

CONTROL System

①

- It is a system that is required in every type of applications in day to day life for maintaining the input according to desired output.
- A control system is a system that compares the actual output with a reference input and gives the desired output.

* Advantage of control system.

- Quality of the system is improved.
- Productivity increase.
- Overall cost of energy production reduces.
- Control system is mainly two types.
 - 1) open loop system.
 - 2) closed loop system.
 - automatic washing machine.

closed loop - Ac

Fridge - Refrigeration.

* Types of control system.

- 1) Linear and Non-Linear control system.
- 2) Time variant and Time varying system.
- 3) continuous time and discrete time system.
- 4) Dynamic and static system.
- 5) single input and single output.
- 6) Deterministic and stochastic system.

Linear and Non Linear

(2)

It is a system that possesses homogeneity and superposition properties.

Superposition position:-

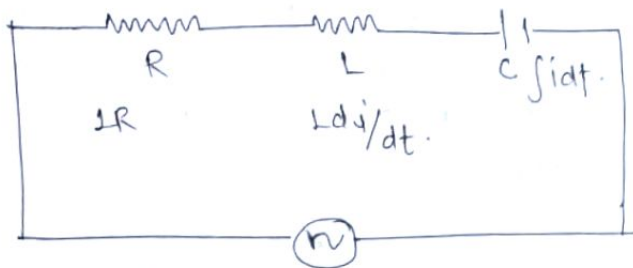
It states that if it is an input $x_1(t) \rightarrow c_1(t)$ and another input $x_2(t) \rightarrow c_2(t)$ then if we combine the input the total system output will be the sum of each output Homogeneity.

When the behaviour of the system is the same for different input is called as homogeneity property.

→ Opposite of Linear System.

The system does not possess.

Time invariant and Time variant



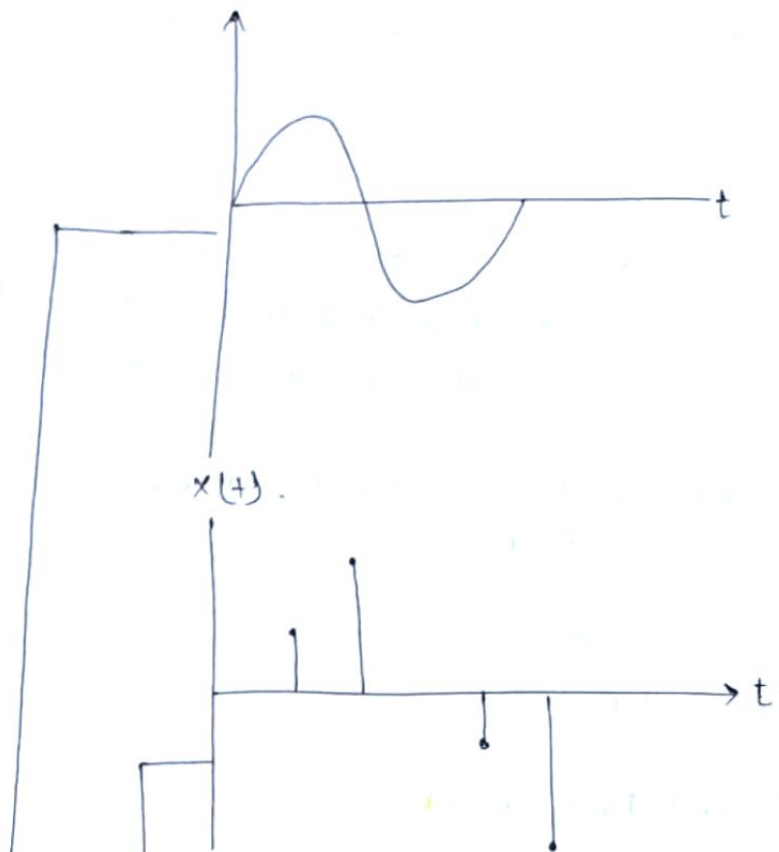
$$V = iR + L \frac{di}{dt} + C \int i dt$$

∴ If the parameter of the system (RLC) does not vary with time the system is called as time invariant system.

• If any of the parameter (one or more) changes its behaviour with time it is called as the time varying system.

a. Continuous time:-

③



Suppose a function $x(t)$ is defined for every instant of time and the value is changing at any instant is called as continuous time system.

If the function $x(t)$ is defined for a specific instant of time the system is called discrete time.

Static system.

In a system the input and output does not change with time.

e.g:- DC electrical circuit with Resistor.

In a system is the output changes even when input is constant is called.

dy.s.

→ AC circuits.

Deterministic and stochastic.

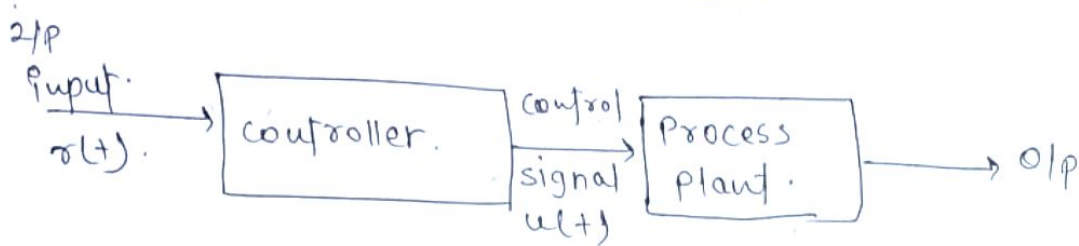
(4)

Deterministic :-

In a system for a given input if the system output one defined or can be calculated easily is called as deterministic.

for a given input if the output is uncertain and can be only predicted then the system.

Open loop control System.



It is type of control system where the control action body depends on the input signal and independent of output response.

Examples :-

Advantages.

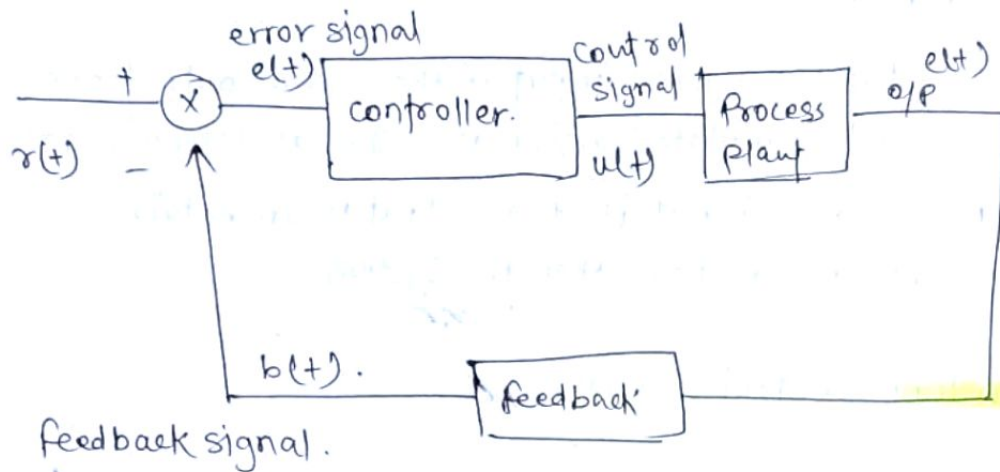
- It is simple to design and construct
- It is economically
- The maintenance cost is very low.
- It provides highly stable operation.

Cons.

It is not accurate when the system input or parameters are variable in nature that's way recalibration of the parameters is required from time to time.

closed loop control System.

(5)



- It is a type of control system where the control action depends on input signal and output response.

example:- automatic iron.

The difference between the actual output of the system and the desired output.

Advantages:-

- It has more accurate operation as comparison to open loop system.
- It can operate efficient even the system inputs or parameter varying in nature.
- It is complex system and costly (disadvantage).
- Time to time re configuration of parameter is not required as there is a facility of automation.

open loop

- 1.) No feedback is given to c.s
- 2.) It cannot be intelligent.
- 3.) As the input is mostly constnt. there is no possibility of system oscillation.

closed loop

- 1.) A feedback is applied.
- 2.) As automation is available it is a intelligent control system.
- 3.) As the system parameter or varying in nature it introduces system oscillation.

4) The output will not vary for constant input.

5) Error detection is not present.

6) It is mostly a stable system

7) It is simple in design and economic

8) It is effected by non linearity

9) The system output vary depends upon feedback loop. (6)

5) Error detection is present.

6) It is prone to instability

7) It has complex structure and costly.

8) its not affected by non linearity.

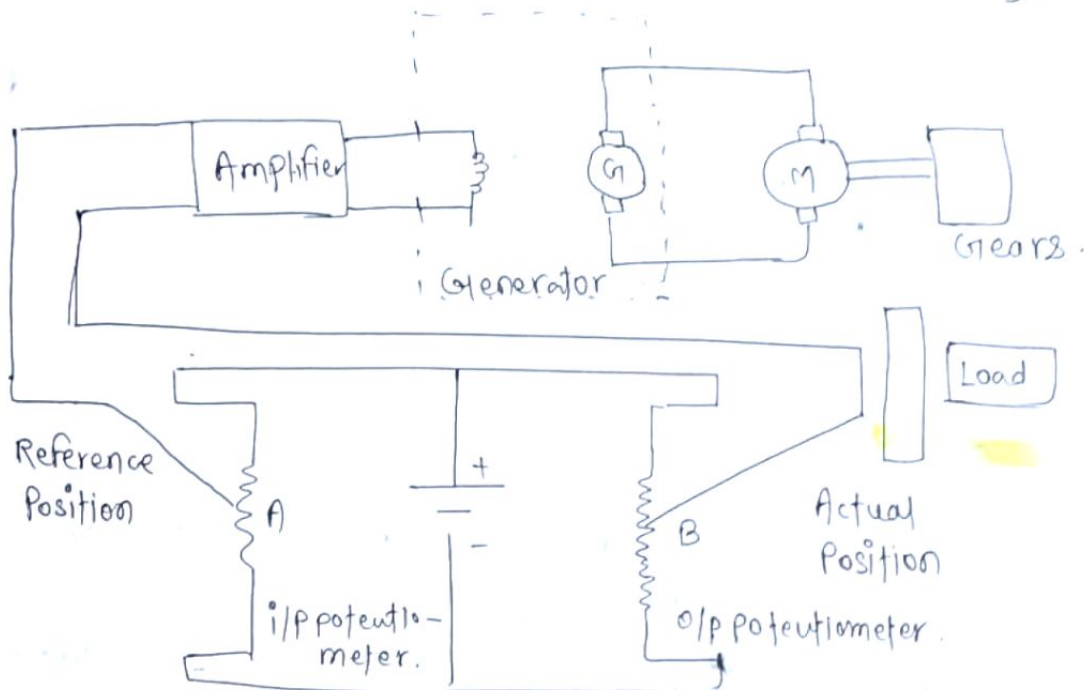
servo Mechanism

- Block diagram representation of Industrial system. (1)

* Servomechanism :-

It is a type of control system mainly used as feedback unit in Mechanical system where both the input and output signal are Mechanical in nature.

- The output signal is directly fed to the comparator
- The control variables are either position signal, velocity or acceleration (Mechanical signal).



