# CIA III ANSWER KEY CFD

# ANSWER KEY 2 MARKS

1. What is finite volume methods?

A : Finite Volume Methods (FVM) are numerical techniques used in computational fluid dynamics (CFD) and other areas of scientific computing to solve partial differential equations that describe physical phenomena like fluid flow, heat transfer, and more. FVM is particularly popular in the simulation of fluid flow in various engineering and scientific applications.

# 2. Why pressure gradient is measured?

A: Pressure gradient is measured in various fields and applications for several reasons, depending on the specific context. The measurement of pressure gradient provides valuable information about fluid flow, material properties, and system performance.

### 3. Define flow field analysis.

A: Flow field analysis is a branch of fluid mechanics and computational fluid dynamics (CFD) that focuses on the study and characterization of the velocity, pressure, temperature, and other properties of a fluid within a defined region or space. It involves the examination of how a fluid, which can be a gas or liquid, behaves and interacts within a given environment, such as a pipe, channel, or around an object.

### 4. What is the term staggered grid?

A: A staggered grid, in the context of numerical methods for solving partial differential equations, particularly in computational fluid dynamics (CFD) and computational electromagnetics, is a discretization scheme used to approximate the solution of a physical problem. Staggered grids are often employed to solve equations such as the Navier-Stokes equations for fluid flow or Maxwell's equations for electromagnetics.

# 5. What are all the properties of turbulence model?

A: Turbulence models are mathematical representations used in computational fluid dynamics (CFD) to describe and predict the behavior of turbulence in fluid flow. Turbulence models aim to provide a simplified yet accurate representation of the complex, three-dimensional, and time-dependent nature of turbulent flows. These models typically characterize various properties and characteristics of turbulence.

# 6. What is the mixing length?

A: The mixing length is a concept in fluid dynamics and turbulence modeling that is commonly associated with the mixing length theory, which was developed to describe turbulent flow in boundary layers. The mixing length is used to estimate the average distance that fluid parcels travel before they mix with the surrounding fluid in a turbulent flow. This concept is particularly relevant in the context of boundary layer flows, which occur near solid surfaces and are characterized by the presence of turbulence.

# 7. Define Adaptive mesh.

A: An adaptive mesh, often referred to as an adaptive grid or mesh refinement, is a computational grid or mesh that changes its resolution or structure dynamically during a simulation or numerical calculation. The purpose of adaptive meshes is to enhance the accuracy and efficiency of simulations by concentrating computational resources in regions where they are needed most and reducing grid density where it is not necessary.

# 16 MARKS

8.a) Summarize in detail about the pressure and velocity corrections.

<u>A:</u> Pressure-velocity corrections are a fundamental aspect of the pressure-velocity coupling in the numerical simulation of incompressible fluid flows, such as those solved using the Navier-Stokes equations in the context of computational fluid dynamics (CFD). The process involves an iterative algorithm that ensures that the velocity field and pressure field are self-consistent and satisfy the fundamental continuity equation. Below is a detailed summary of the pressure-velocity correction procedure in CFD:

# 1. \*\*Initial Guess\*\*:

- The process begins with an initial guess for the velocity field within the computational domain. This initial guess could be based on boundary conditions or a previous time step's velocity field.

# 2. \*\*Momentum Prediction\*\*:

- A preliminary calculation, known as the "momentum prediction" or "velocity prediction," is performed using the guessed velocity field. This step estimates the velocities in the next time step or iteration without considering pressure effects. It's based on the momentum equations.

# 3. \*\*Pressure Correction\*\*:

- A key aspect of the pressure-velocity correction is to correct the pressure field. This is done through the solution of the Poisson equation for pressure (or a variant of it) based on the velocity divergence, which represents the local violation of mass conservation.

- The Poisson equation typically takes the form  $\nabla^2 p' = \nabla \cdot (\rho \nabla \cdot u')$ , where p' is the pressure correction,  $\rho$  is the fluid density, u' is the velocity correction, and  $\nabla$  represents the gradient operator.

