,-4)]
> y [c(1,-1)] X NOT allowed
> y [-1:9] = # y [0] [ +ve & -ve index mixing is not allowed ]
> y [6] = # Na
> y [1:9] = # y [1]
> y + 1
> y + 5:1
```

```
(3) > a <- seq(1, 19, by=2); a
> rep(1:3, length.out=9) -> b; b
> a <- a [1:4]; a
> a + (2*1:5) ->
> a <- 2*1:5
[1] 2 4 6 8 10
```

output

```
(2) [1] 1 4 9 16 25
[1] 4 9 16
[1] 1 9 25
[1] 4 9 16 25
[1] Na
[1] 1
```

functions

abs(x)

sqrt(x)

ceiling(x)

floor(x)

round(x, digit = n)

trunc(x) # truncate the decimal part.

5M

Que Given a vector f as $f \leftarrow c(0, 1, 1, 2, 3, 5, 8, 13, 21, 34)$

What is the output of the following R commands

- ① $f[1:3]$ [1] 0 1 1
- ② $f[-(1:3)]$ [1] 2 3 5 8 13 21 34
- ③ $f < 10$ [1] T T F F T T F F
- ④ $f[f < 10]$ [1] 0 1 1 3 3 5 8 F
- ⑤ $f[f \% \% 2 == 0]$ [1] 0 2 8 34

29th Jan, 2019

warning \rightarrow in matrix (1:5, nrow=3, ncol=3, byrow=TRUE)

data length [5] is not a multiple of the no. of rows [3]

$> c \leftarrow$ matrix (1:5, nrow=3, ncol=3, byrow=TRUE);

	[,1]	[,2]	[,3]
[1,]	1	2	3
[2,]	4	5	1
[3,]	2	3	4

we can rename the dim of the matrix

- 1 rownames $\leftarrow c("r1", "r2", "r3")$
- 2 columnnames $\leftarrow c("c1", "c2", "c3")$

either a list or
a vector list()

> p ← matrix (9:1, 3, 3, TRUE, dimnames =
list(row.names, col.names)) #p

> a

	[1]	[2]	[3]
[1]	1	2	3
[2]	4	5	6
[3]	7	8	9

> a [2, 1]

[1]	4
-----	---

> a [2,] # All the columns

[1]	4	5	6
-----	---	---	---

> a [, 3]

[1]	3	6	9
-----	---	---	---

> a [c(1,2), c(2,3)]

	[, 1]	[, 2]
[1]	2	3
[2]	5	6

> a [c(3,2),] # All the columns

	[, 1]	[, 2]	[, 3]
[1]	7	8	9
[2]	4	5	6

> a [c(3,2)] # only first column

[1]	
[1,]	7
[2,]	4

> a[-1,]

	[, 1]	[, 2]	[, 3]
[1,]	4	5	6
[2,]	7	8	9

It is possible to index a matrix in a single vector while indexing in such a way it acts like a vector formed by stacking the columns of the matrix one after another. Result is returned as a vector.

> a[1, 4] = a[c(1, 2, 3, 4)] → # treated as 1D array.

using logical vectors as index

→ Here rows & columns where the value is true will be returned also, the logical vectors will be recycled if necessary.

→ logical vectors can be mixed with integer vectors for indexing.

3 rows
T, F = recycled when no. are not equal
So, T, F, T
(1st & 3rd row print)

T F F don't work
TRUE f FALSE work.

> x

	[, 1]	[, 2]	[, 3]
[1,]	4	8	3
[2,]	6	0	7
[3,]	1	2	9

> x [c(TRUE, FALSE, TRUE), c(TRUE, TRUE, FALSE)]
= x [c(1, 3), c(1, 2)]

	[, 1]	[, 2]
[1,]	4	8
[1,]	1	2

> x [c(T, F), c(2, 3)]

	[, 2]	[, 3]
[1,]	8	3
[3,]	2	9

→ # treated as 1D array.

> x [c(TRUE, FALSE)] # T F T F T F T F T
4 6 1 8 0 2 3 7 9

[i]	4	1	0	3	9
-----	---	---	---	---	---

> x[x > 5] # 1D array.

[i]	6	8	7	9
-----	---	---	---	---

→ > det(x)

> x

	[, 1]	[, 2]
[1,]	2	4
[2,]	3	11

[i]	10
-----	----

function

1. solve → inverse of matrix

> solve(x)

2. sum → calc or sum of all elements in the matrix.

> sum(x)

[1] 20

3. product →

> prod(x)

> sum(x[1,])

[1] 5

> y ← diag(3); y

	[,1]	[,2]	[,3]
[1,]	1	0	0
[2,]	0	1	0
[3,]	0	0	1

> f(x) # transpose

> y ← matrix(1:4, 2, 2); y

	[,1]	[,2]
[1,]	1	3
[2,]	2	4

> x+y > x/y
> x-y > x*y

element wise add, sub, divide, multiply.

NOT matrix wise

> x * y # element wise multiplication not matrix multi.

↓
> x .* y # matrix multiplication

BM (equatⁿ given)

Q write a R script used to solve a system of linear equation.

$$\begin{aligned} a_1 x_1 + b_1 x_2 &= c_1 \\ a_2 x_1 + b_2 x_2 &= c_2 \end{aligned}$$

$$\begin{bmatrix} a_1 & b_1 \\ a_2 & b_2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} c_1 \\ c_2 \end{bmatrix}$$

$$\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} a_1 & b_1 \\ a_2 & b_2 \end{bmatrix}^{-1} \begin{bmatrix} c_1 \\ c_2 \end{bmatrix}$$

Step 1: make A matrix using previously mentioned function

Step 2:- make B

Step 3 - $y \leftarrow \text{solve}(A)$

Step 4 - $\text{ans} \leftarrow y \% * \% B$ [OR] $\text{solve}(A, B)$

Reading user input

➤ # readline → used to read 1 line of input.

$n \leftarrow \text{as.integer}(\text{readline}(\text{prompt} = \text{"Enter n"}))$
↓
is same for no. or a string.
Type casting to integer

more than 1 input elements.

scan()