Examples :-

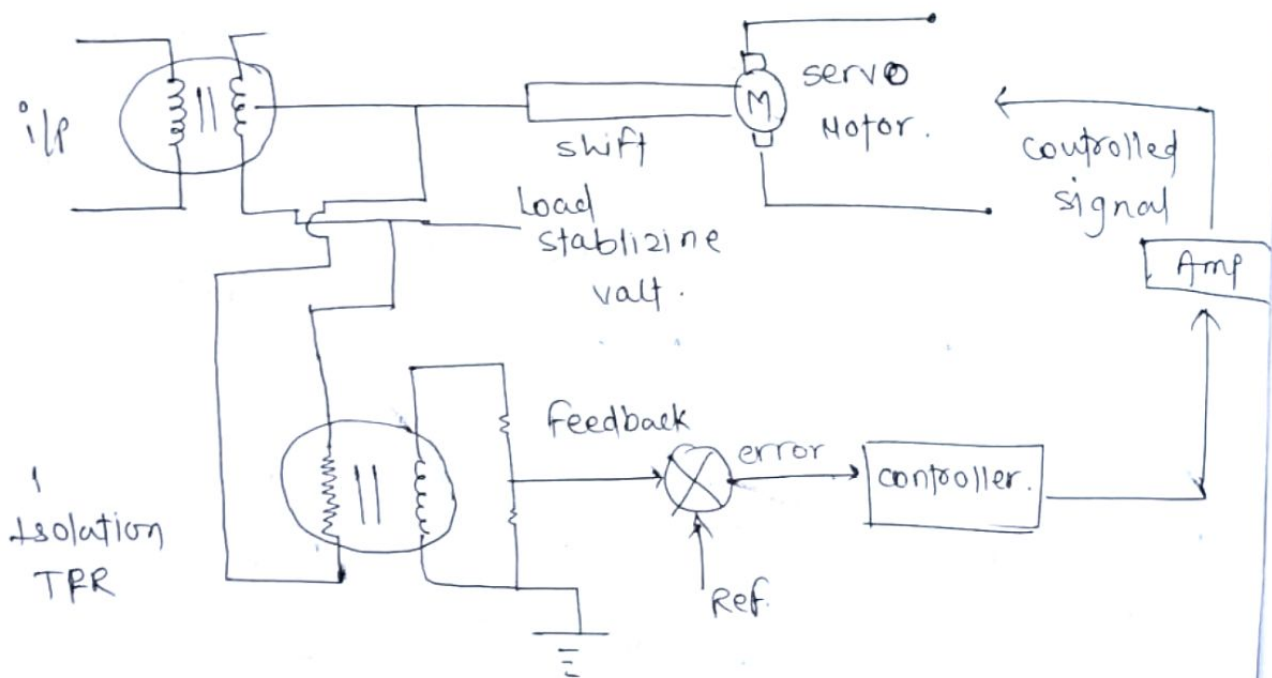
- used in missile launcher
- Machine tool position control
- Power steering of automobile vehicles



* Regulator :-

(8)

It is a feedback unit that is used in electromechanical system where the output is ~~for~~ constant w.r. of ~~constant~~ the output.



* Servomotor :-

It is an linear actuator that is used for the control of linear position velocity and acceleration.

• Here the Motor is ~~coupl~~ ~~coupled~~ coupled with sensor that is used in automated system

* Isolation Transformer :-

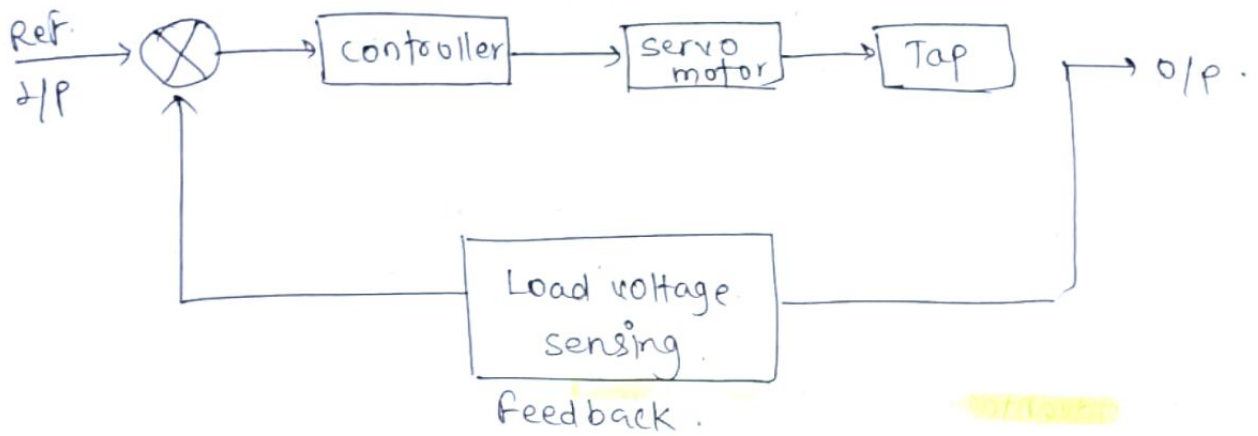
It is the transformer that transfer power from the main A.C source to the device while isolating the Power Device from the Main supply for protection purpose.

• It mainly protect againsts voltage and current ~~against~~ surges.

• It transfer power between two circuit which are not connected electrical.

Regulator :-

(9)



Example of Regulating System

- speed governor
- Temperature Regulation
- frequency Regulation.

Laplace Transform of a common function.

function	Time domain $x(t) = L\{x(s)\}$	Function domain
Delay	$\sigma(t \cdot 2)$	e^{-2s}
unit impulse	$\sigma(t)$	
unit step	$u(t)$	$1/s$
Ramp		$1/s^2$
Exponential decay	$e^{-\alpha t}$	$1/(s + \alpha)$
Exp. approach	$1 - e^{-\alpha t}$	$\alpha / (s + \alpha)$
sine	$\sin \omega t$	$\omega / (s^2 + \omega^2)$

cosine	$\cos \omega t$	$\frac{s}{s^2 + \omega^2}$
my parabolic sine	$\sinh \alpha t$	$\frac{\alpha}{s^2 - \alpha^2}$
hyperbolic cosine	$\cosh \alpha t$	$\frac{s}{s^2 - \alpha^2}$
Exp. delay sine	$e^{-\alpha t} \sin \omega t$	$\frac{\omega}{(s + \alpha)^2 + \omega^2}$
cosine	$e^{-\alpha t} \cos \omega t$	$\frac{s + \alpha}{(s + \alpha)^2 + \omega^2}$

Solⁿ A LOT.

→ LOT can be.

$$N(s) = \frac{A(s)}{B(s)}$$

The denominator can be divided into 3 type.

- unrepeated factor.
- Repeated factor.
- Unrepeated complex factor.

a) unrepeated factor :-

$$\frac{N(s)}{(s+a)(s+b)} = \frac{A}{(s+a)} + \frac{B}{(s+b)}$$

b) Repeated factor :-

$$\frac{N(s)}{(s+a)^2} = \frac{A}{(s+a)^2} + \frac{B}{(s+a)}$$

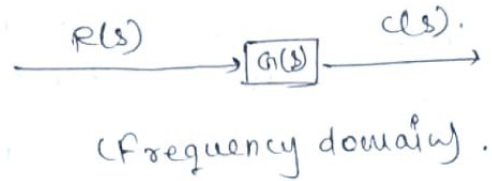
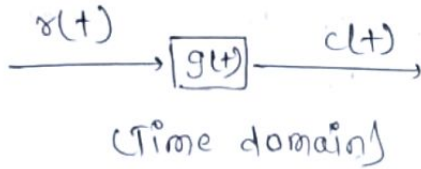
c) Unrepeated complex factor.

$$\frac{N(s)}{(s+a)(s+\bar{a})} = \frac{As+B}{(s+a)^2 + B^2}$$

TRANSFER function :-

(12)

It represents the Ratio of L.T of the o/p of a system to the L.T of i/p of the system, to the L.T of i/p of the system.



$$\text{L.T } \Rightarrow G(s) = \frac{C(s)}{R(s)}$$

initial condition.

Property Transfer func :-

- Zero initial condition.
- It is same as L.T of its impulse response.
- by $\frac{d}{dn}$ function on the transfer function the differential equation can be obtained.

- Stability can be none.
- It can be only applicable in linear system.

Advantage of T.f :-

- 1.) It is the mathematical representation the gain of the system.
- 2.) The impulse response can be found.

Disadvantage :-

(13)

- 1) It is not applicable if the initial condition are neglected.
- 2) It give no information about actual structure physical system.
- 3) The poles of the transform function are those value of 's' which make the transfer function tend to ∞ .
- 4) The 'zero's' of the transfer function are thus value of 's' which make the transfer function tend to zero.
- 5) If either 'poles or zero' consider then such types of poles or zero are calculated Multiple pole or Multiple zero.

$$G(s) = \frac{50(s+3)}{s(s+2)(s+4)^2} = 0$$

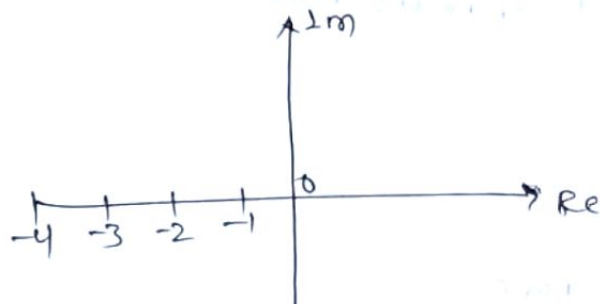
Poles (x) on zeros (o) .

$$s = 0$$

$$s = -3$$

$$s = -2$$

$$s = -4.$$



Signal flow graph (page-17).

=



The poles of the transfer function are those values of s which make the transfer function tend to infinity. (14)

$$G(s) = \frac{50(s+3)}{s(s+2)(s+4)^2} \quad \begin{array}{l} \text{(Poles)} \\ \text{zero.} \end{array}$$

The zero's of the transfer function are those value of s which make the transfer function tend to zero.

- If either poles or zero go inside then such type of poles or zero are called multiple pole and multiple zero.

$$G(s) = \frac{50(s+3)}{s(s+2)(s+4)^2} = 0$$

Poles(zero(s))

$$s = 0 \quad s = -3$$

$$s = 2$$

$$s = 4$$

A system having input $x(t)$ and output $y(t)$ is represented by

$$\frac{dy(t)}{dt} + 4y(t) = \frac{dx(t)}{dt} + 5x(t).$$

$$\frac{dy(t)}{dt} + 4y(t) = \frac{dx(t)}{dt} + 5x(t)$$

$$y(t) \xrightarrow{\text{Lap}} y(s)$$

$$\left[\frac{dy(t)}{dt} + 4y(t) \right] = \left[\frac{dx(t)}{dt} + 5x(t) \right] \quad \frac{dy(t)}{dt} \xrightarrow{\text{Lap}} \text{sys}$$

$$s y(s) + 4y(s) = s x(s) + 5x(s).$$

$$y(s) [s+4] = x(s) [s+5]$$

$$\boxed{\frac{y(s)}{x(s)} = \frac{(s+5)}{(s+4)}}$$

Q:- The transfer function of the system is given by

(15)

$$G(s) = \frac{4s+1}{s^2+2s+3}$$

Find the differential eqn of the system having input $x(t)$ and output $y(t)$.

Ans:- Input $x(t) \xrightarrow{L.T} x(s)$
output $y(t) \xrightarrow{L.T} y(s)$.