- Solving this equation provides the pressure correction field p', which ensures that the divergence of the corrected velocity field  $\nabla (u + u')$  is zero.

# 4. \*\*Velocity Correction\*\*:

- After obtaining the pressure correction, the velocity correction u' is computed using  $\nabla u' = -\nabla p'$ , where  $\nabla u'$  represents the gradient of the velocity correction field.

- This velocity correction adjusts the preliminary velocity prediction, ensuring that the corrected velocity field satisfies the continuity equation ( $\nabla \cdot u = 0$ ), which represents mass conservation.

# 5. \*\*Pressure and Velocity Update\*\*:

- The final pressure and velocity fields are updated by adding the respective corrections to the initial guess:  $p_new = p_old + p'$  and  $u_new = u_old + u'$ .

# 6. \*\*Convergence Check\*\*:

- The pressure-velocity correction process is typically performed iteratively until a convergence criterion is met. This criterion is often based on the change in pressure and velocity fields between successive iterations. When the solution reaches a steady state, the process stops.

# 7. \*\*Boundary Conditions and Source Terms\*\*:

- Throughout this process, boundary conditions and source terms (e.g., external forces, heat sources) are considered as appropriate.

The pressure-velocity correction method, often referred to as the SIMPLE (Semi-Implicit Method for Pressure-Linked Equations) or SIMPLER (SIMPLE Revised) algorithm, is widely used in CFD to solve incompressible flows. It ensures that the velocity and pressure fields satisfy the governing equations, particularly the continuity equation, and is essential for maintaining numerical stability and accuracy in simulating fluid flows.

#### b. Explain about the SIMPLE Algorithm in detail.

A: The SIMPLE algorithm (Semi-Implicit Method for Pressure-Linked Equations) is a widely used computational technique in the field of computational fluid dynamics (CFD) for solving the Navier-Stokes equations, particularly for simulating incompressible fluid flows. It is an iterative method that ensures the pressure-velocity coupling in a manner that conserves mass and maintains stability in the numerical simulation. Here is a detailed explanation of the SIMPLE algorithm:

# \*\*1. Problem Setup:\*\*

- Begin with a description of the geometry, boundary conditions, initial conditions, and governing equations, which are typically the incompressible Navier-Stokes equations. These equations describe the conservation of mass and momentum in fluid flow.

# \*\*2. Discretization:\*\*

- Discretize the governing equations on a computational grid. This involves dividing the domain into grid cells and approximating the derivatives in the equations using numerical methods such as finite differences or finite volumes.

# \*\*3. Initial Guess:\*\*

- Provide an initial guess for the velocity and pressure fields within the domain. This initial guess could be based on the boundary conditions, previous time steps, or another reasonable estimate.

# \*\*4. Pressure-Velocity Coupling:\*\*

- The heart of the SIMPLE algorithm lies in the pressure-velocity coupling process. It consists of the following steps, which are typically performed iteratively:

# \*\*a. Momentum Prediction:\*\*

- Compute a preliminary velocity field based on the initial guess. This step is often referred to as the momentum prediction or velocity prediction step. It uses the discretized momentum equations but does not consider the pressure effects.

\*\*b. Pressure Correction:\*\*

- Solve the Poisson equation for pressure correction ( $\Delta p'$ ) using the corrected velocities. The Poisson equation typically takes the form:

 $\nabla^2 p' = \nabla \cdot (\rho \nabla \cdot u')$ 

where p' is the pressure correction,  $\rho$  is the fluid density, u' is the velocity correction, and  $\nabla$  represents the gradient operator.

# \*\*c. Velocity Correction:\*\*

- Compute the velocity correction field u' based on the pressure correction using the relationship:

 $\nabla u' = -\nabla p'$ 

\*\*d. Pressure and Velocity Update:\*\*

- Update the pressure and velocity fields by adding the respective corrections to the initial guess. The updated fields are:

 $p_new = p_old + p'$  $u_new = u_old + u'$ 

\*\*e. Continuity Check:\*\*

- Verify that the continuity equation ( $\nabla \cdot u = 0$ ) is satisfied with the updated velocity field.

