Name :	
Roll No. :	An Annual (V Kanadada and Kanadada
Invigilator's Signature :	

CS/BBA (H)/BIRM/BSCM/SEM-2/BBA-202/2011 2011 MATHEMATICS – II

Time Allotted : 3 Hours

Full Marks : 70

The figures in the margin indicate full marks. Candidates are required to give their answers in their own words as far as practicable.

GROUP – A

(Multiple Choice Type Questions)

1. Choose the correct alternatives for any *ten* of the following :

 $10 \times 1 = 10$

- i) The value of $\lambda t_{n \to \infty} \left(1 + \frac{1}{n} \right)^n$ is
 - a) e b) $\frac{1}{e}$
 - c) 0 d) 1.
- ii) The derivative of xe^x is
 - a) e^x
 - b) $e^{x}(x+1)$
 - c) $e^{x}(x-1)$
 - d) none of these.

2052

[Turn over

CS/BBA (H)/BIRM/BSCM/SEM-2/BBA-202/2011
ii) If
$$y = 8x^2$$
, then $\frac{d^2y}{dx^2}$ is
a) 8 b) 0
c) 16 d) none of these.
iv) A function $f(x)$ is said to be an even function if $f(-x)$ is equal to
a) $f(x)$ b) $-f(x)$
c) $-f(-x)$ d) none of these.
v) The value of $\int_{0}^{1} 2e^x dx$ is
a) $2e$ b) 2
c) $2(e-1)$ d) none of these.
vi) The co-factor of c is the determinant $\begin{vmatrix} a & h & g \\ h & b & f \\ g & f & c \end{vmatrix}$ is
a) $(-1)^{3+3} \begin{vmatrix} a & h \\ h & b \end{vmatrix}$
b) $(-1)^{3+2} \begin{vmatrix} a & h \\ h & b \end{vmatrix}$
c) $(-1)^{1+3} \begin{vmatrix} a & h \\ h & b \end{vmatrix}$
d) none of these.
vii) The determinant of an orthogonal matrix is
a) 0 b) 1
c) ± 1 d) none of these.



[Turn over

CS/BBA (H)/BIRM/BSCM/SEM-2/BBA-202/2011 xiii) The function (5x + 3) is increasing in the interval a) (0, 5) b) (-1, 5) c) (-∞, -∞) d) none of these. xiv) The function $u(x, y) = \frac{(x+y)^2}{(x-y)^2}$ is a homogeneous function of degree a) 0 b) 1 c) 2 d) none of these.

GROUP – B (Short Answer Type Questions)

Answer any *three* of the following. $3 \times 5 = 15$

- 2. Verify Euler's theorem for the function $f(x, y) = x^2 + 10xy + y^2$.
- 3. Show that the matrix $A = \begin{pmatrix} 1 & 2 \\ 3 & 1 \end{pmatrix}$ satisfies the equation $A^2 2A 5I = 0$ and hence find A^{-1} .

4. Find the rank of the matrix $A = \begin{pmatrix} 1 & 1 & 1 & 1 \\ 4 & 1 & 0 & 2 \\ 0 & 3 & 4 & 2 \end{pmatrix}$.

- 5. Find the equation of the parabola whose vertex is (-2, 2) and focus is (-6, 6).
- 6. Solve the following system of equation by Cramer's rule :

$$x + y + z = 8$$

$$x - y + 2z = 6$$

$$3x + 5y - 7z = 14.$$
7. Evaluate
$$\int_{0}^{\frac{\pi}{2}} \frac{\sqrt{\sin x}}{\sqrt{\sin x} + \sqrt{\cos x}} dx.$$

CS/BBA (H)/BIRM/BSCM/SEM-2/BBA-202/2011 Ulean **GROUP – C** (Long Answer Type Questions) Answer any three of the following. 45 a) If x + y + z = 0, then show that $\begin{vmatrix} x & y & z \\ x^3 & y^3 & z^3 \end{vmatrix} = 0$. 8. Show that the matrix $A = \begin{pmatrix} 2 & -3 & 1 \\ 3 & 1 & 3 \\ -5 & 2 & -4 \end{pmatrix}$ satisfies the b) equation A(A - I)(A + 2I) = 0. Compute the inverse of the matrix $A = \begin{pmatrix} 2 & -1 & 1 \\ -15 & 6 & -5 \\ 5 & -2 & 2 \end{pmatrix}$. c) Verify whether the following matrix $A = \frac{1}{3} \begin{pmatrix} -1 & 2 & -2 \\ -2 & 1 & 2 \\ 2 & 2 & 1 \end{pmatrix}$ is 9. a) orthogonal or not. Find A^{-1} . b) Solve the following system of equation by matrix inversion method : x + y + z = 6x - y + z = 22x + y - z = 1Find the value of t for which the matrix $\begin{pmatrix} 2 & 0 & 1 \\ 5 & t & 3 \\ 0 & 3 & 1 \end{pmatrix}$ is c)

5

singular.

2052

[Turn over

CS/BBA (H)/BIRM/BSCM/SEM-2/BBA-202/2011

10. a) Verify whether the function f(x) as defined below is continuous or not at x = 2.

$$f(x) = \begin{cases} x^2 + 4, & x > 2 \\ 8, & x = 2 \\ 3x^2 - 4 & x < 2 \end{cases}$$

b) Find $\frac{d^2 y}{dx^2}$ if $x = \frac{t^2}{1+t}$ $y = \frac{t}{1+t}$.

c) If
$$y = \sin\left(m \sin^{-1} x\right)$$
 then show that
 $\left(1 - x^2\right)y_2 - xy_1 + m^2y = 0.$

- 11. a) If $y = a \sin(mx) + b \cos(mx)$ then show that $\frac{d^2y}{dx^2} = m^2 y.$
 - b) If $A = \begin{pmatrix} 2 & 4 \\ 1 & 3 \end{pmatrix}$ and $B = \begin{pmatrix} -1 & 0 \\ 5 & 1 \end{pmatrix}$ then verify that $(AB)^{-1} = B^{-1}A^{-1}$.

c) Prove that
$$\sqrt{3} \sin x + 3\cos x$$
 has a maximum at $x = \frac{\pi}{6}$.

12. a) If
$$u = x^2 + y^2 + z^2$$
 then show that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} + z \frac{\partial u}{\partial z} = 2u$.

b) Find the equation of the ellipse which meets the straight line $\frac{x}{7} + \frac{y}{2} = 1$ on the *x*-axis and the straight line $\frac{x}{3} + \frac{y}{5} = 1$ on the *y*-axis and whose axes lie along the axes of coordinates. Determine the foci of the ellipse.

c) Evaluate
$$\int e^{x} \left(\frac{1}{x} - \frac{1}{x^{2}}\right) dx$$
.

CS/BBA (H)/BIRM/BSCM/SEM-2/BBA 202/2011
13. a) Find the maximum and minimum value of the function

$$f(x) = x^3 + \frac{1}{x^3}$$
.
b) Prove that $\begin{vmatrix} 1 & b+c & b^2+c^2 \\ 1 & c+a & c^2+a^2 \\ 1 & a+b & a^2+b^2 \end{vmatrix} = (a-b)(b-c)(c-a).$

c) Find the area above the *X*-axis bounded by x - 2y + 4 = 0, x = 1 and x = 9.