```
> x ← scan() ←
```

```
1: 3 ←
```

```
2: 7 ←
```

```
3: 5
```

ctrl z ≠ ctrl d (for windows & linux)

```
→ Read 3 input
```

Que Take 2 vectors of size 2 as an input from the user & combine those vectors to form a matrix where the elements will be filled by row.

function → scan() for input.
→ rbind()

```
> a ← scan()
```

```
1: 1
```

```
2: 2
```

```
3:
```

```
read 2 items
```

```
> b ← scan()
```

```
1: 3
```

```
2: 4
```

```
3:
```

```
read 2 items
```

```
> x ← rbind(a, b)
```

chap - 5
R - Intro

Test for R syntaxes

chap 1, 2, 3
finished

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- Data Structures
- Deep Learning
- Digital Image Processing
- Discrete Mathematics
- Information Security
- Internet Technologies
- Java Programming
- JavaScript & jQuery
- Machine Learning
- Microprocessor
- Operating System
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06-02-19

Practice

user defined functions in R

```
{ func_name ← function (arg1, arg2...)
```

```
  |  
  |  
  |
```

```
} return # optional, this will not effect the  
  prototype of a function
```

Progl:1

```
print ("Fibonacci series")
```

```
a ← -1
```

```
b ← 1
```

```
{ f ← function (n)
```

```
  while (n > 0)
```

```
  {
```

```
    x ← a + b
```

```
    print (x)
```

```
    a = b
```

```
    b = x
```

```
    n ← n - 1
```

```
  }
```

```
}
```

```
→ n ← as.integer ( readline ("Enter x") )  
  f(n)
```


to implement

Ques Write a R script a linear search using function
Take the vector & the key to search as an
input from the user.

Input \rightarrow using scan

12/02/19

name of function

code for Armstrong number

sum of digits in a cube of no. is equal to no.

```

function (n)
{
    s ← 0
    m ← n
    while (n > 0)
    {
        r = n % 10 # modulus returns
        s = s + (r * r * r)
        n = n // 10 # Integer division.
    }
    print (m)
    print (s)
    if (m == s) {
        print ("a")
    } else {
        print ("b")
    }
}
n ← as.integer (.....)
f(n)
    