\*\*f. Convergence Check:\*\*

- Check for convergence by evaluating criteria, such as the change in pressure or velocity fields between successive iterations. If the criteria are met, the algorithm terminates.

### \*\*g. Iteration:\*\*

- If convergence criteria are not met, continue iterating between the pressure correction and velocity correction steps until convergence is achieved.

# \*\*5. Output and Post-Processing:\*\*

- Once the algorithm converges, analyze and post-process the results, such as calculating flow parameters, visualizing flow patterns, or extracting specific data of interest.

The SIMPLE algorithm is known for its ability to handle incompressible flows and ensure pressurevelocity coupling in a stable and accurate manner. It is the foundation of many CFD codes and has been extended and adapted in various forms, including the SIMPLEC, SIMPLER, and PISO (Pressure-Implicit with Splitting of Operators) algorithms, to address specific needs and improve computational efficiency in different flow scenarios.

### 9. a) Explain in detail about the grid generation.

A: Grid generation, also known as mesh generation, is a critical step in numerical simulations, particularly in computational fluid dynamics (CFD), finite element analysis (FEA), and other computational methods. The grid, or mesh, divides the computational domain into discrete elements, such as cells or elements, to facilitate the numerical solution of partial differential equations. Here's a detailed explanation of the grid generation process:

### \*\*1. Problem Definition:\*\*

- The grid generation process starts with a clear understanding of the physical problem to be solved. This includes defining the geometry of the domain, specifying boundary conditions, and selecting the appropriate mathematical model (e.g., Navier-Stokes equations for fluid flow, heat conduction equation for heat transfer, etc.).

### \*\*2. Domain Discretization:\*\*

- The computational domain is divided into discrete elements or cells. The choice of grid type and structure depends on the nature of the problem and the available numerical method. Grids can be structured or unstructured.

- Structured grids: These are regular grids with a well-defined pattern, such as Cartesian grids in 2D or 3D. They are suitable for simple geometries and can be efficient for certain types of problems.

- Unstructured grids: These are more flexible and adaptive, allowing for mesh refinement in regions of interest or complex geometries. Unstructured grids often use triangles, quadrilaterals, tetrahedra, or hexahedra as elements.

\*\*3. Grid Generation Methods:\*\*

- Grids can be generated using various methods, including:

# \*\*a. Algebraic Methods:\*\*

- Algebraic methods use mathematical equations to define grid points. They are often used for simple geometries and structured grids, like the transfinite interpolation method.

# \*\*b. Elliptic Methods:\*\*

- Elliptic methods involve solving elliptic partial differential equations to generate grids. The Laplace equation is a common choice for this purpose.

# \*\*c. Sweeping Methods:\*\*

- Sweeping methods involve "sweeping" through the domain to create grids. These methods are particularly useful for structured grids.

# \*\*d. Unstructured Grid Generation:\*\*

- Unstructured grids are often generated using techniques like Delaunay triangulation or advancing front methods, which adapt to the geometry.

### \*\*e. Hybrid Methods:\*\*

- Hybrid methods combine various techniques to take advantage of both structured and unstructured grid generation. They are used in complex problems with irregular geometries.

### \*\*4. Grid Quality and Metrics:\*\*

- Grid quality is crucial for numerical accuracy and convergence. Grid quality metrics, such as cell aspect ratio, skewness, and orthogonality, are used to assess the quality of the generated grid. Grid optimization techniques can be applied to improve quality.

# \*\*5. Boundary Conditions:\*\*

- Grid generation must account for boundary conditions. Grid points near boundaries need to align with the specified boundary conditions, whether they are no-slip walls, inflow/outflow boundaries, or other types.

#### \*\*6. Grid Refinement:\*\*

- Grid refinement is the process of increasing the resolution in specific regions to capture fine details or gradients in the solution. Adaptive mesh refinement is a technique where grid cells are refined based on the local solution behavior.

