

BCA 2nd SEMESTER EXAM., 2015

MATHEMATICS CODE- 303202

Time: 3 hours

Full Marks: 60

Instructions:

- i. The Marks are indicated in the right -hand margin.
- ii. There are **SEVEN** questions in this paper.
- iii. Attempts **FIVE** question in all.
- iv. Question Nos. **1** and **2** are compulsory.

1. Choose the correct option (any six).

2*6=12

(a) The rounded value of 57.275 to two decimal place is

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|-------------|------------------------|
| (I) 57.27 | (II) 5' |
| (III) 57.26 | (IV) None of the above |

(b) A non-zero polynomial $f(x)$ of degree 3 has roots at $x = 1$, $x = 2$ and $x = 3$.

Which of the following is true?

- | | |
|-------------------------|------------------------|
| (I) $f(0) + f(4) < 0$ | (II) $f(0)f(4) > 0$ |
| (III) $f(0) + f(4) > 0$ | (IV) None of the above |

(c) The function $f(x) = 1 + \cos x - 5x^2$ is an example of

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|-------------------------|------------------------|
| (I) Polynomial | (II) Transcendental |
| (III) Both (I) and (II) | (IV) None of the above |

(d) Newton-Raphson method is based on Taylor's series but

- (I) neglecting 3rd and heigher order derivatives
- (II) accepting up to 3rd order derivatives
- (III) accepting up to 4th order derivatives
- (IV) neglecting 2nd order and higher order derivatives

(e) If y_0, y_1, \dots, y_n denote a set of values of y , then Δy_0 is

- | | |
|--------------------|------------------------|
| (I) $(E + 1)y_0$ | (II) $E y_0$ |
| (III) $(E - 1)y_0$ | (IV) none of the above |

(f) Simpson's $\frac{1}{3}rd$ rule requires the division of the entire into

- (I) odd number of sub-intervals of equal length
- (II) even number if sub-intervals of equal length

- (III) odd or even numbers of sub-intervals of equal length
 (IV) None of the above
- (g) Back-substitution is used in
 (I) Jacobi method (II) Gauss elimination method
 (III) Gauss-Jordan method (IV) none of the above
- (h) Convergence in the Gauss-Seidel method is _____ as fast as Gauss-Jacobi method
 (I) same (II) twice
 (III) thrice (IV) None of the above
- (i) Lagrange polynomial of degree two passes
 (I) one point (II) two points
 (III) three points (IV) none of the above
- (j) Error in Simpson's $\frac{3}{8}$ rd rule is _____ compare to Simpson's $\frac{1}{3}$ rd rule.
 (I) small (II) negligible
 (III) zero (IV) large

2. Answer any three of the following:

4*3=12

- (a) State the principle used in Gauss-elimination method.
- (b) Solve $x + 2y = 5$
 $2x + y = 4$
 using Gauss-Jordan method.
- (c) State Newton's algorithms for finding square root of N .
- (d) If the matrix A is such that $A = \begin{pmatrix} 2 \\ -4 \\ 7 \end{pmatrix} \begin{pmatrix} 1 & 9 & 5 \end{pmatrix}$
 then find $\det(A)$.
- (e) Find $\Delta \sin x$.

Answer any three of the following:

12*3=36

3. Find the missing term of the table given below :

X :	1	2	3	4	5	6	7
Y :	2	4	8	--	32	64	128

4. The velocity V km/min of a motorbike that starts from rest is given below :

t :	2	4	6	8	10	12	14	16	18	20
V :	10	18	25	29	32	20	11	5	2	0

Find the approximate distance covered in twenty minutes using Simpson's $\frac{1}{3}$ rd rule.

5. Use Jacobi method to find the solution of the following set of linear equations :

$$5x_1 - 2x_2 + 3x_3 = -1$$

$$-3x_1 + 9x_2 + x_3 = 2$$

$$2x_1 - x_2 - 7x_3 = 3$$

6. Find $\Delta^n (e^{ax+b})$.

7. Describe Lagrange's interpolation formula. Consider the following X_i 's :

$$i \quad : \quad 0 \quad 1 \quad 2$$

$$X_i \quad : \quad 1 \quad 3 \quad -2$$

Find $L_0(x)$, $L_1(x)$ and $L_2(x)$

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