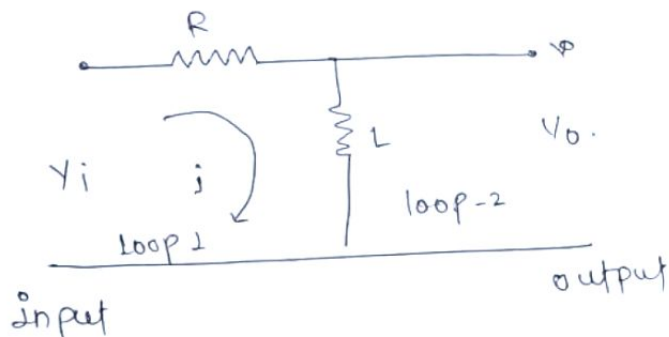
$$G(s) = \frac{y(s)}{x(s)} = \frac{4s+1}{s^2+2s+3}$$

$$= y(s)(s^2+2s+3) = x(s)(4s+1)$$

$$= s^2 y(s) + 2s y(s) + 3 y(s) = 4s x(s) + x(s)$$

$$= \frac{d^2 y(t)}{dt^2} + 2 \frac{dy(t)}{dt} + 3 y(t) = 4 \frac{dx(t)}{dt} + x(t)$$

Ques:- Find the transfer function of the given network



$$V_i(t) = R i(t) + L \frac{di(t)}{dt}$$

$$V_o(t) = L \frac{di(t)}{dt}$$

taking Lapalce transfer

$$V_i(s) = R I(s) + s L I(s)$$

$$V_o(s) = s L I(s)$$

$$T.F = \frac{V_o(s)}{V_i(s)} = \frac{s L I(s)}{R I(s) + s L I(s)} = \frac{s L}{(R + s L)}$$

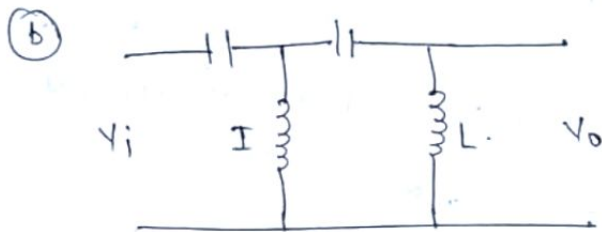
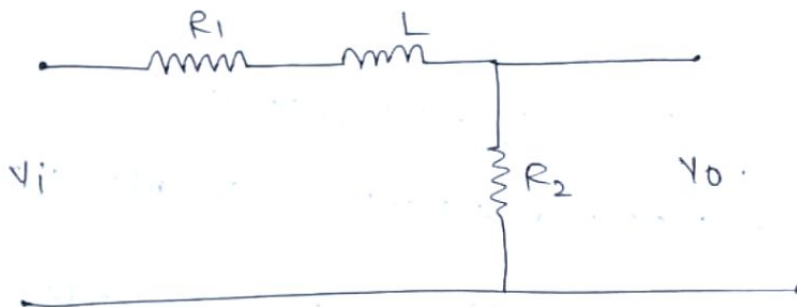
① for the given differential eqn. find transfer function. (16)

① $a > \frac{d^2y}{dt^2} + 10 \frac{dy}{dt} - 5y = 3x.$

② $b > \frac{d^2y}{dt^2} + 3y = 5x.$

$y(t) \rightarrow$ output. $x(t) \rightarrow$ input.

② determine the transfer function of a given network.



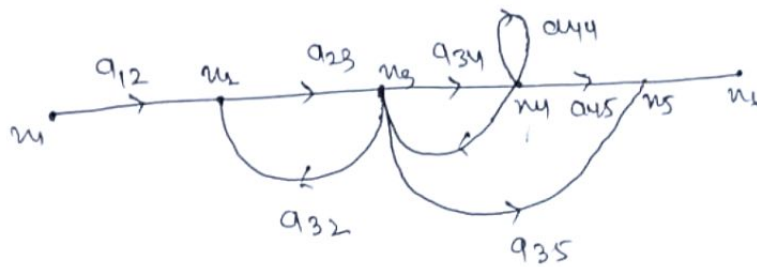
if $L = 1H.$

$C = 2F.$

Signal Flow Graph:-

The process of block diagram reduction was developed by S.J Mason.

- This method does not require any reduction technique.
- It is a diagram which represents a set of simultaneous equations.
- It is applicable to linear time invariant systems.
- Each variable is represented by a node, connected by a direct line called branches.
- Every branch having an arrow represents the flow of signal.



1) Input Nodes / source Node:-

It has only outgoing branches. $\rightarrow x_1$

2) Output Node / sink nodes:-

It has only one or more incoming branches. $\rightarrow x_4$

3) Mixed Nodes:-

A node having incoming as well as outgoing branches. $- x_2, x_3, x_4, x_5$

4.) Transmittance :-

(18)

It is also known as transfer function which is normally written on the branch near the arrow. - a_{12}, a_{23}, a_{32} etc

5.) forward path :-

It originates from the input nodes and terminates at the output node and along which no node is traversed more than one.

$$1) x_1 - x_2 - x_3 - x_4 - x_5 - x_6$$

$$2) x_1 - x_2 - x_3 - x_5 - x_6$$

6.) Loop :-

It is a path that originates and terminates on the same nodes and along which no other node is traversed more than one.

$$x_2 - x_3 - x_2$$

$$x_3 - x_4 - x_3$$

7.) self Loop :-

It is a path which originates and terminates on the same node and does not require other nodes to complete the loop.

8.) Path Gain :- The product of the branch gains along the path is called path gain

for forward path 1

$$\text{Gain} :- a_{12}, a_{23}, a_{34}, a_{45} \cdot 1$$

for forward path 2

$$\text{Gain} :- a_{12}, a_{23}, a_{35} \cdot 1$$

9.) Loop Gain :-

$$\text{Loop 1} :- a_{23}, a_{32}$$

$$\text{Loop 2} :- a_{31}, a_{43}$$

$$\text{Loop 3} :- a_{44}$$

10.) Non touching Loop :- It has having no common nodes and branches path.

$$x_2 \text{ to } x_3 \text{ and } x_4 - x_5$$

The Gain of signal flow graph is given by Mason's Gain formula. (19)

Mason's Gain formula \rightarrow

$$T(s) = \frac{\sum g_k \Delta_k}{\Delta}$$

T(s) :- Transfer function / Gain of the overall system.

$\Delta = 1 -$ [sum of all individual loop gain]

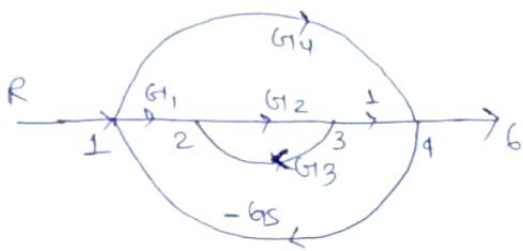
+ [sum of all possible gain products of two non touching loops]

$-$ [sum of all possible gain products of three non-touching loops]

$\Delta_k =$ the part of Δ not touching the k^{th} forward path.

$g_k =$ Gain of the k^{th} forward path.

Q:- 7-Dec



No of forward path (k) = 2. 20

Path-I 1-2-3-4.

Path-II 1-4

Gain of forward path I (G₁) = G₁G₂G₄
 " " " " I₁(G₂) = G₄

No. of Individual Loops = 3.

$$L_1 (2-3-2) = G_2 G_3$$

$$L_2 (1-2-3-4-1) = -G_1 G_2 G_3 G_4$$

$$L_3 (1-4-1) = G_4 + G_5 - G_4 G_5$$

Two non touching Loop (L₁, L₃).

$$L_1 L_3 = -G_2 G_3 G_4 G_5$$

$$\Delta = 1 - [L_1 + L_2 + L_3] + L_1 L_3$$

$$\Delta_1 = 1 - 0 = 1 \quad (\text{forward path 1})$$

$$\Delta_2 = 1 - G_2 G_3 \quad (\text{" " 2})$$

$$\text{If T.F} = \frac{C}{R} = \frac{\sum g_k \Delta_k}{\Delta}$$

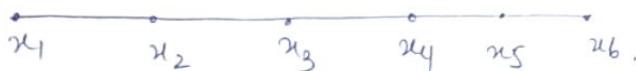
$$= \frac{g_1 \Delta_1 + g_2 \Delta_2}{\Delta}$$

$$= \frac{G_1 G_2 - 1 + G_4 (1 - G_2 G_3)}{1 - (G_2 G_3 + (-G_1 G_2 G_3) + (-G_4 G_5) + (-G_2 G_3 G_4 G_5))}$$

$$1 - (G_2 G_3 + (-G_1 G_2 G_3) + (-G_4 G_5) + (-G_2 G_3 G_4 G_5))$$

$$\text{T.F.} = \frac{G_1 G_2 + G_4 - G_2 G_3 G_4}{1 - G_2 G_3 - G_1 G_2 G_3 - G_4 G_5 - G_2 G_3 G_4 G_5}$$

e.g.



$$x_2 = a x_1 + b x_5$$

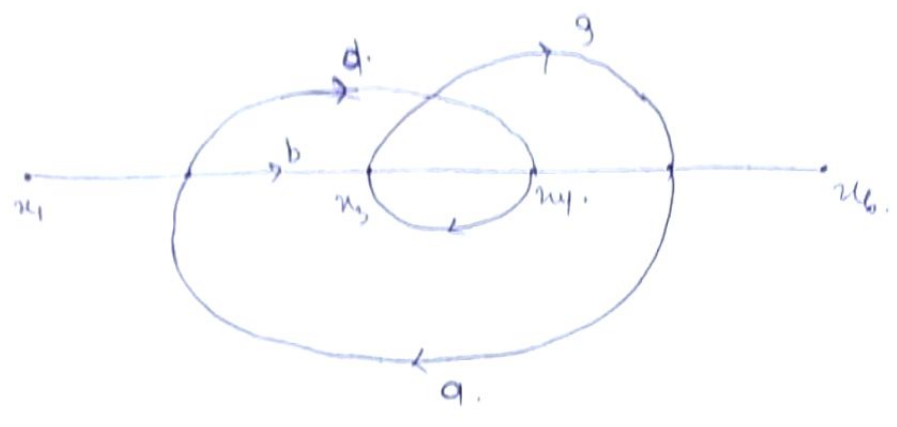
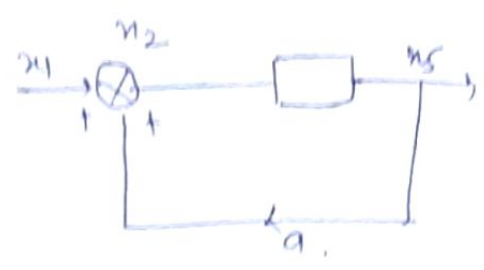
$$x_3 = c x_2 + d x_4$$

$$x_4 = e x_2 + f x_3$$

$$x_5 = g x_4 + h x_3$$

$$x_6 = x_5$$

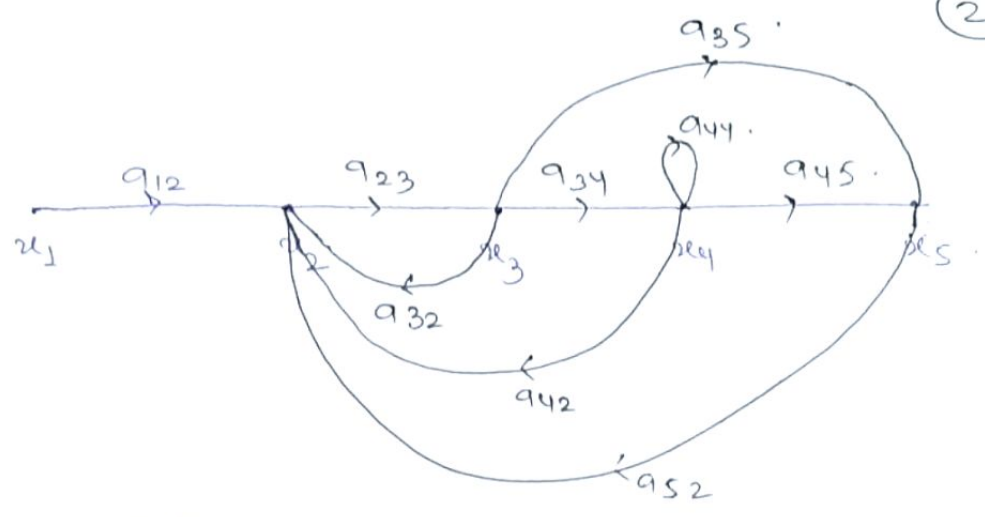
$x_2 = a_1 x_1 + a_2 x_5$
 $x_3 = b x_2 + c x_4$
 $x_4 = d x_2 + e x_3$
 $x_5 = f x_4 + g x_3$
 $x_6 = x_5$



(3) For the systems represented by given equations. Find T.F $\frac{x_5}{x_1}$ by the help of signal flow graph technique.