### \*\*7. Grid Connectivity:\*\*

- Proper connectivity between grid cells is essential for numerical solution techniques. Grid generation must ensure that cells share common faces or edges, and that information is accurately passed between neighboring cells.

### \*\*8. Grid Export:\*\*

- Once the grid is generated, it is typically exported in a format compatible with the chosen simulation software. Common formats include STL (Stereolithography), unstructured mesh formats like .msh, and structured formats like HDF5 or VTK.

#### \*\*9. Grid Validation:\*\*

- Before running simulations, the generated grid should undergo validation to check for any errors or inconsistencies. This includes checking for grid quality, cell aspect ratios, and compatibility with the chosen numerical method.

Grid generation is a crucial step in the numerical simulation process, as the quality of the grid can significantly impact the accuracy and efficiency of the simulation. It often requires careful consideration of the problem's complexity, boundary conditions, and solution requirements. Grid generation software and tools have been developed to automate and facilitate this process for various applications.

# 9} B. Illustrate the turbulence model equation in detail.

Turbulence models are used in computational fluid dynamics (CFD) to describe and simulate turbulent flow, which is characterized by chaotic and unsteady fluid motion. Different turbulence models make various approximations and assumptions to simplify the Navier-Stokes equations and other transport equations. Here, I'll illustrate one of the most widely used turbulence models, the Reynolds-Averaged Navier-Stokes (RANS) equations, which includes the k- $\epsilon$  turbulence model in detail:

# \*\*1. RANS Equations:\*\*

- The Reynolds-Averaged Navier-Stokes (RANS) equations are derived from the Navier-Stokes equations but include the concept of Reynolds averaging to separate the flow variables into mean and fluctuating components.

- The RANS equations consist of the following equations for the three velocity components (u, v, w), pressure (p), and the turbulence variables (k and  $\epsilon$ ):

\*\*a. Continuity Equation:\*\*

-  $\nabla \cdot \mathbf{u} = 0$  (for incompressible flow).

\*\*b. Momentum Equations:\*\*

- These equations describe the mean velocity field (U):

- Here, \(U\) represents the mean velocity, \(P\) is the mean pressure, \(Re\) is the Reynolds number, \(u'\_i\) and \(u'\_j\) are the fluctuating velocity components, \(vt\) is the turbulent eddy viscosity, and the right-hand side terms represent pressure gradients, viscous effects, and Reynolds stresses.

\*\*c. Turbulence Variables (k-ε Model):\*\*

- The k- $\epsilon$  turbulence model is based on two additional transport equations for turbulence variables, kinetic energy (k) and turbulence dissipation rate ( $\epsilon$ ):

\*\*Turbulent Kinetic Energy Equation (k):\*\*

 $(\frac{\partial k}{\partial t} + U \cdot \nabla k = \nabla \cdot (v t \nabla k) + Pk - \varepsilon)$ 

- In this equation, (Pk) represents the production of turbulent kinetic energy, and  $(\epsilon)$  represents the dissipation rate of turbulence kinetic energy.

\*\*Turbulence Dissipation Rate Equation (ε):\*\*

 $(\frac{\partial \epsilon}{\partial t} + U \cdot \nabla \epsilon = \nabla \cdot (v t \nabla \epsilon) + C \epsilon \frac{k}{Pk} - C \epsilon 2 \epsilon^2)$ 

- In this equation,  $(C\epsilon 1)$  and  $(C\epsilon 2)$  are model constants, and the terms  $(C\epsilon 1\epsilon/kPk)$  and  $(C\epsilon 2\epsilon^2)$  account for turbulent energy dissipation.

#### \*\*2. Closure Models:\*\*

- The k- $\epsilon$  turbulence model requires additional closure models to calculate turbulence production, dissipation, and the turbulent eddy viscosity (\(vt\)) based on the modeled turbulence variables. Closure models are empirical relationships or equations that involve turbulence properties and model constants.