```

Input n=6

s ← 0
m ← 6

36 × 6
216

6
216
6

Arrays in R

↳ n-dim obj

3 × 4 × 2

matrix level

↓

based on { row column }
matrix index.

¹
[, 1] [, 2] [, 3] [, 4]

[1,]
[2,]
[3,]

²
[, 1] [, 2] [, 3] [, 4]

[1,]
[2,]
[3,]

a cube
equal to
v.

array (data, dim = c(r, c, m), dimnames = list(m, n, mn))

eg. a → array(1:24, dim = c(3, 4, 2))

36x6
16

eg. v1 ← 1:12
v2 ← 13:24

b ← array(c(v1, v2), dim = c(3, 4, 2))

All the functions are applicable at this place.

eg.

> v1 ← c(5, 9, 3)

> v2 ← c(10, 11, 12, 13, 14, 15)

> x ← array(c(v1, v2), dim = c(3, 3, 2))

> print(x)

1st arg has to be data or matrix with a element could also be provided.

		1	2	3
	[,]	[, 1]	[, 2]	[, 3]
[1,]	5	10	13	
[2,]	9	11	14	
[3,]	3	12	15	

		1	2
	[,]	[, 1]	[, 2]
[1,]	5	10	13
[2,]	9	11	14
[3,]	3	12	15

[4]

eg.
=> i ← array (c (1:3, 3:1), dim = c(3, 2))
> i

	[, 1]	[, 2]
[1,]	1	3
[2,]	2	2
[3,]	3	1

> a ← array (1:24, dim = c(3, 4, 2))
> row.names ← c("r1", "r2", "r3")
> col.names ← c("c1", "c2", "c3")

names to a pre-defined array.

> m.names ← c("m1", "m2")
> b ← array (1:24, dim = c(3, 4, 2), dimnames = list(row.names, col.names, m.names))

	output
	c1 c2 c3
functions to check	
→ name()	r1
→ attributes()	r2
→ mode()	r3

is.matrix() # object is matrix or not.

> a = array (1:9, dim = c(3, 4, 1))
> a

	1	2	3	4
[, 1]				
[, 2]				
[, 3]				

↓
if for one() was not written it won't be a matrix

→ works on every function - transpose, product etc.

different array not this
 \downarrow
 x

	r_1	r_2	r_3
$a[1, 2, 1] \# 4$	c_1	c_2	c_3
$a[1, 2, 1] \# 4 5 6$	5	10	13
$a[, ,] \# a$ entire array.	9	11	14
$a[c(1), c(2, 3), 2] \# 13 16$	3	12	15
$a[c(TRUE, FALSE), c(2, 3), 2]$			m_2
	c_1	c_2	c_3
$a[-1, 1, 1] X$	5	10	13
$a[-1, , 1] X$	9	11	14
$a[-1, ,]$	3	12	15

- either the name of array
- $sum(a) \#$ sum of matrix $a(21)$
- $nrow(a)$ } ?? no. of row & col.
- $ncol$
- mean
- median

→ $\% \# \% \#$ # dimensions has to be same

INDEX MATRIX

$> x \leftarrow$ array(1:20, dim=c(4,5))

$> x$

	[, 1]	[, 2]	[, 3]	[, 4]	[, 5]
[1,]	1	5	9	13	17
[2,]	2	6	10	14	18
[3,]	3	7	11	15	19
[4,]	4	8	12	16	20

$> i \leftarrow$ array(c(1:3, 3:1), dim=c(3,2))

$> i$

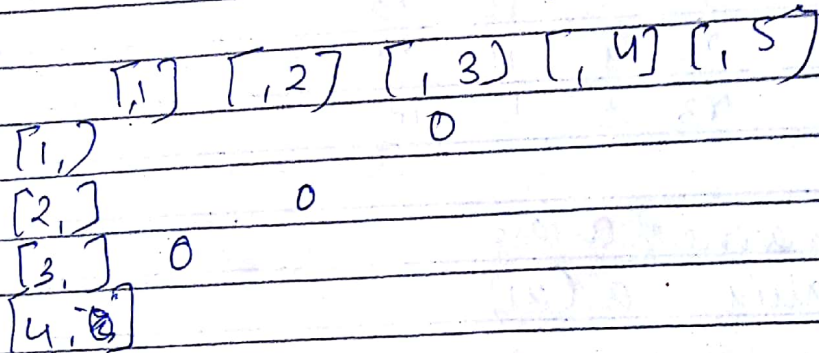
	[, 1]	[, 2]
[1,]	1	3
[2,]	2	2
[3,]	3	1

```
> x[i]
[1] 9 6 3
```

```
> x[i] ← 0.
> x
```

negative indexes are not allowed in matrix.
index.

NA of '0' values are allowed.
row in index matrix containing 0 is ignored.



LISTS

difference betⁿ vector & list

- ① vector → homogeneous { 1D.
- list → heterogeneous

$v \leftarrow c(1, 2, c(1, 2)) \neq$ a vector.
 (you can't have vector inside a vector.)
 $v \leftarrow c(1, 2, 1, 2)$

- ② vector → can't be nested
- list → can be nested.

```
> list_1 ← list("Red", "G", c(21, 32, 11), 51.23, TRUE)
> list_1
```

↓
heterogeneous in nature

```
[[1]] # components of lists
[1] "Red"
[[2]]
[1] "G"
```

```
[3]  
[1] 21 32 11
```

```
[4] 51.23  
[1] 51.23
```

```
[5]  
[1] TRUE
```

Suppose a matrix with 100 elements of the screen size is 20

```
> v  
[1] 1 2 . . . . . 20  
[2] 21 22 23 24 . . . 40  
[4] 41 42 . . . . . 60  
  . . . . .
```

corresponding to the object's element being printed on the line.

```
> list-1 [1]
```

```
[1]  
[1] "Red"
```

* in vectors, if size = 6, we give 8th element. So 7th is NA.

```
> list-1[[1]]
```

```
[1] "Red"
```

* in list, it is NULL.