$x_2 = a_{12} x_1 + a_{32} x_3 + a_{42} x_4 + a_{52} x_5$
 $x_3 = a_{23} x_2$
 $x_4 = a_{34} x_3 + a_{44} x_4$
 $x_5 = a_{35} x_3 + a_{45} x_4$

$x_1 \rightarrow$ input.
 $x_5 \rightarrow$ output.



No. of forward path (K) = 2

Path I = $x_1 - x_2 - x_3 - x_4 - x_5$

Path II = $x_1 - x_3 - x_5$

Gain of forward path I (g_1) = $g_{12} g_{23} g_{34} g_{45}$

Gain of forward path II (g_2) = $g_{13} g_{35}$

No. of individual Loop = 5

$L_1 (x_2 - x_3 - x_2) = g_{23} g_{32}$

$L_2 (x_2 - x_3 - x_4 - x_2) = g_{23} g_{34} g_{42}$

$L_3 (x_2 - x_3 - x_4 - x_5 - x_2) = g_{23} g_{34} g_{45} g_{52}$

$L_4 (x_2 - x_3 - x_4 - x_2) = g_{35} g_{45} g_{34} g_{23} g_{35} g_{52}$

$L_5 (x_4) = g_{44}$

Two non touching Loop

$(L_1 \cdot L_5)$ and $(L_4 \cdot L_5)$

$L_1 \cdot L_5 = g_{23} g_{32} g_{44}$

$L_4 \cdot L_5 = g_{23} g_{35} g_{52} g_{44}$

$\Delta = 1 - [L_1 + L_2 + L_3 + L_4 + L_5] + (L_1 \cdot L_5 + L_4 \cdot L_5)$

$= 1 - [g_{23} g_{32} + g_{23} g_{34} g_{42} + g_{23} g_{34} g_{45} g_{52} + g_{23} g_{35} g_{52} + g_{44}]$
 $+ (g_{23} g_{32} g_{44} + g_{23} g_{35} g_{52} g_{44})$

$$\Delta_1 = 1 - 0 = 1 \text{ (all nodes are involved)}$$

$$\Delta_2 = 1 - L_5 = 1 - a_{44}$$

$$T.F = \frac{!c}{R} = \frac{g_k \Delta_k}{\Delta}$$

$$= \frac{g_1 \Delta_1 + g_2 \Delta_2}{\Delta}$$

$$= \frac{a_{12} a_{23} a_{34} a_{45} \cdot 1 + a_{12} a_{23} a_{35} (1 - a_{44})}{\Delta}$$

$$= \frac{a_{12} a_{23} a_{34} a_{45} + a_{12} a_{23} a_{35} (1 - a_{44})}{1 - [a_{23} a_{32} + a_{23} a_{34} a_{42} + a_{23} a_{34} a_{45} a_{52} + a_{23} a_{35} a_{52} + a_{44}] + (a_{23} a_{32} a_{44} + a_{23} a_{35} a_{52} a_{44})}$$

Assignment Question.

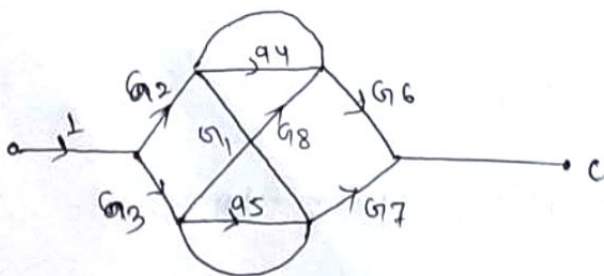
1. Obtain the signal flow graph of T.F through following eqn.

$$x_2 = 9x_1 + 2x_3 + 2x_2$$

$$x_3 = 6x_1 + 5x_2 + 2x_3$$

$$x_4 = 2x_2 + 2x_3$$

2. Obtain the T.F from the signal flow graph.



Answer.

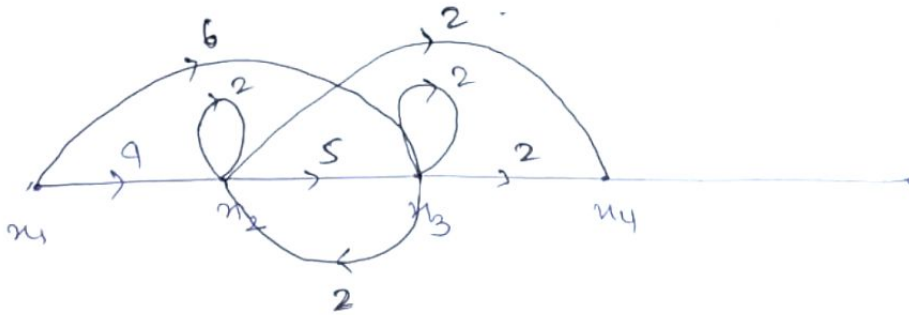
(24)

① Given eqn.

$$x_2 = 4x_1 + 2x_3 + 2x_2$$

$$x_3 = 6x_1 + 5x_2 + 2x_3$$

$$x_4 = 2x_2 + 2x_3$$



No. of forward path. $(K) = 3$.

$$\text{Path 1} = x_1 - x_2 - x_3 - x_4$$

$$\text{Path 2} = x_1 - x_2 - x_4$$

$$\text{Path 3} = x_1 - x_3 - x_4$$

$$\text{Gain of forward path (1)} (g_1) = 4 \times 5 \times 2 = 40$$

$$\text{Gain of forward path 2} (g_2) = 6$$

$$\text{Gain of forward path 3} (g_3) = 4 \times 2 = 8$$

No. of individual loop. = 5.

$$L_1 (x_1 - x_3 - x_2 - x_1) = 6 \times 2 \times 4 = 48$$

$$L_2 (x_4 - x_2 - x_4 - x_2 - x_4) = 4 \times 2 \times 2 \times 5 \times 4 = 320$$

$$L_3 (x_2 - x_3 - x_2) = 5 \times 2 = 10$$

$$L_4 (x_2 - x_2) = 2$$

$$L_5 (x_3 - x_3) = 2$$

Two non touching loop.

$$(L_2 \cdot L_5) \& (L_4 \cdot L_5)$$

$$L_2 \cdot L_5 = 320 \times 2 = 640$$

$$L_4 \cdot L_5 = 2 \times 2 = 4$$

$$\Delta = 1 - [L_1 + L_2 + L_3 + L_4] + [L_2 \cdot L_5 + L_4 \cdot L_5]$$

(25)

$$= 1 - [48 + 320 + 10 + 2 + 2] + [640 + 4]$$

$$= 1 - [382] + [644]$$

$$= 1 - 1026$$

$$= -1025.$$

$$\Delta_1 = 1 - 0 = 1$$

$$\Delta_2 = 1 - L_4 = 1 - 2 = -1.$$

$$\Delta_3 = 1 - L_5 = 1 - 2 = -1.$$

$$T \cdot f = \frac{C}{R} = \frac{\sum K \Delta K}{\Delta}$$

$$= \frac{g_1 \Delta_1 + g_2 \Delta_2 + g_3 \Delta_3}{\Delta}$$

Δ

$$= \frac{40 \times 1 + 6 \times -1 + 8 \times -1}{-1025}$$

$$= \frac{40 - 6 - 8}{-1025} = \frac{40 - 14}{-1025} = \frac{26}{-1025} = -\frac{26}{1025}$$

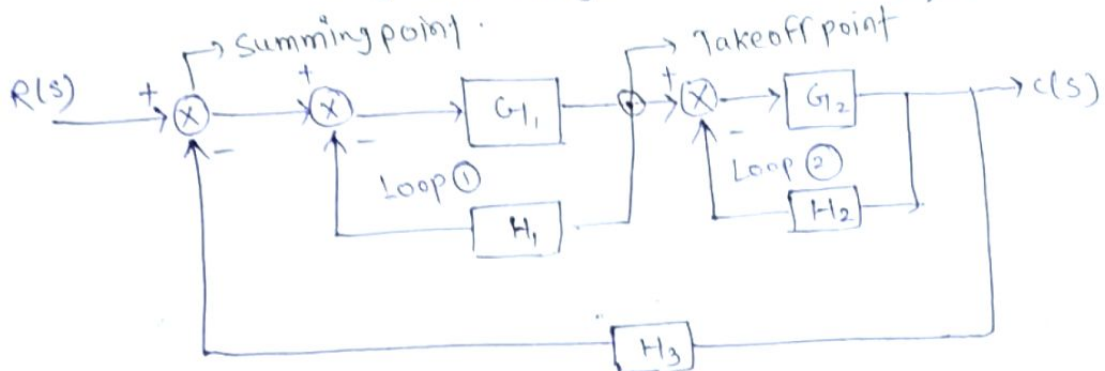
$$T \cdot f = \frac{-26}{1025}$$

Block Diagram Reduction Technique.

(26)

- Block diagram is a pictorial Representation of the complicated control system. It can be Reduced by the Reduction Rule.
- When A No blocks are connected the overall T.F obtained by Block diagram Reduction Technique.

1.) Drive the T.F using Block diagram Reduction Technique



close loop \rightarrow o/p depend on i/p.

There is a relation between o/p and i/p.

Open Loop \rightarrow o/p \nrightarrow not depend on i/p.

This is no any Relation between o/p and i/p.

