## Code No: 09A1BS04

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY, HYDERABAD

## B. Tech I Year Examinations, May/June-2013 <br> MATHEMATICAL METHODS

(Common to EEE, ECE, CSE, EIE, BME, IT, ETM, ECM, ICE)
Time: 3 hours
Max. Marks: 75

## Answer any five questions

## All questions carry equal marks

1.a) Find the value of k such that the rank of A is 2 , where $\mathrm{A}=\left[\begin{array}{cccc}1 & 1 & -1 & 1 \\ 1 & -1 & k & -1 \\ 3 & 1 & 0 & 1\end{array}\right]$
b) Solve the system of linear equations by matrix method.

$$
x+y+z=6,2 x+3 y-2 z=2,5 x+y+2 z=13
$$

2. Verify Cayley Hamilton theorem and find the inverse of the matrix

$$
\left[\begin{array}{rrr}
7 & -1 & 3 \\
6 & 1 & 4 \\
2 & 4 & 8
\end{array}\right]
$$

3. Reduce the following quadratic form to canonical form. Find the matrix of the transformation.

$$
6 x^{2}+3 y^{2}+3 z^{2}-4 x y-2 y z+4 x z
$$

4.a) Find a real root of the equation $x \log _{10} x-1.2=0$ using Regula Falsi method.
b) Find the interpolation polynomial for $\mathrm{x}=2.4,3.2,4.0,4.8,5.6$ and $\mathrm{f}(\mathrm{x})=22,17.8$, 14.2, 38.3, 51.7 using Newton's forward interpolation formula.
5.a) Fit a parabola of the form $y=a x^{2}+b x+c$ for the data

| $x$ | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 1090 | 1220 | 1390 | 1625 | 1915 |

b) Evaluate $\int_{0}^{\pi} \sin x d x$ by dividing the range into 10 equal parts using
i) Trapezoidal rule,
ii) Simpson's $1 / 3$ rd rule.
6. Find $\mathrm{y}(0.8)$ using Adam's Predictor corrector method by finding the previous values using Euler's modified method, given that $\frac{d y}{d x}=y-x^{2}, y(0)=1$.
7.a) Obtain the Fourier series for the function $\mathrm{f}(\mathrm{x})=\mathrm{x} \operatorname{Sin} \mathrm{x}$ in $[0,2 \pi]$
b) Find the half range cosine series for $\mathrm{f}(\mathrm{x})=\mathrm{x}(2-\mathrm{x})$ in $0<x<2$.
8.a) Solve the partial differential equation ( $x-y$ ) $p+(y-x-z) q=z$.
b) Find $z^{-1}\left[\frac{z^{2}-z}{(z-2)(z-3)}\right]$.