```
> length(list-1)
```

```
[1] 6
```

```
> list-1[[8]] = c(1, 1)
```

```
> length(list-1)
```

```
[1] 8
```

```
> list-1
```

```
⋮  
[7]  
[1] NULL  
[[8]]  
[1] 1 1
```

```
> list_data ← list (c("Jan", "Feb", "M"),  
matrix (c(3, 9, 5, -1, 2, 8),  
nrow = 2),  
list ("green", 12.3))
```

```
> names(list_data) ← c("1st", "A", "B")  
> list_data
```

```
$ '1st'  
[1] "Jan" "Feb" "M"  
  
$ A  
  [,1] [,2] [,3]  
[1,] 3 5 +2  
[2,] 9 -1 8  
  
$ 'B'  
$ 'B' [[1]]  
[1] "green"  
  
$ 'B' [[2]]  
[1] 12.3
```

```
> x ← list (day = "Tues", lecture = "DS", date =  
c(13, 2, 2018))
```

```
> x
```

\$ day [1] "Tues"	\$ date [1] 13 2 2018
\$ lecture [1] "DS"	


```
> x$day
[1] "Tues"
```

```
> x$date
[1] 13 2 2018
```

Merging list

```
> is.list(x)
[1] TRUE
```

```
> y = c(1)
> is.list(y)
[1] FALSE
```

```
> y = as.list(y)
> is.list(y)
[1] TRUE
```

```
> new-list = c(x,y) # vector
> new-list
```

```
$day
[1] "Tues"
$lecture
[1] "DS"
$date
[1] 13 2 2018
[[4]] [1] 1
```

• c function is also used to combine multiple lists

x & y list are getting combined into new list.

$$c(x, y) \neq c(y, x)$$

Converting list into vector

sum, prod etc functions are not applicable in list. So we have to convert into vectors.

use unlist() function.

```
> list1 ← list(1:5)
> list2 ← list(10:14)
> list1 + list2
```

~~ERROR~~

```
> v1 ← unlist(list1)
> v2 ← unlist(list2)
> v1 + v2
```

```
[1] 11 13 15 17 19
```

12th
MAR, 19,

> class (data) # numeric

> class (f1)
[1] factor

> levels (f1) # will return the levels
corresponding to factor f1

[1] "east" "north" "west"

changing the order of the levels

factor → ordered factor
 → unordered
 (by default unordered)

> max(f1) or min(f1)
will give max^m & min^m level of f1
↳ of no use when ordered.

or max
[1] min is not meaningful for factors

> is.ordered(f1)

[1] FALSE

> f2 ← factor(data, # ordered ke case me,
 levels="east", "north", "west", # necessary to specify
 ordered = TRUE) # levels

> f2

[1] _____

Levels: east < north < west

> max(f2)

[1] "west"

> str(f1) # structure of f1
Factor w/3 levels | 3 | 2 | 3

e - 1
w - 3
e - 2
n - 2
w

Output Questions

- > `f1[3]` [1] east
- > `f1[c(2,4)]` [1] west north
- > `f1[-1]` [1] west east north west
- > `f1[c(TRUE, FALSE)]` [1] east east west
- > `length(f1)` [1] 5
- > `f1[6]` ← "south" # since no level is south so, invalid
- > `invalid factor level, NA generated`
`f1[2]` ← "south" # 2 k jagah NA.
- > `f1`
[1] , , , , , NA
levels: "east", "north", "west"

Adding levels to an existing factor

> `levels(f1) ← c(levels(f1), "south")`

> `nlevels(f1)` [1] 4

> `f1[6]` ← "south" # now valid.

applicatⁿ visualization of data

apply()

This functⁿ is used to run a pre-defined or a user defined functⁿ on a factor

employee	region	incomes
e1	e	20k
e2	south	30k
	n	
	w	

Can be treated as factor
(we want east ki avg salary)

~~> mean-income~~

> region ← c("e", "w", "e", "n", "s", "e", "n", "s")

> s1 ← factor(region)

> incomes ← c(20, 40, 60, 80, 30, 30, 60, 40)

> mean_income ← apply(incomes, s1, mean)

data vector
(same calc jisme kame hai)

functⁿ that you want to run (can be user defined or pre-defined)

> mean-income
e n s w
200 300 400 500

2018
Ques differentiate bet ordered & unordered factor and OUTPUT question.

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strings factor = TRUE
by default

items ← data.frames (colour = c('red', 'blue', 'b', 'r',
g, g, y, b, g, y, r, b, b, g, r, y),
size = c(5, 10, 11, 6, 15, 16, 20, 9, 13, 18, 7, 14, 8,
13, 6, 10))

> tapply (items\$size, items\$colour, sum)

blue	green	red	yellow
52	57	24	56

> tapply (items\$size, items\$colour, mean)

27th Mar, 19

unit-5 (Chap-10 GRAPHICS)
(5-10 Marks)

- > data() # whatever data we have in R-environment
- > data(iis) # load iis dataset in current environment.
- > install package...
- > str(iis) # structure of dataset.
- > summary(iis)
- > head(iis) # 1st 5 records.
- > head(iis, n=10)
- > tail(iis) # last 5

head always return 6 rows but theory wise 5 rows

b, x,
g, s, y)
14, 8,

- > tail (iris, -6)
- > head (pressure)
- > max (pressure & temp)
- > min (")
- > mean (")
- > median (")
- > quantile (")
- > summary (")
- > nrow (iris)
- > ncol (iris)
- > dimension (iris)

	data sets divided into
quartile	4 parts
decile	10 parts
percentile	100 parts

Graphs.

- scatter plot graph
 - line plot graph
 - bar plot graph
 - box plot graph
- # Statistical

histogram # like bar plot.

pie chart



SYNTAX

① plot(x, y, main, xlab, ylab, xlim, ylim, axes)

(title) (label)

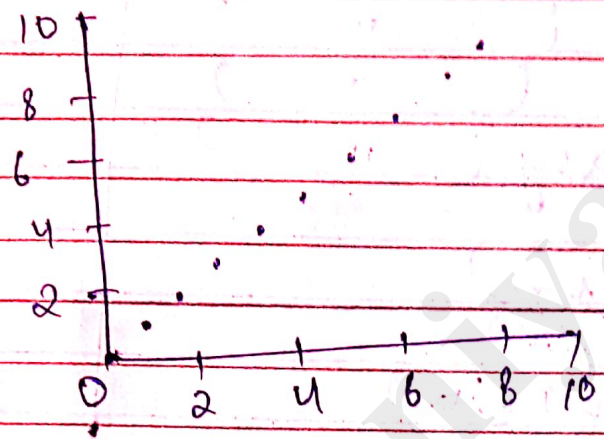
(heading)

~~plot~~ x → mandatory parameter.