Step-1:- There are 2 internal Loop. Remove this loop By using the equation

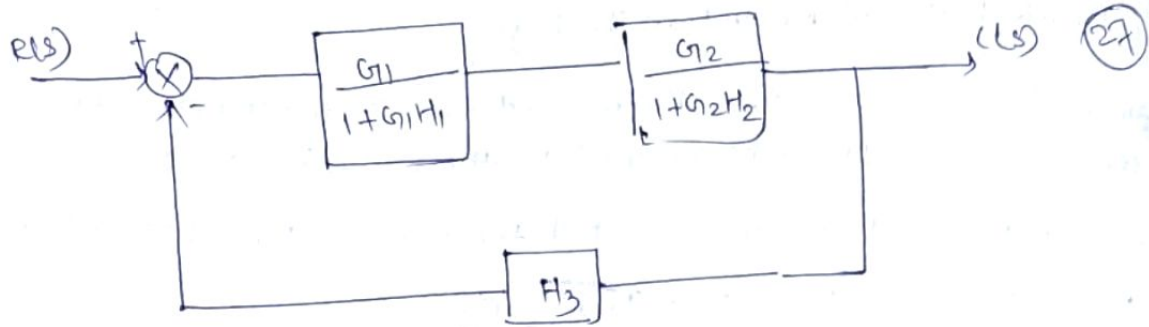
$$\frac{C(s)}{R(s)} = \frac{G(s)}{1 + G(s) \cdot H(s)}$$

Internal Loop - 1.

$$\frac{c(s)}{R(s)} = \frac{G_1(s)}{1 + G_1(s) \cdot H_1(s)} = \frac{G_1(s)}{1 + G_1 H_1} \quad \text{for -ve feedback}$$

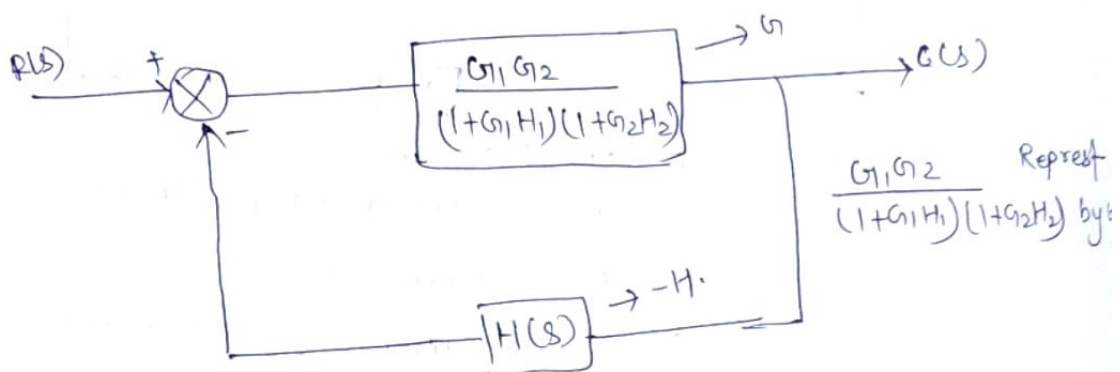
Internal Loop - 2

$$\frac{C(s)}{R(s)} = \frac{G_2(s)}{1 + G_2 H_2}$$



Step 2 :- The 2 Blocks are in cascade after that

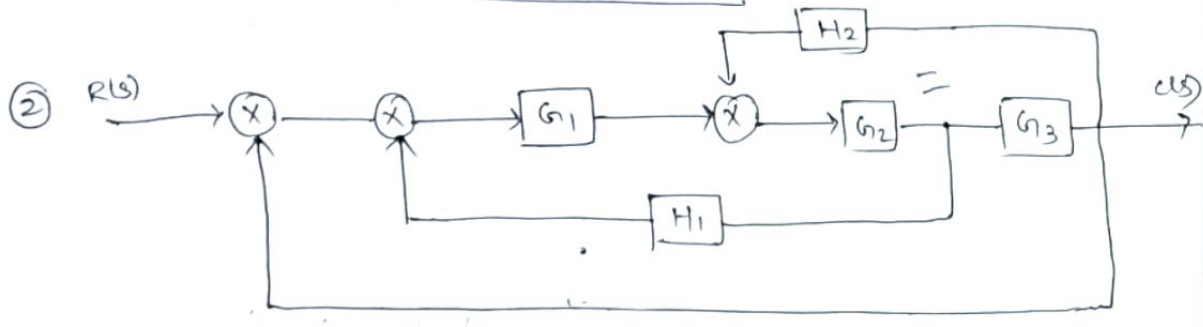
Rule 1 :- When 2 or more block are in cascade (series) The resultant Block is a product of individual Block Transfer function.



step 3:- Use the close loop equation to Reduce the Block.

$$\begin{aligned} \frac{C(s)}{R(s)} &= \frac{G_1}{1 + G_1 H} = \frac{G_1 G_2}{(1 + G_1 H_1)(1 + G_2 H_2)} \\ &= \frac{G_1 G_2}{(1 + G_1 H_1)(1 + G_2 H_2)} \cdot \frac{H_3}{H_3} \\ &= \frac{G_1 G_2}{(1 + G_1 H_1)(1 + G_2 H_2)} \\ &= \frac{G_1 G_2}{(1 + G_1 H_1)(1 + G_2 H_2) + G_1 G_2 H_3} \end{aligned}$$

$$R(s) \rightarrow \left[\frac{G_1 G_2}{(1 + G_1 H_1)(1 + G_2 H_2) + G_1 G_2 H_3} \right] \rightarrow C(s) \quad (28)$$



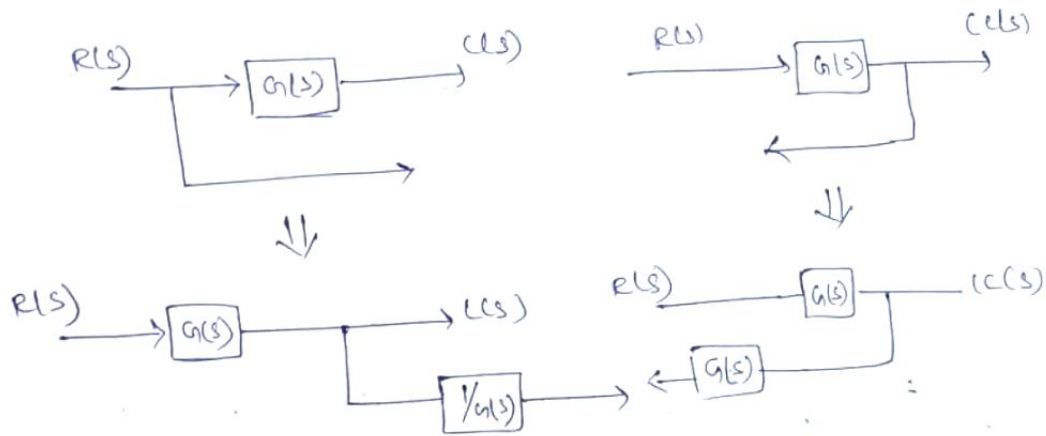
Solution

Step 1 :- shift the take off point beyond the block G_3 .

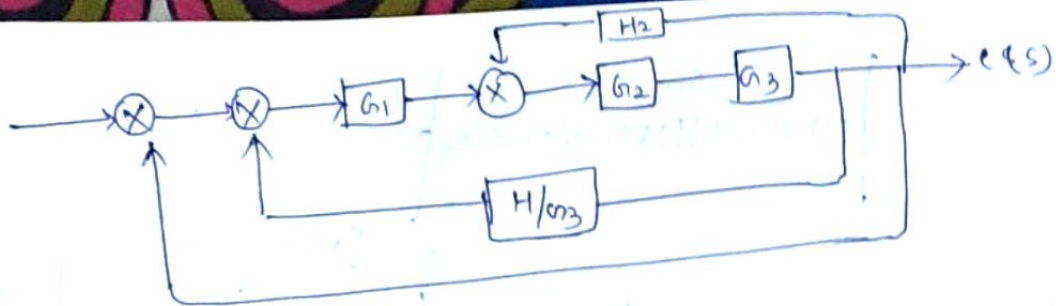
$$\frac{C(s)}{R(s)} = \frac{G(s)}{1 + G(s)H(s)}$$

Rule 4 :- Moving a take off point after the block

If the take off point is move after a block. A block with the Reciprocal with the T.F is introduce in the Branch of a take off point as shown fig:-

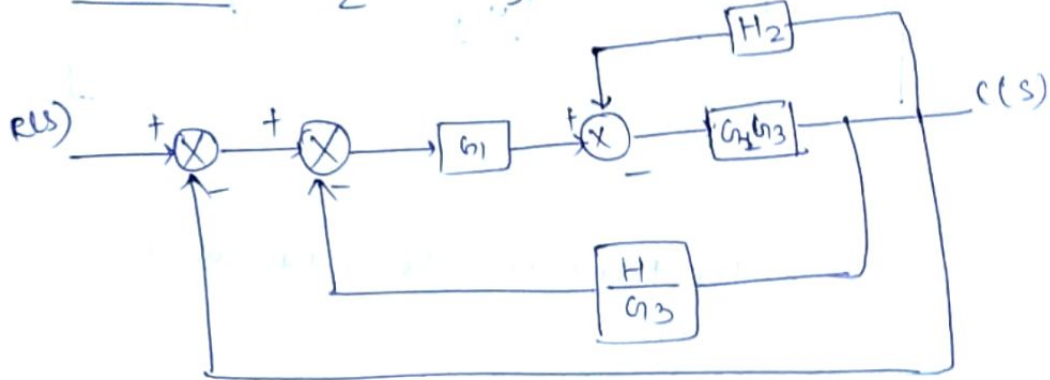


If the take off point is move before a block. A block with the same with the T.F is introduce in the branch of a take off point.



(29)

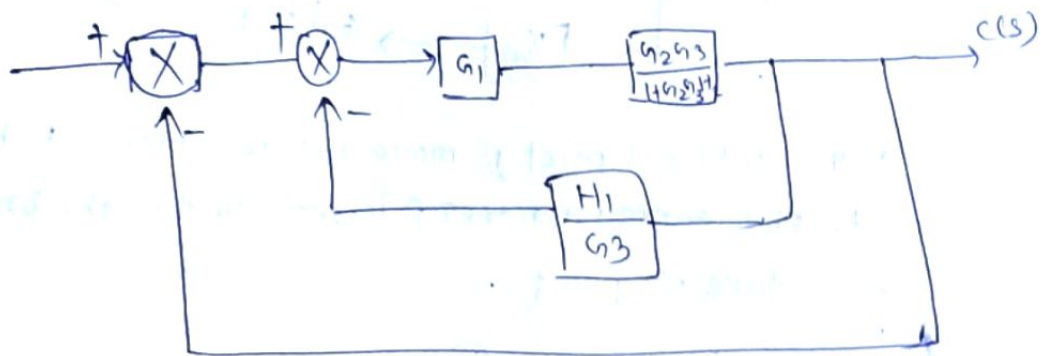
Step 2 :- G_2 and G_3 cascade



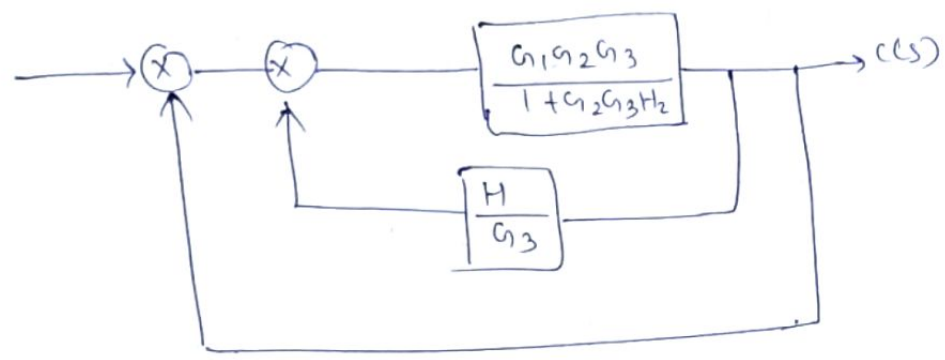
Step 3 :- Reduce the close loop system

where $G_0 = G_2 G_3$ and $H = H_2$

$$\begin{aligned} \frac{C(s)}{R(s)} &= \frac{G_0}{1 + G_0 H} \\ &= \frac{G_2 G_3}{1 + G_2 G_3 \cdot H_2} \\ &= \frac{G_2 G_3}{1 + G_2 G_3 H_2} \end{aligned}$$



step-4:- G_1 and $\frac{G_2 G_3}{1 + G_2 G_3 H_2}$ are cascade.