- For example, the production of turbulent kinetic energy (\(Pk\)) is often estimated using the gradient of mean velocity and Reynolds stresses:

 $(Pk = -u'_i u'_j frac{\partial U_i}{\partial x_j})$ 

\*\*3. Boundary Conditions:\*\*

- Proper boundary conditions for velocity, pressure, and turbulence variables are essential in the RANS equations. These conditions depend on the specific flow problem and are often set based on physical insights or experimental data.

# \*\*4. Solution Process:\*\*

- The RANS equations, along with turbulence models and closure models, are solved using numerical methods such as finite volume or finite element techniques. The solution process involves iterative steps until convergence is achieved.

The k-ɛ turbulence model is widely used for simulating turbulent flows in engineering applications due to its computational efficiency and reasonable accuracy for many scenarios. However, it's important to note that there are more advanced turbulence models (such as Large Eddy Simulation and Reynolds Stress Models) that provide improved accuracy in simulating complex turbulence phenomena but may be computationally more demanding. The choice of turbulence model depends on the specific flow problem and the available computational resources.

10. a. Explain in detail about the mesh refinement.

Mesh refinement is a technique used in numerical simulations, particularly in computational fluid dynamics (CFD), finite element analysis (FEA), and other computational methods, to increase the resolution in specific regions of the computational domain. The primary goal of mesh refinement is to capture fine details, gradients, or important flow features, thus improving the accuracy of the simulation. Here's a detailed explanation of mesh refinement:

### \*\*1. Motivation for Mesh Refinement:\*\*

- Mesh refinement is employed when the problem being solved requires a more accurate representation of the solution in certain regions of the domain. This may be due to steep gradients, flow separations, shock waves, or other flow features that cannot be adequately resolved with a coarse mesh.

### \*\*2. Types of Mesh Refinement:\*\*

- There are several ways to perform mesh refinement:

### \*\*a. H-Refinement (Hierarchical Refinement):\*\*

- H-refinement involves subdividing coarser mesh cells into smaller ones. It is a common technique when more details are needed in specific areas.

\*\*b. P-Refinement (Polynomial Refinement):\*\*

- In the context of the finite element method, P-refinement involves increasing the polynomial degree of the basis functions within elements. Higher-degree polynomials provide better representation of the solution.

\*\*c. Adaptive Mesh Refinement:\*\*

- Adaptive mesh refinement (AMR) is a dynamic approach that selectively refines grid cells based on local solution characteristics. It is particularly useful when you need high resolution only in specific regions and want to save computational resources elsewhere.

# \*\*d. Local Refinement:\*\*

- Local refinement targets specific regions where high resolution is required. It is a controlled way to focus computational effort where it's needed most.

#### \*\*3. Steps in Mesh Refinement:\*\*

- The process of mesh refinement involves several steps:

#### \*\*a. Error Estimation:\*\*

- Error estimation techniques assess the accuracy of the current solution. They identify areas with high errors, where refinement is needed. Common methods include Richardson extrapolation, residual-based error estimation, and gradient-based error estimation.

# \*\*b. Grid Adaptation:\*\*

- Based on error estimates, grid adaptation algorithms decide where to refine the mesh. This could involve splitting cells, adding new nodes, or increasing the order of basis functions.

#### \*\*c. Grid Connectivity:\*\*

- Ensuring proper connectivity between refined and unrefined cells is crucial to maintain a continuous grid. This involves updating neighbors, edges, and nodes to maintain grid consistency.

# \*\*d. Boundary Conditions:\*\*

- Boundary conditions must be appropriately modified to account for the refined mesh, ensuring that they remain consistent with the new mesh topology.

#### \*\*e. Solver Updates:\*\*

- The simulation solver may need updates to incorporate the refined mesh. This includes reassembly of stiffness matrices, interpolation of variables, and solution of the updated equations.

# \*\*f. Iterative Process:\*\*

- Mesh refinement is often an iterative process. After refinement, the simulation solver is typically run again to reach convergence. This may require several iterations.

# \*\*4. Validation:\*\*

- Refined grids must undergo validation to verify that the results are consistent with the physics of the problem and the expected behavior. Validation often involves comparing simulation results to experimental data or analytical solutions.