```
main = "title"  
xlab = "speed"  
ylab = "distance"
```

xlim = c(5, 50) # limits
ylim = c(0, 20)
axes → by default. True
↳ false if you don't
want to show axes.

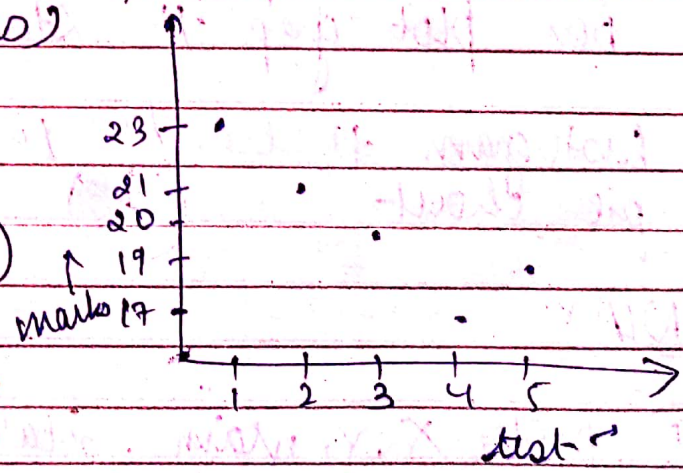
```
> x ← 1:10  
> plot(x)
```



```
> plot(x, y)
```

```
> plot(df) # by default graph of 1'st 2 col.  
of dataframe
```

```
> test ← 1:5  
> marks ← c(23, 21, 20, 17, 19)  
> plot(test, marks)
```



```
> df = data.frame  
(test, marks)
```

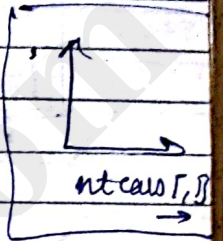
```
> plot(df)
```

if 2 other col for graph
> plot(df\$c, df\$d)

unit 5 - 15 marks

- > data(mtcars)
- > head(mtcars)

- > plot(mtcars[,1], mtcars[,2]) or
> plot(mtcars\$mpg, mtcars\$cyl)



OR

- > attach(mtcars) # mtcars is added to the search path for R.
- > plot(mpg, cyl)

~~*~~

- > plot(x,y) = > plot(y~x)

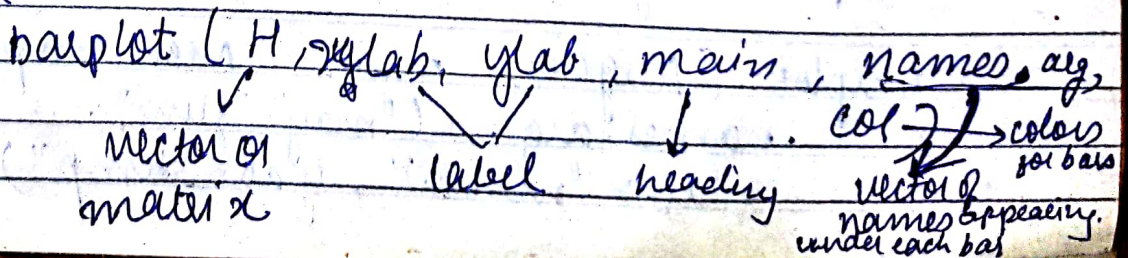
- > ~~dataframe~~ df = read.csv("path of file")
- > str(df)

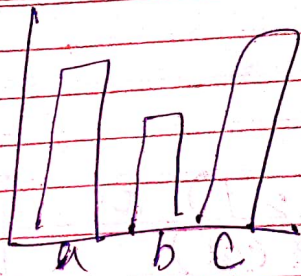
- > nrow(df)
- > ncol(df)
- > dim(df)

- > plot(df\$length, df\$weight, main="length vs", xlab="length", ylab="weight")

BAR CHART

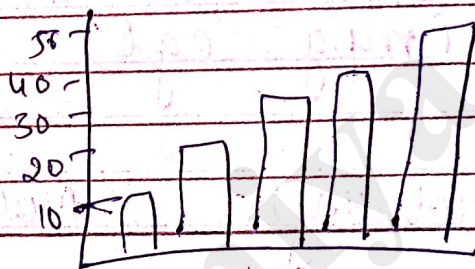
Syntax:





vectors would be recycled for names & colors