step 5:- Reduce the closed Loop

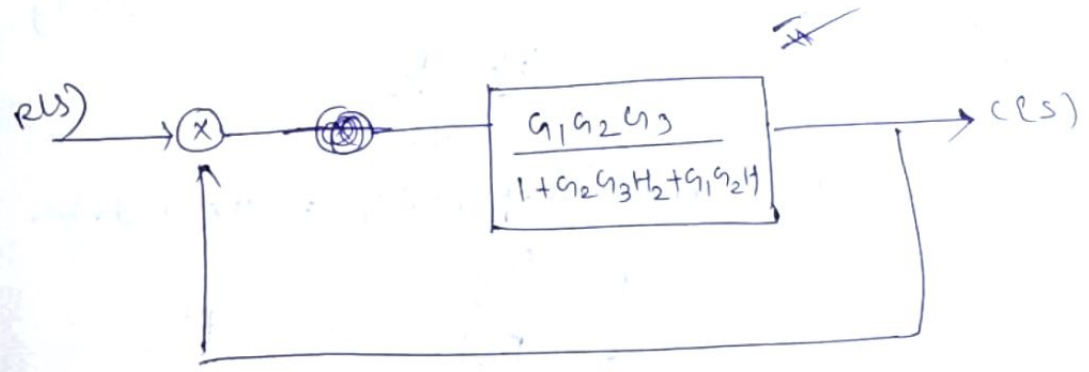
where $G = \frac{G_1 G_2 G_3}{1 + G_2 G_3 H_2}$

and $H = H/G_3$

$$\frac{C(s)}{R(s)} = \frac{G}{1 + GH} = \frac{G_1 G_2 G_3}{1 + G_2 G_3 H_2} \cdot \frac{H}{1 + \frac{G_1 G_2 G_3}{1 + G_2 G_3 H_2} \cdot \frac{H}{G_3}}$$

$$= \frac{G_1 G_2 G_3}{1 + G_2 G_3 H_2 + G_1 G_2 H}$$

$$= \frac{G_1 G_2 G_3}{1 + G_2 G_3 H_2 + G_1 G_2 H}$$



Step 6:- Find the final Transfer function.

(9)

When No given value of H
then $H = 1$

If $H = 0$ no path.

$$\frac{C(s)}{R(s)} = \frac{G(s)}{1+GH} = \frac{G_1 G_2 G_3}{1 + G_2 G_3 H_2 + G_1 G_2 H_1}$$

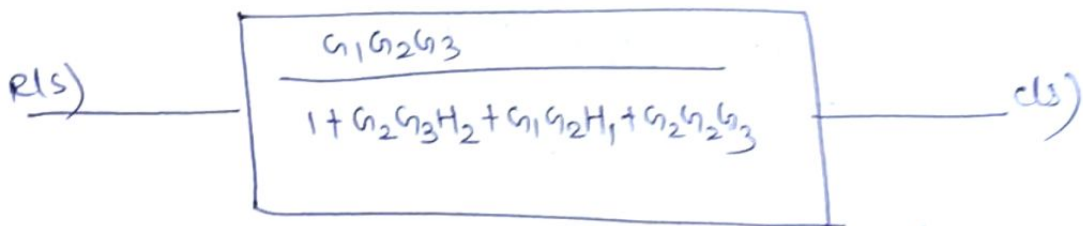
$$= \frac{G_1 G_2 G_3}{1 + G_2 G_3 H_2 + G_1 G_2 H_1 + G_1 G_2 G_3}$$

$$= \frac{G_1 G_2 G_3}{1 + G_2 G_3 H_2 + G_1 G_2 H_1}$$

$$1 + G_2 G_3 H_2 + G_1 G_2 H_1 + G_1 G_2 G_3$$

$$1 + G_2 G_3 H_2 + G_1 G_2 H_1$$

$$= \frac{G_1 G_2 G_3}{1 + G_2 G_3 H_2 + G_1 G_2 H_1 + G_1 G_2 G_3}$$



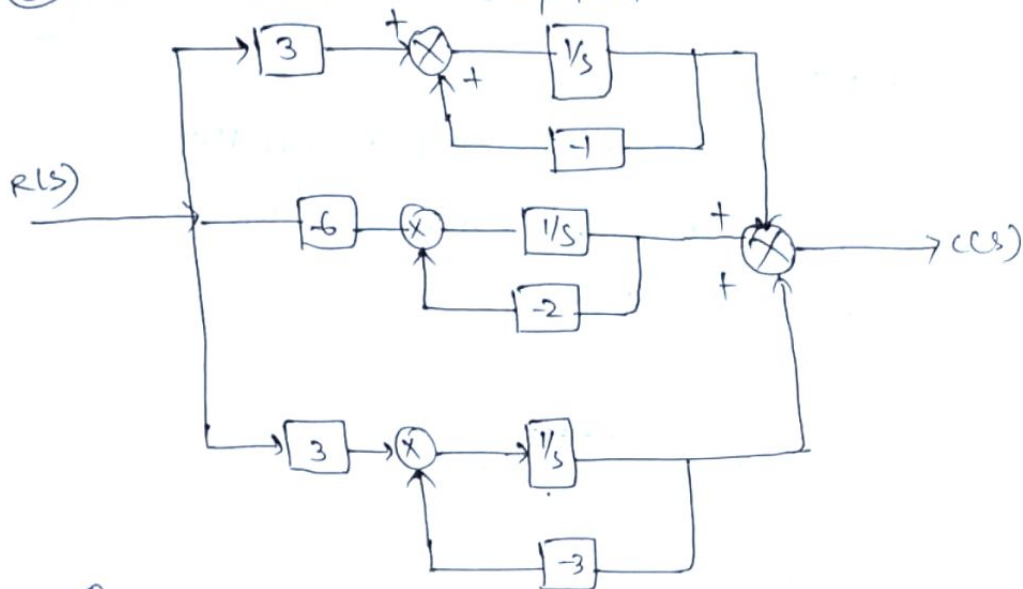
Note:- When block in cascade (series) = Multiply
eg:- $G_1 \rightarrow G_2$
 $G_1 G_2$

When block in parallel = add.



3) Find the T.F of the system

32



Solⁿ :-

Reduce close loop system

$$\text{Loop 1} := \frac{C(s)}{R(s)} = \frac{G}{1-GH} \quad (\text{+ve feedback})$$

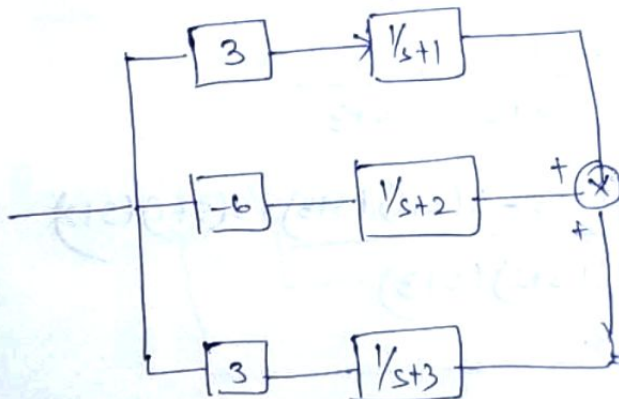
$$= \frac{1/s}{1 - [1/s \cdot -1]}$$

$$= \frac{1/s}{1 + 1/s} = \frac{1/s}{\frac{s+1}{s}} = \frac{1}{s+1}$$

simillary

$$\text{Loop 2} := \frac{C(s)}{R(s)} = \frac{G}{1-GH} = \frac{1}{s+2}$$

$$\text{Loop 3} := \frac{C(s)}{R(s)} = \frac{G}{1-GH} = \frac{1}{s+3}$$



Case #

(33)

Rule 2. Rules

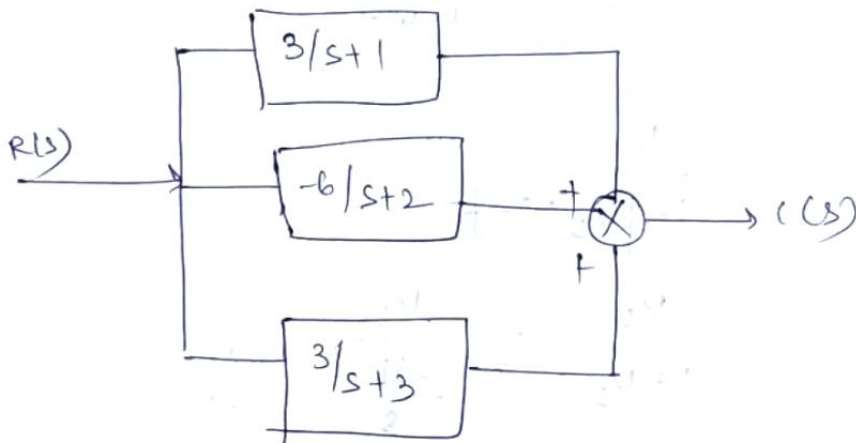
When 2 or more Block parallel is parallel
the Resultant Block is the sum of
Individual Block T.F.

step :- 2

3 and $\frac{1}{s+1}$ cascade

-6 and $\frac{1}{s+2}$ "

3 and $\frac{1}{s+3}$ "



⊙ $\frac{3}{s+1}$ and $\frac{-6}{s+2}$ and $\frac{3}{s+3}$ are in parallel

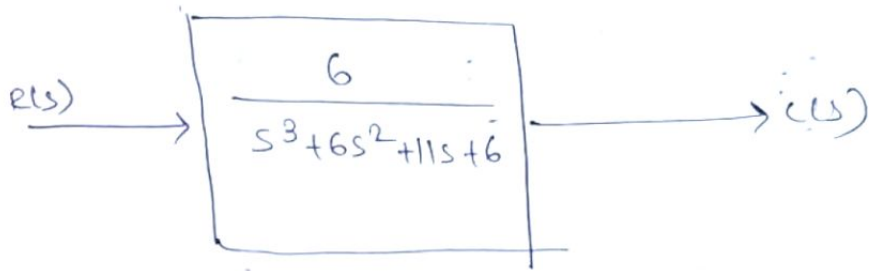
then
$$\frac{e(s)}{R(s)} = \frac{3}{(s+1)} + \left(\frac{-6}{s+2}\right) + \frac{3}{s+3}$$

$$= \frac{3}{s+1} - \frac{6}{s+2} + \frac{3}{s+3}$$

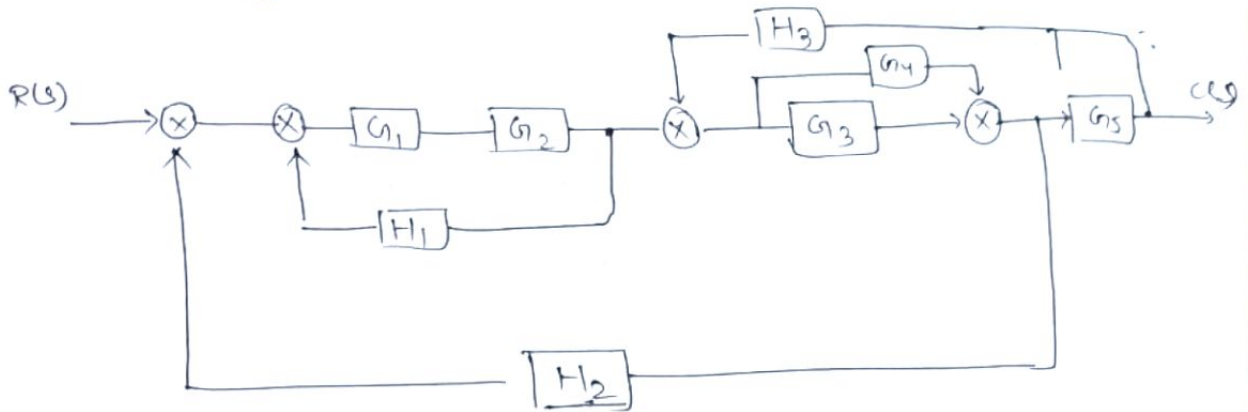
$$= \frac{3(s+2)(s+3) - 6(s+1)(s+3) + 3(s+1)(s+2)}{(s+1)(s+2)(s+3)}$$

$$= \frac{6}{s^3 + 6s^2 + 11s + 6}$$

3W

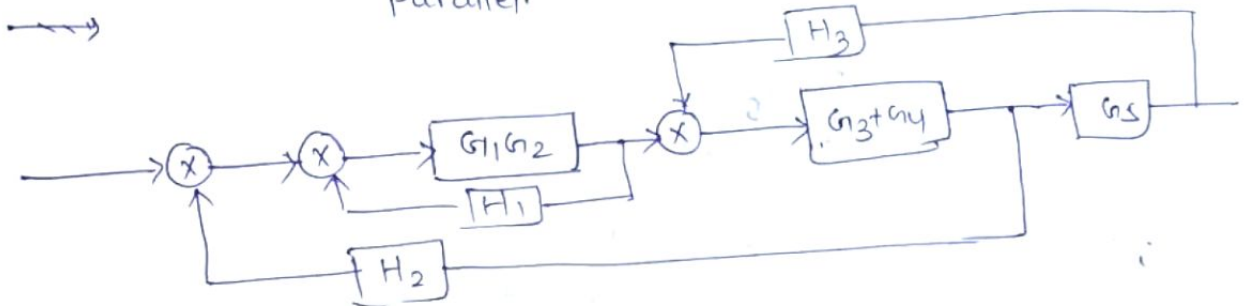


Question.