### \*\*5. Trade-offs:\*\*

- Mesh refinement can significantly increase computational demands, as it leads to more grid cells, equations, and computational effort. Care must be taken to strike a balance between computational cost and improved accuracy.

Mesh refinement is a powerful tool for obtaining accurate and detailed results in numerical simulations. However, it should be used judiciously, as excessive refinement can lead to increased computational resources and longer simulation times. Properly applied, mesh refinement can be essential for solving complex problems in engineering and science.

10. b. Explain about the software tools used in CFD.

A: Computational Fluid Dynamics (CFD) is a multidisciplinary field that involves the simulation and analysis of fluid flows and heat transfer phenomena using numerical methods. To perform CFD simulations effectively, various software tools and packages are available, each with its unique features and capabilities. Here, I'll explain some of the software tools commonly used in CFD:

# 1. \*\*ANSYS Fluent:\*\*

- ANSYS Fluent is one of the most widely used commercial CFD software packages. It offers a broad range of capabilities for simulating fluid flow, heat transfer, turbulence, and multiphase flows. ANSYS Fluent is known for its user-friendly interface and extensive post-processing capabilities.

# 2. \*\*OpenFOAM:\*\*

- OpenFOAM is an open-source CFD software suite that provides a comprehensive range of solvers and utilities for simulating a variety of flow problems. It is highly customizable, allowing users to create and modify their own solvers and models.

#### 3. \*\*COMSOL Multiphysics:\*\*

- COMSOL Multiphysics is a versatile software package that allows for multiphysics simulations, including CFD. It provides a user-friendly interface and features a wide range of physics modules for modeling fluid dynamics, heat transfer, and structural mechanics, among others.

# 4. \*\*CFD++:\*\*

- CFD++ is a CFD software package known for its high parallel performance and scalability. It offers various solvers for compressible and incompressible flows, turbulence, and reacting flows.

# 5. \*\*STAR-CCM+ (by Siemens Simcenter):\*\*

- STAR-CCM+ is a widely used commercial CFD software that excels in providing comprehensive solutions for complex multiphysics simulations. It offers a user-friendly interface, automated meshing tools, and excellent post-processing capabilities.

# 6. \*\*FIoEFD (by Mentor Graphics):\*\*

- FloEFD is a CFD software that integrates with popular CAD packages like SolidWorks, PTC Creo, and Siemens NX. It allows for concurrent CFD analysis during the design phase, making it particularly useful for design engineers.

### 7. \*\*NUMECA:\*\*

- NUMECA provides CFD software solutions for aero- and hydrodynamics applications. Its products are known for their accuracy, high-order meshing techniques, and advanced optimization capabilities.

### 8. \*\*Exa PowerFLOW:\*\*

- Exa PowerFLOW is a CFD software suite focused on high-fidelity simulations for automotive, aerospace, and other engineering applications. It is known for its robust Lattice Boltzmann-based solver and powerful post-processing.

#### 9. \*\*LAMMPS:\*\*

- While primarily used for molecular dynamics simulations, LAMMPS (Large-scale Atomic/ Molecular Massively Parallel Simulator) is a versatile tool that can be adapted for some types of fluid flow simulations, particularly at the molecular level.

#### 10. \*\*SU2:\*\*

- SU2 is an open-source CFD code that is gaining popularity. It provides a wide range of solvers for various types of flows, including compressible and incompressible, inviscid and viscous, and more.

### 11. \*\*SimScale:\*\*

- SimScale is a cloud-based simulation platform that allows users to perform CFD simulations via a web browser. It offers a user-friendly interface and is accessible for small companies, students, and hobbyists.

### 12. \*\*Gerris Flow Solver:\*\*

- Gerris is an open-source CFD software designed for solving free-surface flow problems. It is useful for simulating complex fluid-structure interactions and multiphase flows.

Each of these software tools has its own strengths, capabilities, and target applications. The choice of CFD software depends on factors like the specific problem to be solved, available computational resources, budget constraints, and user familiarity with the software.