```
> v ← c(10, 20, 30, 40, 50)
> barplot(v)
```



Eg: # plot a bar chart of a mean temperature by months using airquality dataset

```
> data(airquality) # to load dataset
```

```
> heights ← tapply(airquality$temp, airquality$month, mean)
```

`tapply (attribute, attribute, mean)`
 (jisme apply hoga) (factor, jisse divide hoga) (function)

```
> heights
```

```
> barplot(heights)
```

```
> barplot(heights, main = "mean temp, by month",
  names.arg = c("may", "june", ...),
  xlab = "month", ylab = "temp")
```

shades change according to size of bar.

> gray } [limits -> should be 0 to 1.]
> length (heights)
> rank (heights) # rank is ↑sing order

> table(heights) (value choti) (Badi value)

> rel.hts ← rank (heights) / length (heights)

> rel.hts
5 6 7 8 9
0.2 0.6 0.8 1.0 0.4

> grays ← gray (1 - rel.hts) # (rel.hts) same o/p

> grays

> barplot (heights, col = grays,

~~last year~~

5 Marks

Q. write a code in R to plot a graph to depict the relation b/w temperature in celcius (x-axis) & temp in Faren (y-axis) using the formula

$$T(F) = T(C) * \frac{9}{5} + 32$$

label the axis & give the title as "C vs F" to your graph

solⁿ

!- values should be given by person.

Ques. Store the following data in a dataframe & perform the following.

A	B
alpha	150
Beta	100
gamma	80
delta	110

- (i) display the contents of dataframe.
- (ii) draw a barplot of name the bars acc. to the values of column A.

28th Mar, 19

line Plot

syntax:

```
> plot(x, y, type = "l")
```

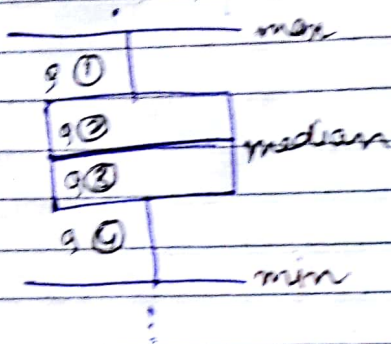
↓
same plot function with another attribute = "l"

eg. `plot(df, type = "l")`

Box Plot :- statistically representing data

- mean (avg)
- std. deviation ($\sum (x - \bar{x})^2$)
- max + min (Range)
- outlier (temp limit = 30, we are getting 60 of some place)
- quartile
↓
dividing into 4 parts. remove outliers

syntax: `boxplot(x, data, notch, valwidth, names, outliers)`



x → vector (any column)

data → data frame

notch → logical value either true or false

valwidth → width manipulation of box

names → names for box (like names.cyl)

eg. `boxplot(pressure $ temperature)`

- > data (mtcars)
- > etc (mtcars)
- > head (mtcars)
- > input ← `mtcars[, c('mpg', 'cyl')]`
- > head (input)
- > dim (input)
- > dim (mtcars)
- > `boxplot (mpg)`
- > `summary (mpg)`
- > `boxplot (mpg, cyl)`
- > `boxplot (mpg ~ cyl)`
- > `boxplot (cyl, mpg)`

if 1st arg is factor then no. of box plots = no. of levels of 1st attribute
cyl has 3 levels
so 3 boxplots
(corresponding to value of mpg)

~~Book eg.~~ (check)

> table (input \$ cyl)

4 6 8
11 7 14

4 ke corresponding 11 rows

Histogram

→ frequency related.

syntax:—

hist (v, main, xlab, xlim, ylim, breaks, col, border)

* histogram can only have 1 column or attribute. Since we are talking about frequency.

v → vector

main → title

col → colors

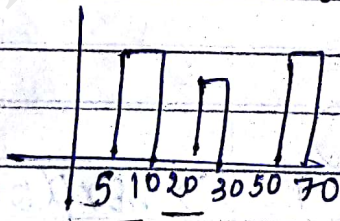
border → for border color
border = c("Red", ...)

xlab → label

ylab is frequency by default

xlim & ylim → limits

breaks → mention the width of each bar



~~eg.~~

> data (cars 93)

> dim (cars 93)

> names (cars 93)

> hist (cars 93 \$MPG.city)



Que Read the given text file & perform the following

- (a) draw a histogram showing the occurrences of various grades.
- (b) Boxplot of variable "final" w.r.t grade
boxplot (final, grade)

Sec 2.6

- (1) mean (x)
- (2) median (x)
- (3) sd (x) # standard deviation
- (4) var (x) # variance
- (5) cor (x, y) # correlation
- (6) cov (x, y) #

5th April, 19

Que Read the given table in a dataframe & answer the following questions 6 Mark

empid	Salary (Rs)	Experience (yes)	Age (yes)	Category
E1	60,000	11	48	married
E2	15,500	2	30	unmarried
E3	45,00	7	35	M
E4	1,59,00	13	47	M
E5	60,000	11	47	M
E6	15,500	2	28	unmarried

(i) draw a boxplot for experience & age of an emp. label the axes of the graph appropriately.

use different colour for different barplots

(ii) draw a histogram for category

(iii) draw a barchart of exp. experience of employees showing emp. Id as label for bars.

syntan to read a table

(a.txt) → path.

df ← read.table ("a.txt", header=TRUE)

if want to make data frame

df ← data.frame (...)

Que 2 :- consider the given data, & the answer following

Item Id	length	Category
i1	65	A
i2	66	B
i3	71	C
i4	70	D
i5	50	A
i6	51	B
i7	40	C
i8	30	D

(i) write a command to display only the last 4 rows of the given dataframes.

(ii) display only rows of the DF where the category is C.

(iii) draw a bargraph to depict the mean length of all the items by their categories. Label the axis of graph appropriately.

→ questions for theory

(iv) draw the boxplot showing the statistical summary of all the items wrt their categories.

(v) write a command to display maximum length within the dataframe.

Quiz write commands to perform the following.

(i) load iris dataset.

(ii) find the dimension of the structure of the dataset.

(iii) print first seven rows of the dataset.

(iv) write a command to display the individual count of all the species present in iris dataset.
command → Table

(v) write a command to display the names of all the attributes +nt in the dataset.

(vi) draw a scatterplot of width & length
sepal.width & sepal.length.

(vii) analyse the output of the command
plot(iris)

(viii) draw a boxplot indicating the statistical aspects of all the species wrt sepal.width

~~also~~ See commands for check on these datasets
also

① mtcars

② Airquality.

Section 2.6

$x \leftarrow c(0, 1, 1, 2, 3, 5, 8, 13, 21, 34) NA$

Standard deviation } command syntax of output
deviation &

$\> \text{mean}(x)$ if $na.rm = TRUE$?

8.8

$$\# \bar{x} = \frac{\sum_{i=1}^n x_i}{n}; n \rightarrow \text{length}$$

$\> \text{median}(x)$

n
Odd even

4

$$\left(\frac{n+1}{2}\right)$$

$$\frac{n}{2} + \frac{n+1}{2}$$

$\> \text{var}(x)$

$$\# \frac{1}{(n-1)} \sum_{i=1}^n (x_i - \bar{x})^2$$

$\> \text{sd}(x)$

$$\# \sqrt{\text{var}(x)}$$

$$\text{var}(x) = \frac{1}{10-1} \sum_{i=1}^{10} (x_i - \bar{x})^2$$

