## Write brief notes on ANY FOUR of the following:

- (i) State transition matrix
- (ii) Settling time
- (iii) Phase cross-over frequency
- (iv) State equation of discrete data systems
- (v) Integrating amplifiers
- (vi) Off-set nulling of integrating amplifiers

TOCHI-682 TOCHI-

B.Tech. Degree V Semester (Supplementary) Examination in Computer Science and Engineering

June 2002

## **CS 504 CONTROL SYSTEMS**

(1995 Admissions)

Time: 3 Hours

Maximum Marks: 100

(All questions carry <u>EQUAL</u> marks)

- I. (a) Distinguish between linear and nonlinear control systems.
  - (b) Define transfer function of a dynamic system. How is it related to its impulse response?
  - (c) Derive the transfer function  $\frac{X_2(s)}{F(s)}$  of the mechanical system shown in figure 1.

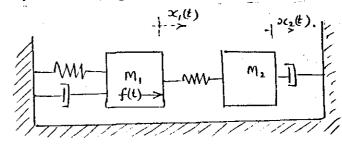


Fig. 1 OR

II. (a) For the sytem modelled by the third order differential equation

$$\frac{d^{3}c}{dt^{3}} + a_{2}\frac{d^{2}c}{dt^{2}} + a_{1}\frac{dc}{dt} + a_{0}c = b_{0}r(t),$$

derive the state variable representation.

(b) State and explain 'Final value theorem' and show how this is used to estimate the steady state error of a feed back system.

What are the drawbacks of this method?

III. (a) Corresponding to the locations of the characteristic-equationroots listed below, sketch the time domain responses.

(i) 
$$s = \sigma[\sigma > 0]$$

(ii) 
$$s = j\omega, j\omega, -j\omega, j\omega$$

(iii) 
$$s = -\sigma + j\omega, -\sigma + j\omega$$

$$\begin{bmatrix}
\sigma > 0 \\
|\sigma| << |\omega|
\end{bmatrix}$$

(b) A feed back system has forward transfer function  $G(s) = \frac{1}{s^3 + 4s^2 + 13s + 36}$  and feed back transfer function

 $H(s) = \frac{k}{s}$ . Use Routh Harvitz' criterion to find the value of k that gives undamped oscillations in the response. What is the frequency of oscillations?

- (c) Explain Liapunov's stability criterion applied to linear systems.

  OR
- (a) Draw the Bode-plot of the system having loop-transferfunction  $G(s)H(s) = \frac{K}{s(1+0.02s)(1+0.05s)}$  for K=80. What value of K will make the system marginally stable?
- (b) A certain control system has coefficient matrix A given by

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix}$$

Obtain the eigen values.

V (a) State and explain Shannon's sampling theorem.

(b) Find Z-transform of the sequences given below

(i) 
$$f(k) = 1,1,1,...$$
 for  $k = 0,1,2,...$ 

(ii) 
$$f(k) = \begin{cases} 1 & \text{for } k = 0, 2, 4, 6, \dots \\ -1 & \text{for } k = 1, 3, 5, 7, \dots \end{cases}$$

VL (a) Solve the difference equation given below using Z-transform:

$$x(k+2)-x(k+1)+0.1x(k) = U_s(k)$$
  
 $x(0) = 0$   
 $x(1) = 0$ 

where  $U_{\epsilon}(k)$  denotes the sampled version of unit step.

(b) Using Jury's test find whether the system characterised by  $z^3 + z^2 + 3z + 0.2 = 0$  is stable or not.

VII. (a) Explain how an OP-AMP is used as a finite gain amplifier.

- (b) How is multiplication of a time function by a constant such as 3.52 carried out in a analog computer.
- (c) Draw and explain the analog computer patch board diagram for generating the function

$$y(t) = 2\cos\left(2t + 60^{\circ}\right)$$

OR

VIII. (a) Citing examples explain the necessity of -

- (i) time-scaling, and
- (ii) amplitude scaling.
- (b) Draw and explain the patch board diagram for simulating the transfer function,

$$G(s) = \frac{10}{s^2 + 7s + 10}$$

in the analog computer.