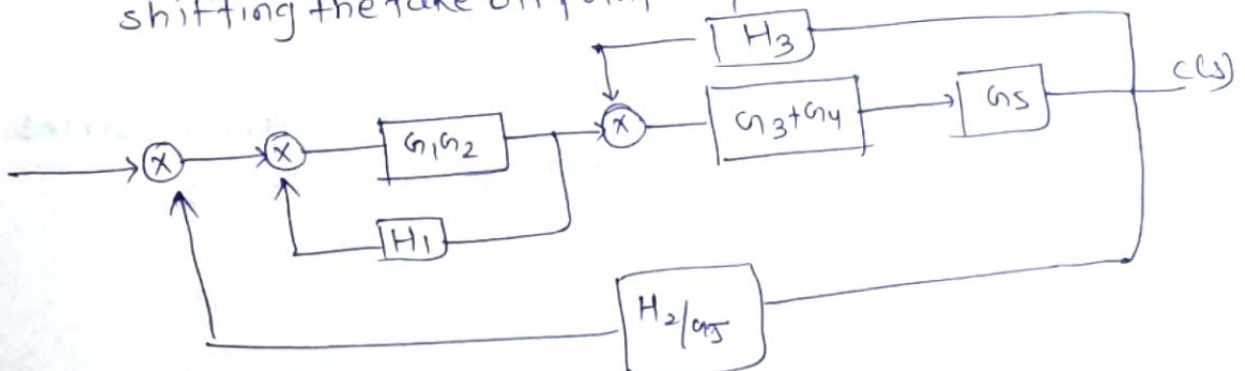
Solve:

Step 1: G_1, G_2 are in series and G_3 and G_4 are parallel.



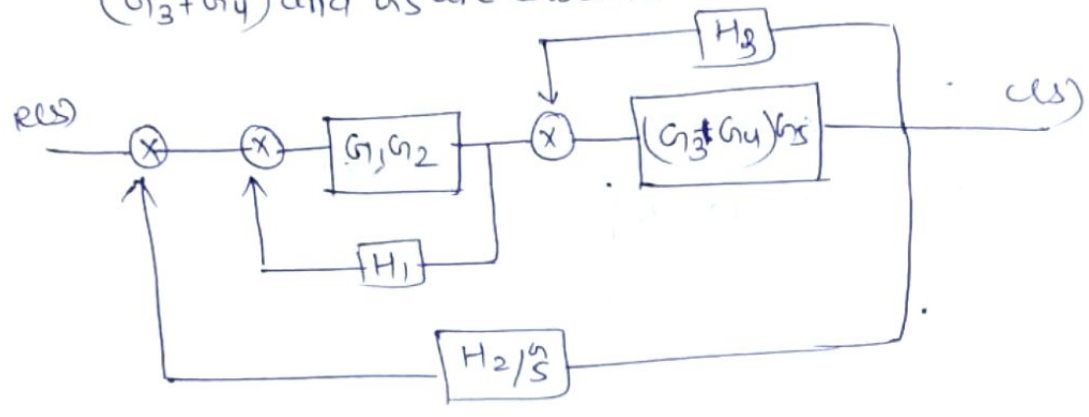
Step 2

shifting the take off point beyond the block G_5 .



step 3.

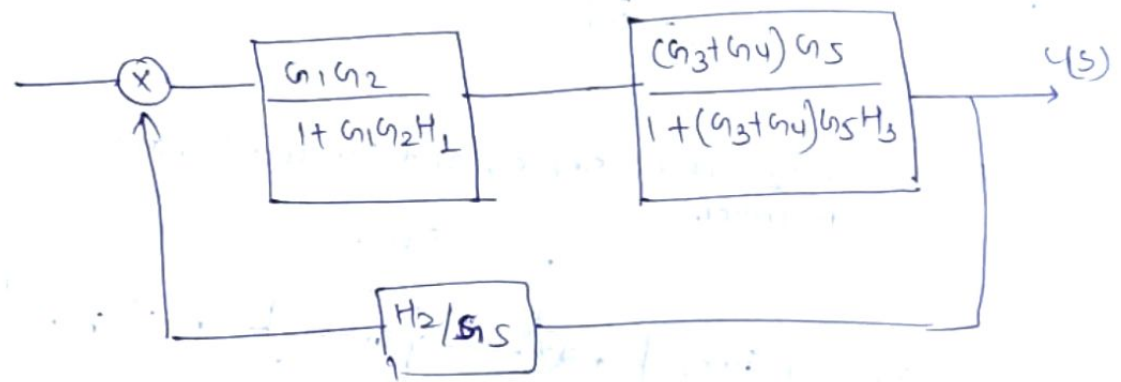
$(G_3 + G_4)$ and G_5 are cascade.



step 4.

Resolve the closed loop

where -
 $G = G_1 G_2$ and $G = (G_3 + G_4) G_5$
 $H = H_1$ $H = H_3$



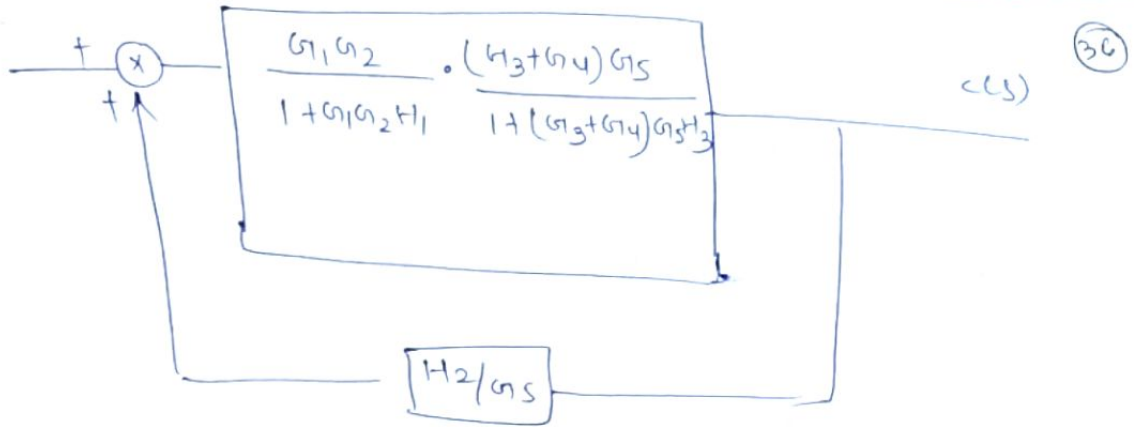
case I.

$$\frac{G(s)}{R(s)} = \frac{G}{1+GH} = \frac{G_1 G_2}{1 + G_2 G_2 H}$$

case II

$$\frac{G}{1+GH} = \frac{(G_3 + G_4) G_5}{1 + (G_3 + G_4) G_5 H_3}$$

step 5. $\frac{G_1 G_2}{1 + G_2 G_2 H_1}$ and $\frac{(G_3 + G_4) G_5}{1 + (G_3 + G_4) G_5 H_3}$ are in series.



Step-6. Find Transfer function

$$\begin{aligned}
 \frac{C(s)}{R(s)} &= \frac{G}{1-GH} \\
 &= \frac{G_1 G_2}{1 + G_1 G_2 H_1} \cdot \frac{(G_3 + G_4) G_5}{1 + (G_3 + G_4) G_5 H_3} \\
 &= \frac{1 - G_1 G_2 (G_3 + G_4) G_5}{(1 + G_1 G_2 H_1) [1 + (G_3 + G_4) G_5 H_3]} \cdot \frac{H_2}{G_5} \\
 &= \frac{G_1 G_2 G_5 (G_3 + G_4)}{(1 + G_1 G_2 H_1) (1 + G_3 + G_4) G_5 H_3} - G_1 G_2 (G_3 + G_4) H_2
 \end{aligned}$$

*. Signal flow Graph from Block diagram:-

Method to obtain signal flow graph from the system equation.

Step-1.

Represent each variable by a separate note.

Step-2.

use the property that value of the variable represented by your note is an algebraic sum of all the signal enterigate that node to simulate the equation

Step-3.

Co-efficient of the variables in the equation are to be represented as the branch gain joining the node in signal flow graph.

Step-4.

Show the input and output variable separately to complete the signal flow graph.

Method to obtain signal flow graph from the given block diagram.

Step-1

Name all the summing point and take off point in the block diagram.

Step-2.

Represent each summing point and take off point by a separate node in signal flow graph (SFG).

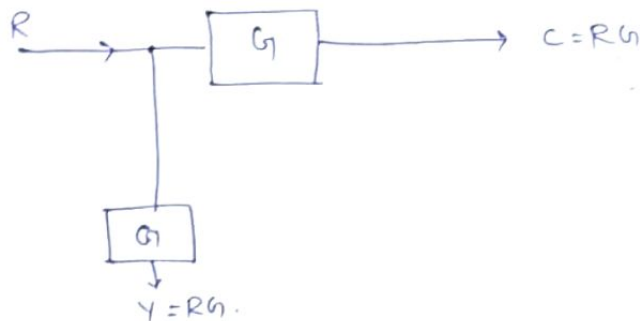
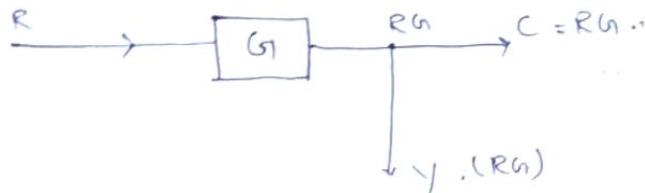
Step-3.

connect them by the branches instead of block indicating block transfer function as the gain of corresponding branches.

Step 4. show the I/p and o/p nodes separately if required to complete the signal flow graph.

- * shifting a take off point behind a block.

