

FACULTY OF INFORMATICS

B.E. 3/4 (IT) I-Semester (Supplementary) Examination, June/July 2011

THEORY OF AUTOMATA

Time : Three Hours]

[Maximum Marks : 75

Answer ALL questions from Part-A.  
Answer any FIVE questions from Part-B.

PART—A (Marks : 25)

1. Distinguish between DFA and NFA. 3
2. Define regular expression and give two examples. 3
3. Define Epsilon-closure of a state. 2
4. What is Chomsky normal form ? Give one example. 3
5. State the pumping lemma for content free languages. 3
6. Define push down Automata. 2
7. List various types of Turing machine. 2
8. What is linear bounded automata ? 2
9. Define LR(K) grammars. 2
10. What is post corresponds problem ? Give one example. 3

PART—B (Marks : 5×10=50)

11. (a) Construct a DFA equivalent to the following NFA :

$$M = (\{q_0, q_1, q_2, q_3\}, \{0, 1\}, \delta, q_0, \{q_3\})$$

where  $\delta$  is given by :

	a	b
q <sub>0</sub>	[q <sub>0</sub> q <sub>1</sub> ]	q <sub>0</sub>
q <sub>1</sub>	q <sub>2</sub>	q <sub>1</sub>
q <sub>2</sub>	q <sub>3</sub>	q <sub>3</sub>
q <sub>3</sub>	—	q <sub>2</sub>

- (b) Construct an  $\epsilon$ -NFA for the regular expression

$$01^* + 1.$$

12. Find the minimum state automata for the following DFA :—

10

	a	b
→ q <sub>0</sub>	q <sub>1</sub>	q <sub>3</sub>
q <sub>1</sub>	q <sub>2</sub>	q <sub>4</sub>
q <sub>2</sub>	q <sub>1</sub>	q <sub>4</sub>
q <sub>3</sub>	q <sub>2</sub>	q <sub>4</sub>
* q <sub>4</sub>	q <sub>4</sub>	q <sub>4</sub>

13. (a) Show that the following grammar is ambiguous :—

$$S \rightarrow aSb \mid SS \mid \epsilon.$$

5

(b) Construct a PDA equivalent to the following grammar :—

$$S \rightarrow AA/a$$

$$A \rightarrow SA/b.$$

5

14. Convert the following grammar into Greibach normal form :—

$$S \rightarrow AA/a$$

$$A \rightarrow SS/b.$$

10

15. (a) Show that the following language is not a CFL :—

$$\{0^i 1^j \mid j = i^2\}.$$

5

(b) Design a Turing machine to accept the language :

$$L = \{a^n b^n \mid n \geq 1\}.$$

5

16. Consider the CFG :

$$S \rightarrow A_1 A_2 \mid A_2 A_3$$

$$A_1 \rightarrow A_2 A_1 \mid 0$$

$$A_2 \rightarrow A_3 A_3 \mid 1$$

$$A_3 \rightarrow A_1 A_2 \mid 0$$

and using the CYK algorithm test 10010 is a member or not.

10

17. Write short notes on :

(a) Recursively enumerable languages

(b) Halting problem

(c) Restricted Turing machines.

10