$$= \frac{1}{9} \left[(0-8.8)^2 + (1-8.8)^2 + (2-8.8)^2 + (3-8.8)^2 + (5-8.8)^2 + (8-8.8)^2 + (13-8.8)^2 + (21-8.8)^2 + (34-8.8)^2 \right]$$

$$= 121.733$$

$$= \frac{1}{9}$$

$$\text{sd}(x) = 11.033$$

Que:- Consider the 2 vectors defined

$$x \leftarrow \text{seq}(1, 10, \text{by} = 2)$$

(i) find mean(x) & median(x)

(ii) $x[6] \leftarrow 2$

$x[7] \leftarrow 4$

$x[c(2, 9, 10)] \leftarrow 2$

> print(length(x))

final mode of x

mode \rightarrow value which occurs of most of the time but mode(x) does not find the frequency & for mode, we have to find a logic

(iii) find standard deviation & variance of x.

(iv) > $x[12] \leftarrow \text{NA}$

now, find mean(x) \rightarrow answer = Na

Also state the effect of the introduction of Na value on this vector x.

Rectify the syntax so as to calculate the actual mean of vector x

Solⁿ:- $x(1, 3, 5, 7, 9)$

(i) > mean(x) [1] 5 $x(1, 3, 5, 7, 9, 2, 4, 2, 2, 2)$
(ii) (length(x))
print [1] 10

> median(x) [1] 5 (iii) var(x) = $\frac{1}{9}(77) = 6.67$

(iv) mean(x) [1] Na sd(x) = 2.58

(iv) $x = c(1, 3, 5, 7, 9, 2, 4, 2, 2, 2)$

no.rm = TRUE

Finding mode of x

where, $x = c(1, 3, 5, 7, 9, 2, 4, 2, 2, 2)$

② $\> ans \leftarrow y [which.max(tabulate(match(x, y)))]$

① $\> y \leftarrow unique(x); y$

① unique functⁿ returns a row vector that contains the sorted set of unique values of its arguments

[set \Rightarrow no duplicate values]

$\> y \leftarrow unique(x); y$
[1] 1 2 3 4 5 7 9

some versions of R returns a set of unique values w/o sorting it.

[1] 1 3 5 7 9 2 4
[1] [2] [3] [4] [5] [6] [7]

① Match functⁿ returns the 1st occurrence of the 1st argument in the 2nd argument

$\> match(x, y)$
[1] 1 2 3 4 5 6 7 6 6 6

① Tabulate funcⁿ takes the integer valued vector & returns the no. of times each integer occurs in it.

> tabulate(match(x,y))
1 1 1 1 1 4 1

① ~~which~~ max → max^m value ; ④
ans ← y [which = 4]

② "which" funcⁿ returns the index of the logical object when it is true.

ERROR

(v) parts of same question.

$y \leftarrow$ rep $(1+x, \text{each}=2)$

find correlation of (x, y) & covariance of x & y .

cor (x, y) & cov (x, y)

(vi) Remove Na value from x & create vector x_1 from x with values less than 4.

(vii) y_1 is set as 1:6. Now, find correlation of (x, y_1) & covariance of (x, y_1)

FORMULAS

$$\text{cov}(x, y) = \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})$$

$$\rho_{\text{cor}}(x, y) = \frac{\text{cov}(x, y)}{\sqrt{\text{var}(x) \cdot \text{var}(y)}} \quad \text{Check}$$

where x & y have to be vectors of same dimensions

(v)

$x \rightarrow$ 1 3 5 7 9 2 4 2 2 Na Na
rep 2 2 4 4

→ $x \leftarrow 1:3$ & $x[1:2:3]$
 $y \leftarrow \text{rep}(x, \text{each}=2)$

1 1 2 2 3 3

or
 $y \leftarrow \text{rep}(x, \text{times}=2)$

1 2 3 1 2 3

→ $\bullet \bullet \bullet$ mismatch in dimensions in the vectors x & y .

Soln :-

(v) $y \leftarrow (2\ 2\ 4\ 4\ 6\ 6\ 8\ 8\ 10\ 10\ 3\ 3)$
 $\quad\quad\quad (5\ 5\ 3\ 3\ 3\ 3\ 3\ 3\ \text{Na}\ \text{Na}\ \text{Na}\ \text{Na})$

$\bullet \bullet \bullet$
 Error

(vi) $x \leftarrow x[! \text{is.na}(x)]; x$

[1] 1 3 5 7 9 2 4 2 2 2

$x \leftarrow x[x < 4]; x$

[1] 1 3 2 2 2 2

$\bar{x} = 2$

(vii) $y_1 \leftarrow c[1:6] \leftarrow [1\ 2\ 3\ 4\ 5\ 6]$

$\bar{y}_1 = 3.5$

$$\text{cov} = (x_1, y_1) = \frac{(-1)(-2.5) + (1)(-1.5)}{5}$$

$$= \frac{2.5 - 1.5}{5} = \frac{1}{5} = 0.2$$

$$\text{cor} = \frac{0.2}{\sqrt{\text{var}(x_1) \text{var}(y_1)}} = \frac{0.2}{\sqrt{(0.2)(3.5)}} = \frac{0.2}{0.7} \quad \times$$

$$\text{var}(x_1) = \frac{1}{5} [(-1)^2 + (1)^2] = \frac{1}{5} = 0.2$$

$$\text{var}(y_1) = \frac{1}{5} [(-2.5)^2 + (-1.5)^2 + (0.5)^2 + (0.5)^2 + (1.5)^2 + (2.5)^2]$$

$$\text{cor}(x_1, y) = 0.169$$

- mean & standard deviation of a dataframe works by column & these functⁿ will only work for the numerical column of data frame

> df

small medium large
 ; ; ;
 ; ;

- ① mean(df)
 small medium large
 mean of col₁ mean of col₂ mean of col₃

- ② med sd(df)

- ③ median(df) ~~X~~ (wrong)

median(df & small) | or apply f
 median(df & medium) | apply
 median(df & large) |
 mode → no functⁿ, do same as median

- variance & co-variance returns a covariance matrix for the dataframes

- ① var(df)

- ② cov(df)

	small	medium	large
small	$\left[\begin{array}{l} cov(s,s) \\ cov(s,m) \\ cov(s,l) \end{array} \right]$	$\left[\begin{array}{l} cov(m,s) \\ cov(m,m) \\ cov(m,l) \end{array} \right]$	$\left[\begin{array}{l} cov(l,s) \\ cov(l,m) \\ cov(l,l) \end{array} \right]$
medium			
large			

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