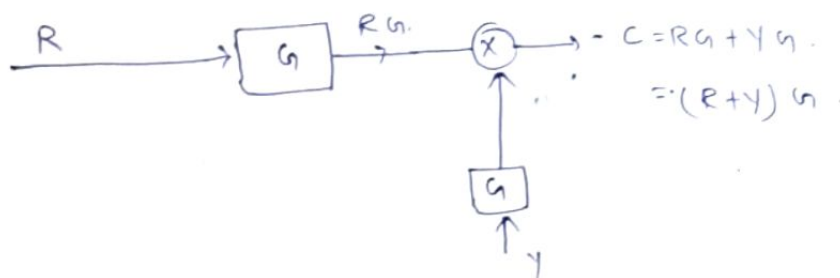
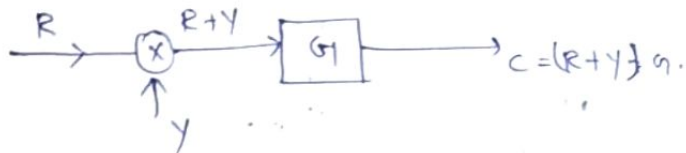
While shifting a take off point behind the Block. add a Block having transfer function same as that of the Block Behind which take off point is to be shifted in series with all the signals taking off from that point.



Q:- Determine the T.o.f. from the Block diagram shown.

- shifting a summing point Beyond the Block.

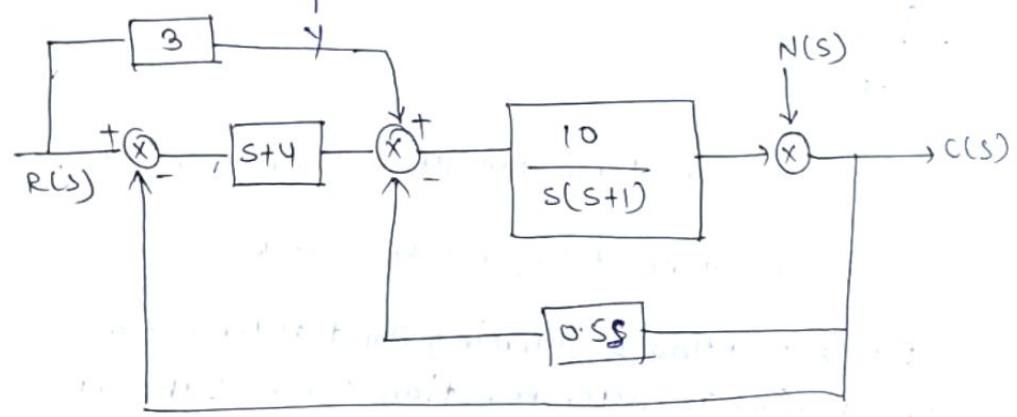
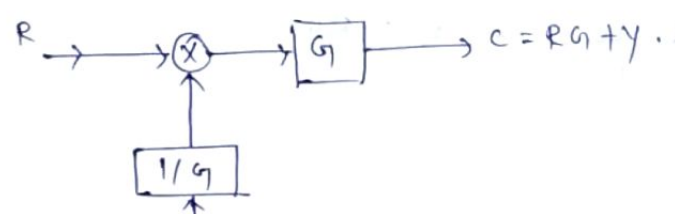
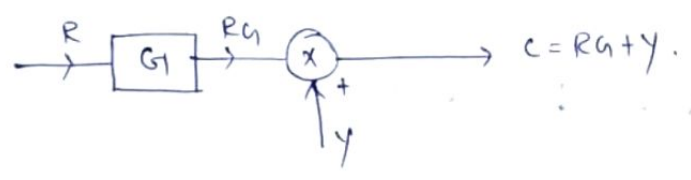
While shifting a summing point after a Block add a Block having Transfer function same as that of the Block after which summing point is to be shifted in series with all the signal at that summing point.



* shifting a summing point behind the block.

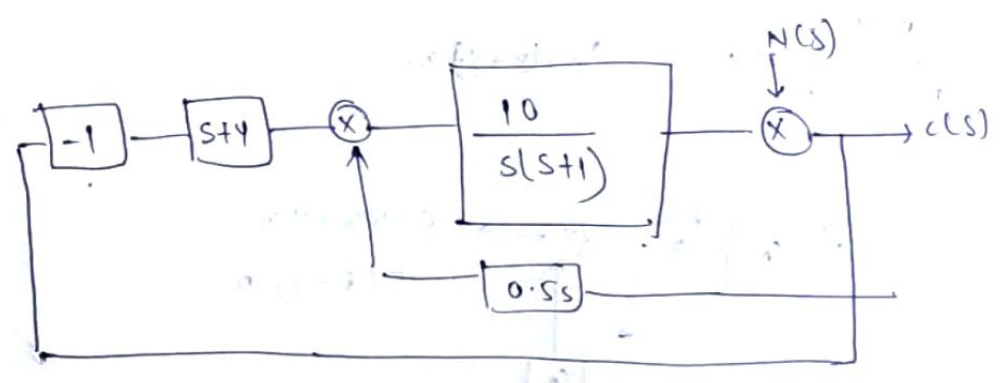
(39)

while shifting a summing point behind a block add a block having Transfer function $\frac{1}{G}$ as Reciprocal of the Tof of the block Before which summing point is to be shifted in series with all the signal at that summing point

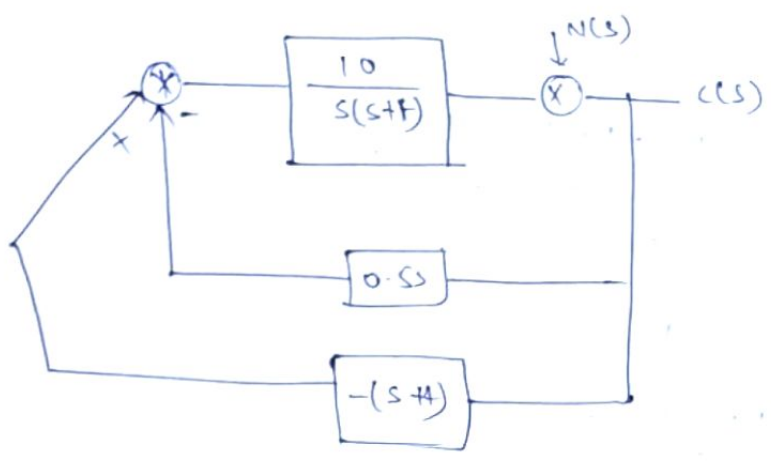


Find $\frac{C(s)}{N(s)}$ if $R(s) = 0$

When given $R(s) = 0$

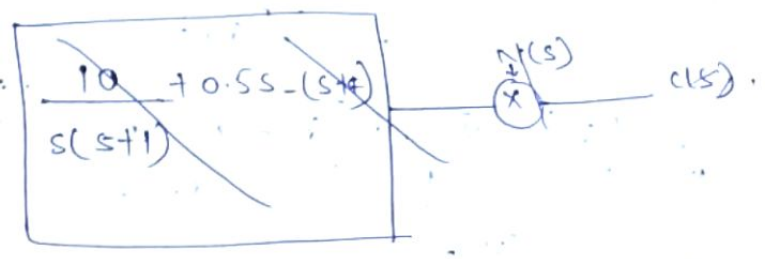


-1 and $s+4$ are cascade.
 $\therefore -(s+4)$.



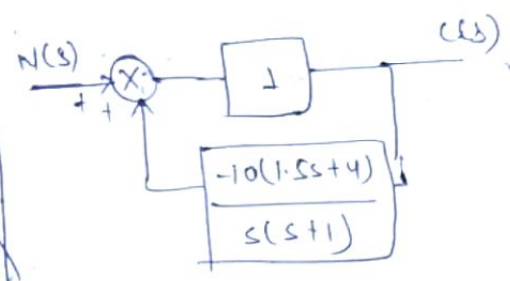
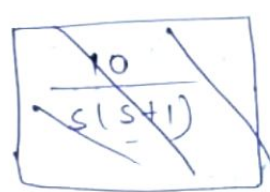
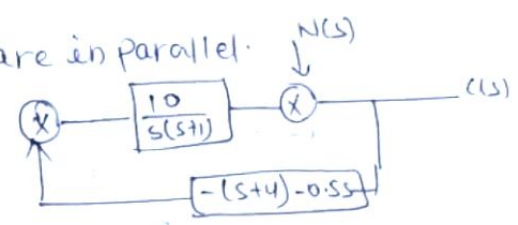
~~$\frac{10}{s(s+1)}$~~ $\rightarrow 0.5s - (s+4)$

$-(s+4) + 0.5s$
 $0.5s - s - 4$
 $-(0.5s + 4)$



$0.5s$ and $-(s+4)$ are in parallel.

$-0.5s - (s+4)$
 $-0.5s - s - 4$
 $-(1.5s + 4)$



$\frac{10}{s(s+1)}$ and $(-1.5s+4)$ are cascade.
 because summing point not existing.

then $\frac{-10(1.5s+4)}{s(s+1)}$

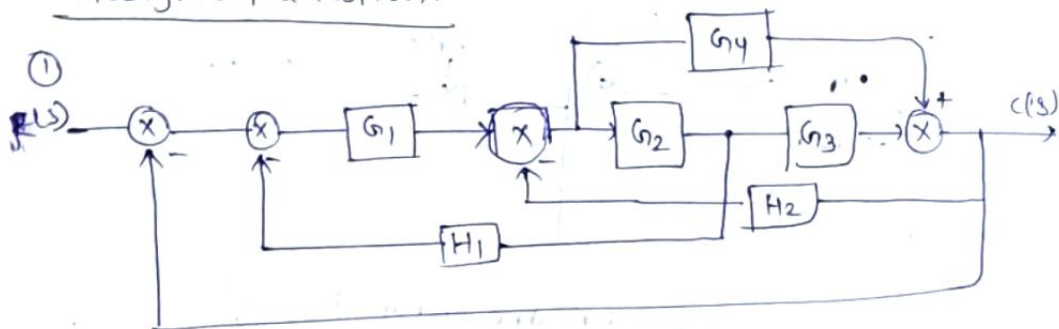
$$\frac{C(s)}{R(s)} = \frac{G}{1 - GH}$$

$$= \frac{1}{1 - 1 \cdot \left[\frac{-10(1.5s+4)}{s(s+1)} \right]}$$

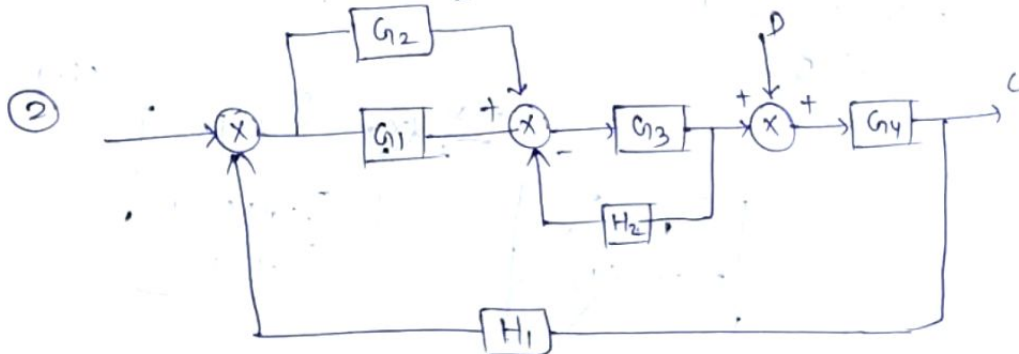
$$= \frac{1}{1 + \frac{10(1.5s+4)}{s(s+1)}}$$

$$= \frac{s(s+1)}{s(s+1) + 10(1.5s+4)}$$

Assignment Question.



determine $\frac{C(s)}{R(s)}$



determine $\frac{C}{R}$, $\frac{C}{D}$ and total output